



Pearson
Edexcel

Mark Scheme (Results)

Summer 2025

Pearson Edexcel International Advanced Level
in Decision Mathematics D1 (WDM11) Paper 01

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

EDEXCEL GCE MATHEMATICS

General Instructions for Marking

1. The total number of marks for the paper is 75.
2. The Edexcel Mathematics mark schemes use the following types of marks:
 - **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
 - **A** marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
 - **B** marks are unconditional accuracy marks (independent of M marks)
 - Marks should not be subdivided.
3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod – benefit of doubt
 - ft – follow through
 - the symbol \checkmark will be used for correct ft
 - cao – correct answer only
 - cso - correct solution only. There must be no errors in this part of the question to obtain this mark
 - isw – ignore subsequent working
 - awrt – answers which round to
 - SC: special case
 - oe – or equivalent (and appropriate)
 - dep – dependent
 - indep – independent
 - dp decimal places
 - sf significant figures
 - * The answer is printed on the paper
 - \square The second mark is dependent on gaining the first mark
4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
 6. If a candidate makes more than one attempt at any question:
 - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
 - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
 7. Ignore wrong working or incorrect statements following a correct answer.

| Question | Scheme | Marks |
|------------------|--|-------|
| 1 (a) | (180 + 300 + 250 + 410 + 240 + 120 + 230 + 310 + 190)/600 = 3.72 | M1 |
| | Lower bound = 4 | A1 |
| | | (2) |
| (b) | Van 1: 180 300 120 | M1 |
| | Van 2: 250 240 | |
| | Van 3: 410 190 | |
| | Van 4: 230 310 | A1 |
| | | (2) |
| (4 marks) | | |
| Notes | | |
| a1M1 | Calculates (2230 +/-410)/ 600 a calculation using the sum of the activities (accept a total in the range 1820 – 2640) (accept 3.71 as correct truncated value). This can be awarded for sight of the calculation or awrt 3.7 | |
| a1A1 | CAO – must follow from a correct calculation or decimal (rounded or truncated), so we must see either 2230/600 o.e. or awrt 3.7 - an answer of 4 with no working scores M0 | |
| b1M1 | The correct first five items placed correctly (the bold values) and at least seven values placed in bins (allow repeated values). Condone cumulative totals or calculation of the remaining space for M1 only | |
| b2A1 | CSO | |

| Question | Scheme | Marks |
|---|---|--|
| <p style="text-align: center;">2</p> <p>(a)</p> | <p>PR PU UV PQ RS ST</p> <p style="margin-left: 20px;"><u>PR</u> 8</p> | <p style="text-align: center;">M1</p> <p style="text-align: center;">A1</p> |
| | | (2) |
| <p>(b)</p> | <p>“540” x 2 = 1080 (metres)</p> | <p style="text-align: center;">M1</p> <p style="text-align: center;">A1ft</p> |
| | | (2) |
| <p>(c)</p> | <p>PRSTUVQP</p> <p>880 (metres)</p> | <p style="text-align: center;">M1</p> <p style="text-align: center;">A1</p> <p style="text-align: center;">A1</p> |
| | | (3) |
| <p>(d)</p> | <p>$540 - 75 + (75 + 180) = 720$ (metres)</p> | <p style="text-align: center;">M1</p> <p style="text-align: center;">A1</p> |
| | | (2) |
| | | (9 marks) |

