

**INTERNATIONAL A-LEVEL  
MATHEMATICS**

**MA05**

(9660/MA05) Unit M2 Mechanics

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Mark scheme

January 2025

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**Key to mark scheme abbreviations**

<b>M</b>	Mark is for method
<b>m</b>	Mark is dependent on one or more M marks and is for method
<b>A</b>	Mark is dependent on M or m marks and is for accuracy
<b>B</b>	Mark is independent of M or m marks and is for method and accuracy
<b>E</b>	Mark is for explanation
<b>√ or ft</b>	Follow through from previous incorrect result
<b>CAO</b>	Correct answer only
<b>CSO</b>	Correct solution only
<b>AWFW</b>	Anything which falls within
<b>AWRT</b>	Anything which rounds to
<b>ACF</b>	Any correct form
<b>AG</b>	Answer given
<b>SC</b>	Special case
<b>oe</b>	Or equivalent
<b>A2, 1</b>	2 or 1 (or 0) accuracy marks
<b>-x EE</b>	Deduct x marks for each error
<b>NMS</b>	No method shown
<b>PI</b>	Possibly implied
<b>SCA</b>	Substantially correct approach
<b>sf</b>	Significant figure(s)
<b>dp</b>	Decimal place(s)
<b>ISW</b>	Ignore subsequent working



Q	Answer	Marks	Comments
1(b)	Work done against the resistance force  $W = kv^{\frac{9}{4}} \times (vt)$  $W = 6.53 \times 18^{\frac{9}{4}} \times (18 \times 30)$  $W = 4357.89... \times 540$  $W = 2.4 \times 10^6 \text{ [J]}$	M1          A1	Note: unrounded answer is $W = 2.353082432 \times 10^6 \text{ [J]}$ if unrounded value for $k$ is used <b>AWRT</b> $2.4 \times 10^6 \text{ [J]}$
		2	

Q	Answer	Marks	Comments
1(c)	At maximum speed, resultant force is zero  $\frac{P}{v} = kv^{\frac{9}{4}}$  $\frac{P}{k} = v^{\frac{13}{4}}$  $v = \left(\frac{P}{k}\right)^{\frac{4}{13}}$  $v = \left(\frac{345 \times 10^3}{6.53}\right)^{\frac{4}{13}} \left[ = (52833.07...)^{\frac{4}{13}} \right]$  $v = 28 \text{ [m s}^{-1}\text{]}$	M1          A1	Note: unrounded answer is $28.39304389 \text{ m s}^{-1}$ if $k = 6.529... \text{ used}$ <b>AWRT</b> 28
		2	

	<b>Question 1 Total</b>	<b>7</b>	
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Q	Answer	Marks	Comments
2(a)	$82 = 100\cos\alpha$	<b>M1</b>	Use of equilibrium perpendicular to slope, with at least one side correct
	$\cos\alpha = \frac{82}{100}$ $\alpha = 35^\circ$	<b>A1</b>	<b>CAO</b> to nearest degree
		<b>2</b>	

Q	Answer	Marks	Comments
2(b)	$F = 100\sin\alpha$	<b>M1</b>	Use of equilibrium parallel to slope, with at least one side correct <b>ft</b> their $\alpha$
	$F = 57 \text{ [N]}$	<b>A1ft</b>	<b>ft</b> their $\alpha$ <b>AWRT</b> 57
		<b>2</b>	

Q	Answer	Marks	Comments
2(c)	$F = \mu R$		
	$\mu = \frac{F}{R} = \frac{57}{82}$ $\mu = 0.70$	<b>B1</b>	<b>oe</b> <b>AWRT</b> 0.7 Condone one significant figure answer
		<b>1</b>	

	<b>Question 2 Total</b>	<b>5</b>	
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Q	Answer	Marks	Comments
3(b)(i)	$