| Notes | |
|---------------|--|
| a1M1 | Prim - first three arcs correctly chosen in order (PR, PU, UV, ...) or first four nodes {P, R, U, V, ...}. If any explicit rejections seen at some point then M1 (max) only. Order of nodes may be seen at the top of a matrix/table {1, -, 2, -, -, 3, 4 }. Starting at any other node can score M1 only for first three arcs chosen correctly |
| a1A1 | CSO – all arcs correctly stated and chosen in the correct order (with no additional arcs). They must be considering arcs for this mark (do not accept a list of nodes or numbers across the top of the matrix unless the correct list of arcs (in the correct order) is also seen) |
| b1M1 | Calculates the weight of their MST and doubles If their MST is incorrect, follow through the total for their tree (must be exactly 6 arcs) |
| b1A1ft | 1080 or 2 x “their 540” (if any subsequent calculations are seen do not isw this is A0) (1080 implies both marks) |
| c1M1 | NN route attempted, first five nodes correct PRSTU (accept arcs for this mark PR, RS, ST, TU, ...) (do not accept numbering across the matrix here unless nodes or arcs are stated in the correct order) |
| c1A1 | CAO – Route correct including return to P (accept arcs PR, RS, ST, TU, UV, VQ, QP) (condone if arcs stated alphabetically instead of in route order) |
| c2A2 | CAO – 880 (metres) (if they double the length of the NN route do not isw, this is A0) |
| d1M1 | Their “540” – 75 + two shortest from T (a new calculation to find the RMST may be seen e.g. new table with T deleted and a new MST calculation, with the correct 5 arcs circled PR PU UV PQ RS plus two shortest from T) |
| d1A1 | CAO – A final answer of 720 implies both marks (if additional calculations seen do not isw) |

| Question | Scheme | Marks | |
|------------------|--|---|------------|
| 3. (i)(a) | <p data-bbox="199 248 379 282">Middle Right</p> <p data-bbox="1233 322 1299 356">Pivot</p> <p data-bbox="284 416 1286 450">28 18 50 27 48 8 <u>25</u> 12 56 31 33 42 25</p> <p data-bbox="284 510 1299 544">18 <u>8</u> 12 25 28 50 27 48 <u>56</u> 31 33 42 8, 56</p> <p data-bbox="284 604 1299 638">8 18 <u>12</u> 25 28 50 27 <u>48</u> 31 33 42 56 12, 48</p> <p data-bbox="284 698 1347 732">8 12 18 25 28 27 <u>31</u> 33 42 48 50 56 (18), 31, (50)</p> <p data-bbox="284 792 1299 826">8 12 18 25 28 <u>27</u> 31 33 <u>42</u> 48 50 56 27, 42</p> <p data-bbox="284 887 1150 920">8 12 18 25 27 28 31 33 42 48 50 56</p> <p data-bbox="199 954 352 987">Middle Left</p> <p data-bbox="1233 1028 1299 1061">Pivot</p> <p data-bbox="284 1122 1270 1155">28 18 50 27 48 <u>8</u> 25 12 56 31 33 42 8</p> <p data-bbox="284 1216 1286 1249">8 28 18 50 27 48 <u>25</u> 12 56 31 33 42 25</p> <p data-bbox="284 1310 1299 1344">8 <u>18</u> 12 25 28 50 27 <u>48</u> 56 31 33 42 18, 48</p> <p data-bbox="284 1404 1335 1438">8 12 18 25 28 27 <u>31</u> 33 42 48 <u>50</u> 56 (12), 31, 50</p> <p data-bbox="284 1498 1335 1532">8 12 18 25 <u>28</u> 27 31 <u>33</u> 42 48 50 56 28, 33, (56)</p> <p data-bbox="284 1592 1150 1626">8 12 18 25 27 28 31 33 42 48 50 56</p> | <p data-bbox="1481 344 1528 378">M1</p> <p data-bbox="1481 490 1528 524">A1</p> <p data-bbox="1481 584 1544 618">A1ft</p> <p data-bbox="1481 725 1528 759">A1</p> | |
| | | | (4) |

| | | |
|-------------------------|---|--|
| <p>(i)(b)</p> | <p>8 12 18 25 27 28 31 33 42 48 50 56 Pivot 31</p> <p>31 < 40 so discard 31 and below</p> <p style="text-align: right;">33 42 48 50 56 Pivot 48</p> <p>48 > 40 so discard 48 and above</p> <p style="text-align: right;">33 42 Pivot 42</p> <p>42 > 40 so discard 42</p> <p style="text-align: right;">33</p> <p>33 ≠ 40 so 40 is not in the list</p> | <p>M1</p> <p>A1</p> <p>A1</p> |
| | <p>Alternatively</p> <p>56 50 48 42 33 31 28 27 25 18 12 8 Pivot 28</p> <p>28 < 40 so discard 28 and below</p> <p>56 50 48 42 33 31 Pivot 42</p> <p>42 > 40 so discard 42 and above</p> <p style="text-align: right;">33 31 Pivot 31</p> <p>31 < 40 so discard 31</p> <p style="text-align: right;">33</p> <p>33 ≠ 40 so 40 is not in the list</p> | <p>(3)</p> |
| <p>(ii)</p> | <p>$x > 15$ or $x < 19$ o.e. $x > 15$ and $x < 19$ leading to $15 < x < 19$ or $16 \leq x \leq 18$ o.e.</p> | <p>B1 B1</p> |
| | | <p>(2)</p> |
| <p>(9 marks)</p> | | |

Notes

| | |
|----------------|--|
| ia1M1 | Quick sort using all 12 numbers (condone one item error or omission), pivot, p, chosen (must be choosing middle left or right – choosing first/last item as the pivot is M0). After the first pass the list must read (values less than the pivot), pivot, (values greater than the pivot). If only choosing one pivot per iteration then M1 only |
| ia1A1 | First and second passes correct, but not choice of pivots for 3 rd pass |
| ia2A1ft | Third and fourth passes correct following through from their second pass and choice of pivots for the third pass. The pivots for the third, and fourth passes must be consistent (so all MR or all ML) |
| ia3A1 | CSO (correct solution only – all previous marks in this part must have been awarded) including a fifth pass (with both 27 and 42 chosen as pivots MR or both 28 and 33 chosen as pivots ML) |
| | Special Case for (a) If the candidate sorts into descending order they can score M1 as per the main scheme (but with the values either side of the pivot reversed), A1 for a fully correct sort then A0 A0 even if the list is reversed at the end (so 2 marks max.). See below |
| ib1M1 | Correct choice of pivot (must be using MR) (31 ascending or 28 descending) and discards 8 to 31 or 28 (must be using the sorted list, but could be sorted into either ascending or descending order) It must be clear which values are being discarded or the reduced list must be shown. If pivots are retained, this will score M1 only. Candidates may either compare with the actual values or the positions of items in a correctly sorted list. The actual rejections may be shown as values from the list or the positions in the list. (If they do not not have the correct 12 numbers in their sorted list in (a) they can score M1 only for using their sorted list here) |
| ib1A1 | 2 nd and 3 rd pass correct choice of pivots and discards (if pivot not discarded A0) |
| ib2A1 | CSO - Final pass correct, compares with 33 and concludes 40 is not in list |
| ii1B1 | One inequality correct – if a list of inequalities is seen, they must clearly select from this list otherwise B0 |
| ii2B1 | Both inequalities correct and combined to give a range of values (accept either form or list of values 16, 17, 18) (SC if just 16, 17, 18 seen accept this for both marks) (accept interval notation either (15, 19) or [16, 18]) |

Special Case Descending Max M1 A1 A0 A0

Middle Right

Pivot

| | | | | | | | | | | | | |
|-----------|-----------|-----------|----|-----------|-----------|-----------|-----------|-----------|-----------|-----------|----------|----------------|
| 28 | 18 | 50 | 27 | 48 | 8 | <u>25</u> | 12 | 56 | 31 | 33 | 42 | 25 |
| 28 | 50 | 27 | 48 | <u>56</u> | 31 | 33 | 42 | 25 | 18 | <u>8</u> | 12 | 56, 8 |
| 56 | 28 | 50 | 27 | <u>48</u> | 31 | 33 | 42 | 25 | 18 | <u>12</u> | 8 | 48, 12 |
| 56 | <u>50</u> | 48 | 28 | 27 | <u>31</u> | 33 | 42 | 25 | <u>18</u> | 12 | 8 | (50), 31, (18) |
| 56 | 50 | 48 | 33 | <u>42</u> | 31 | 28 | <u>27</u> | 25 | 18 | 12 | 8 | 42, 27 |
| 56 | 50 | 48 | 42 | 33 | 31 | 28 | 27 | 25 | 18 | 12 | 8 | |

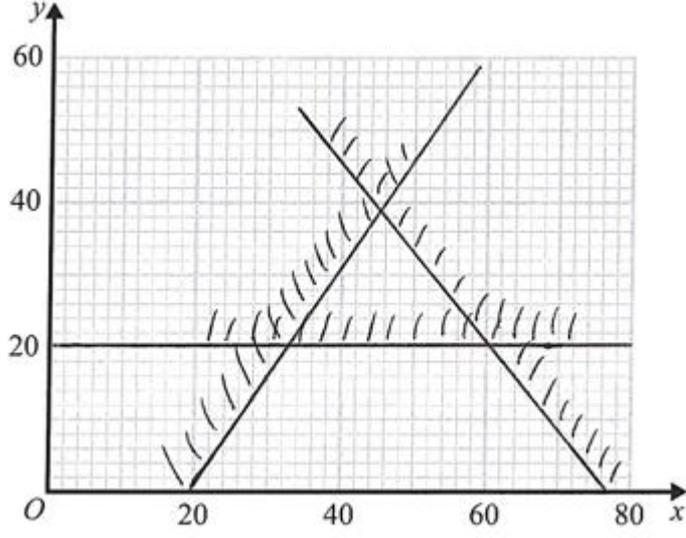
Middle Left

Pivot

| | | | | | | | | | | | | |
|-----------|-----------|-----------|-----------|----|-----------|-----------|----|-----------|-----------|-----------|----------|--------------|
| 28 | 18 | 50 | 27 | 48 | <u>8</u> | 25 | 12 | 56 | 31 | 33 | 42 | 8 |
| 28 | 18 | 50 | 27 | 48 | <u>25</u> | 12 | 56 | 31 | 33 | 42 | 8 | 25 |
| 28 | 50 | 27 | <u>48</u> | 56 | 31 | 33 | 42 | 25 | <u>18</u> | 12 | 8 | 48, 18 |
| <u>50</u> | 56 | 48 | 28 | 27 | <u>31</u> | 33 | 42 | 25 | 18 | <u>12</u> | 8 | 50, 31, (12) |
| 56 | 50 | 48 | <u>33</u> | 42 | 31 | <u>28</u> | 27 | 25 | 18 | 12 | 8 | 33, 28 |
| 56 | 50 | 48 | 42 | 33 | 31 | 28 | 27 | 25 | 18 | 12 | 8 | |

| Question | Scheme | Marks |
|------------------------------------|--|--|
| <p>4. (a)(i)</p> | <p>Fastest route: ACBEFGJH</p> | <p>M1 A1 (ACB D)</p> <p>A1 (EFG)</p> <p>A1ft (JH)</p> <p>A1</p> |
| <p>(ii)</p> | <p>Fastest time: 53 (minutes)</p> | <p>A1ft</p> |
| | | <p>(6)</p> |
| <p>(b)</p> | <p>Either calculates new fastest route $AF(35) + FH(22) = 57$ Or calculates the change to sections of the route e.g. ACDF compared with ACBEF and FGJH compared with FJH</p> <p>Difference $57 - "53" = 4$ (minutes) or $2 + 2 = 4$ (minutes)</p> | <p>M1</p> <p>A1ft</p> |
| | | <p>(2)</p> |
| <p>(8 marks)</p> | | |

| Notes | |
|----------------|---|
| | <p>In (a) it is important that all values at each node are checked very carefully – the order of the working values must be correct for the corresponding A mark to be awarded e.g. at E the working values must be 27 26 in that order (so 26 27 is incorrect)</p> <p>It is also important that the order of labelling is checked carefully. The order of labelling must be a strictly increasing sequence – so 1, 2, 3, 3, 4, ... will be penalised once (see notes below) but 1, 2, 3, 5, 6, ... is fine. Errors in the final values and working values are penalised before errors in the order of labelling</p> |
| ai1M1 | A larger value replaced by a smaller value at least twice in the working values at either B, D, E, F, G, H, J |
| ai1A1 | All values at A, C, B and D correct and the working values in the correct order |
| ai2A1 | All values at E, F and G correct and the working values in the correct order |
| ai3A1ft | All values in J and H correct on the follow through and the working values in the correct order. To follow through J check that the working values at J follow from the candidate's final values for the nodes that are directly attached to J (which are F and G). For example, if correct then the order of labelling of nodes F and G are 6 and 7 respectively so the working values at J should come from F and G in that order. The first working value at J should be their 50 (the Final value at F) + 17 (the weight of the arc FJ), the second working value at J should be their 48 (the Final value at G) + G (the weight of the arc GJ). Repeat the process for H (which will have working values from E, F and J with the order of these nodes determined by the candidate's order of labelling at E, F and J) |
| ai4A1 | CAO |
| aiiA1ft | Follow through their final value at H only – if answer is 53 but the final value at H is not 53 then A0 (condone lack of minutes) |
| bM1 | <p>Either calculates the revised time of 57 minutes</p> <p>Or compares the route in stages e.g. ACBEF against ACDF difference 2 and FGJH against FJH difference 2. If their final value at H is not 53 follow through their final value at F and shortest from F to H for these calculations</p> |
| bA1ft | 4 (minutes) (may be seen as $2 + 2 = 4$) or follow through 57 - their fastest to H (which may be in sections AF + FH) |

| Question | Scheme | Marks |
|--------------|--|--|
| 5 (a) | Maximise ($P = $) $x + y + z$ | B1 |
| | | (1) |
| (b) | $12.50x + 10y + 15z \leq 1400$ $\Rightarrow 5x + 4y + 6z \leq 560$ * | M1 A1 |
| | | (2) |
| (c) | $x \geq \frac{40}{100}(x + y + z)$ $\Rightarrow 3x \geq 2y + 2z$ | M1 A1 |
| | $3y \leq 2z$ | B1 |
| | | (3) |
| (d) | $3x \geq 2y + 2 \times 30$ $\Rightarrow 3x - 2y \geq 60$ * | M1 A1 |
| | | (2) |
| (e) |  <p data-bbox="367 1691 957 1758">Optimal point (60, 20) 60 red (rose bushes), 20 yellow (rose bushes)</p> | M1 A1 A1 A1 |
| | | (4) |
| | | (12 marks) |

| Notes | |
|--------------|--|
| aB1 | CAO – must have maximise (accept max but not maximum) and $x + y + z$ |
| bM1 | Forms inequality using the costs and attempts to simplify. If a correct equation is formed and then changed to an inequality this is M1 A0 |
| bA1 | CSO * |
| cM1 | Attempts to form inequality with either 0.4 or 40/100 (o.e. fraction) combined with $(x + y + z)$. Accept any inequality or equals for this mark |
| cA1 | CAO – fully simplified with integer coefficients |
| cB1 | CAO |
| dM1 | Substitutes $z = 30$ into their $3x \geq 2y + 2z$ and attempts to simplify (Allow recovery if their inequality is not fully simplified e.g. $6x \geq 4y + 4z$) |
| dA1 | CSO * |
| eM1 | Draws at least two of the three lines with at least one correct (Condone no consideration of $y \geq 0$) |
| e1A1 | Any two lines correct $y = 20$ $5x + 4y = 380$ passes through (60, 20) and (76, 0) $3x - 2y = 60$ passes through (20, 0) and (40, 30) (must be within $\frac{1}{2}$ small square from these points) |
| e2A1 | All three lines correct |
| e3A1 | CSO – must have drawn the correct region (we do not require shading or for the feasible region to be marked with R , but if this is done, the region selected must be correct) The answer must be in context so $x = 60, y = 20$ is A0 Accept 60 red and 20 yellow with no mention of rose bushes. We do not need to see any mention of white roses here. |

| Question | Scheme | Marks |
|---|---|---|
| 6 (a) | Considers pairings of nodes F, J, K and M $FJ + KM = 32 + 14 = 46$ $FK + JM = 15 + 26 = 41$ $FM + JK = 13 + 17 = 30$ Repeat FG GM JL LK Total length = $338 + 30 = 368$ (km) | M1 A1 A1 A1 A1ft |
| | Special Case Max M1 A1 A0 A0 A0 Considers pairings of A, F, K and M $AF + KM = 26 + 14 = 40$ $AK + FM = 41 + 13 = 54$ $AM + FK = 39 + 15 = 54$ | |
| | | (5) |
| (b) | Now only repeat needed is KM, length 14 e.g. New length $338 + 18 + 14 = 370$ (km) (Increases length by) 2 (km) | M1 A1 (2) |
| (7 marks) | | |
| Notes | | |
| a1M1 | The correct three pairings of the correct four nodes F, J, K and M with one row correct (including total) | |
| a1A1 | Two rows correct including pairings and totals | |
| a2A1 | All three rows correct including pairings and totals | |
| a3A1 | CAO for the repeated arcs | |
| a4A1ft | $338 +$ their smallest from a choice of three totals | |
| M1 A1 A0 A0 A0 | Special Case – considers A, F, K, M M1 Three pairings of the four nodes with one row correct (including total) A1 All three rows correct including pairings and totals A0 No further marks available A0 A0 | |
| b1M1 | Considers KM (may be implied by a correct calculation) as only pair of odd nodes and calculates new length $338 + 18 + 14$ or calculates $18 + 14$ as new additional length | |
| b1A1 | CAO – 2 (km) (must not come from any incorrect working) | |

| Question | Scheme | | | | Marks |
|----------------------|----------|-----|----------|-----|--|
| <p>7.</p> <p>(a)</p> | Activity | IPA | Activity | IPA | <p>B1 (DEFGH)</p> <p>B1 (IJK)</p> <p>B1 (LMN)</p> |
| | A | - | H | B C | |
| B | - | I | D E | | |
| C | - | J | F | | |
| D | A B | K | F | | |
| E | B | L | F G H | | |
| F | B | M | I J | | |
| G | B | N | K L | | |
| | | | | | (3) |
| <p>(b)</p> | | | | | <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> |
| | | | | | (4) |

| | | |
|-------------------|---|--|
| (c) | Lower bound = $(8+12+14+6+4+8+8+5+7+2+6+6+6+4)/31 = 96/31 = 3.1$ Therefore 4 workers required | M1 A1 |
| | | (2) |
| (d) | <p>The Gantt chart displays activities A through N on a timeline from 0 to 32. Activity A (0-8), B (0-12), C (0-14), D (12-18), E (12-16), F (12-20), G (12-18), H (14-20), I (20-26), J (20-24), K (20-26), L (20-26), and N (26-30). Shaded vertical bars indicate worker requirements at intervals: 8-12 (1 worker), 14-16 (1 worker), 16-18 (1 worker), 18-20 (1 worker), 20-22 (1 worker), 22-24 (1 worker), 24-26 (1 worker), 26-28 (1 worker), and 28-30 (1 worker).</p> | M1 A1 A1 A1 |
| | | (4) |
| (e) | At $13 < t < 14$ activities D, C, F and G must be happening and at $16 < t < 17$ activities D, F, G and H must be happening. Also activity E must be happening at either $13 < t < 14$ or $16 < t < 17$ so a total of five workers | M1 A1 A1 |
| | | (3) |
| (16 marks) | | |

| Notes | |
|--------------|---|
| a1B1 | Activities D, E, F, G and H correct |
| a2B1 | Activities I, J and K correct |
| a3B1 | Activities L, M and N correct |
| b1M1 | All top boxes complete, values generally increasing in the direction of the arrows ('left to right'), condone one rogue value which is a number in a top box greater than the subsequent value |
| b1A1 | CAO (top boxes) |
| b2M1 | All bottom boxes complete, values generally decreasing in the opposite direction of the arrows ('right to left'), condone one rogue value which is a number in a bottom box greater than the previous value. Condone missing 0 and/or their 31 (at the end event) for the M mark only |
| b2A1 | CAO (bottom boxes) |
| c1M1 | Calculates $96 (+/-14)/31$ – a calculation using the sum of the activities (accept a total in the range 82 – 110) divided by their finish time or sight of awrt 3.1 |
| c1A1 | 4 workers but must follow from a correct calculation (awrt 3.1) with no incorrect working seen (note an answer of 4 with no working is M0) |
| d1M1 | <u>Cascade Chart not a schedule.</u> At least 9 activities including at least 5 floats |
| d1A1 | Critical activities (BDIM) and at least 3 non-critical activities correct |
| d2A1 | At least 7 non-critical activities correct |
| d3A1 | CAO All 14 activities present (just once). No errors. |
| e1M1 | A statement mentioning one of the following <ul style="list-style-type: none"> • 4 workers, 4 of D C E F G stated and time 13 – 14 • 4 workers, 4 of D E F G H stated and time 16 – 17 • 5 workers, either D C E F G or D E F G H stated and any time interval |
| e1A1 | A correct statement of 5 workers with details of both the time and activities for one of the intervals. Candidates must give a time within one of the correct intervals. Either $13 < t < 14$, e.g. 13.5 (or 'on/during day 14') and state the correct activities D, C, E, F and G or $16 < t < 17$ (or e.g. 16.5 or 'on/during day 17') and the correct activities D, E, F, G and H. Please note an inequality for the time interval implying a time of 13, 14, 16 or 17 is incorrect. Answers given as an interval of time are acceptable provided the time interval stated is correct for all its possible values (e.g. time 13 – 14 or 'between 13 and 14' is A0) |
| e2A1 | A fully correct statement mentioning both intervals and both correct groups of activities and stating 5 workers |

| Question | Scheme | Marks |
|------------------------------------|---|---|
| <p>8.</p> <p>(a)</p> | $y \leq 2x + 5$ $x + 5y \leq 150$ $2x + y \leq 70$ $5y \geq 3x - 15$ | <p>B1</p> <p>B1</p> <p>(2)</p> |
| <p>(b)</p> | $3x + 2y = 48 \qquad x + 5y = 150$ $5y = 3x - 15 \Rightarrow \left(\frac{90}{7}, \frac{33}{7}\right) \quad 2x + y = 70 \Rightarrow \left(\frac{200}{9}, \frac{230}{9}\right)$ $\frac{90}{7}a + \frac{33}{7}b = \frac{1419}{7} \Rightarrow 30a + 11b = 473$ $\frac{200}{9}a + \frac{230}{9}b = \frac{1730}{3} \Rightarrow 20a + 23b = 519$ $a = 11 \quad b = 13 \quad \text{or} \quad P = 11x + 13y$ | <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>(4)</p> |
| <p>(c)</p> | <p>Considers the gradient of $Q = 3x + 2y$ and attempts to find a limiting value for k</p> <p>Considers the gradient of $Q = 2x + y$ and attempts to find a limiting value for k</p> <p>e.g.</p> $-\frac{1}{k} < -\frac{3}{2} \quad \text{and} \quad -\frac{1}{k} > -2$ $\Rightarrow k < \frac{2}{3} \quad \text{or} \quad k > \frac{1}{2}$ $\frac{1}{2} < k < \frac{2}{3}$ | <p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p> |

| | | |
|--------------------------|---|--|
| | <p>Alternative 1</p> <p>Compares value of objective function at A and E Compares value of objective function at C and D</p> $\frac{38}{7} + \frac{111}{7}k < \frac{90}{7} + \frac{33}{7}k \Rightarrow k < \frac{2}{3}$ $\frac{200}{9} + \frac{230}{9}k > \frac{365}{13} + \frac{180}{13}k \Rightarrow k > \frac{1}{2} \text{ giving } \frac{1}{2} < k < \frac{2}{3}$ | <p>M1 M1</p> <p>A1</p> <p>A1</p> |
| | <p>Alternative 2</p> <p>Rearranges $3x + 2y = 48$ to compare with $x + ky$ Rearranges $2x + y = 70$ to compare with $x + ky$</p> $x + \frac{2}{3}y = 16 \Rightarrow k < \frac{2}{3}$ $x + \frac{1}{2}y = 35 \Rightarrow k > \frac{1}{2} \quad \frac{1}{2} < k < \frac{2}{3}$ | <p>M1 M1</p> <p>A1 A1</p> |
| | | <p>(4)</p> |
| | <p>For reference the coordinates of all points of intersection</p> <p>A $\left(\frac{38}{7}, \frac{111}{7}\right)$ $3x + 2y = 48$ and $y = 2x + 5$</p> <p>B $\left(\frac{125}{11}, \frac{305}{11}\right)$ $y = 2x + 5$ and $x + 5y = 150$</p> <p>C $\left(\frac{200}{9}, \frac{230}{9}\right)$ $x + 5y = 150$ and $2x + y = 70$</p> <p>D $\left(\frac{365}{13}, \frac{180}{13}\right)$ $2x + y = 70$ and $5y = 3x - 15$</p> <p>E $\left(\frac{90}{7}, \frac{33}{7}\right)$ $5y = 3x - 15$ and $3x + 2y = 48$</p> | |
| <p>(10 marks)</p> | | |

| Notes | |
|--------------|---|
| a1B1 | Any two inequalities correct (accept equivalent rearrangements) |
| a2B1 | CAO – all four correct (ignore any mention of $3x + 2y \geq 48$ (SC B1 B0 for all four strict inequalities) |
| b1M1 | Attempts to solve both correct pairs of simultaneous equations (candidates may use their calculator to solve these, so the correct values for both points implies both marks) Ignore any additional work to find other points of intersection |
| b1A1 | CAO – both pairs of coordinates (accept awrt (12.9, 4.7) and (22.2, 25.6)) Ignore additional points of intersection |
| b2M1 | Forms a pair of simultaneous equations using their minimum and maximum points and solves to obtain a and b (may be unsimplified). If they have calculated additional points of intersection, then they must use their answer for the correct two points here |
| b2A1 | CAO – must be exact values (either stating a and b or as function $P =$) |
| c1M1 | Considers $3x + 2y$ and attempts to find a value for k by comparing gradients or compares the value of the objective function at A and E (accept the use of m for $-1/k$ to compare gradients even if not clearly defined) |
| c2M1 | Considers $2x + y$ and attempts to find a value for k by comparing gradients or compares the value of the objective function at C and D |
| c1A1 | Either $k < \frac{2}{3}$ or $k > \frac{1}{2}$ (allow use of \leq and \geq) (If gradients are compared please check inequalities carefully to ensure that any working shown is fully correct) (this mark can be awarded following either of the M marks so M0 M1 A1 A0 or M1 M0 A1 A0 are possible) |
| c2A1 | Both values correct and correct interval stated (allow use of \leq) (both M marks must be awarded and must not come from incorrect working) |

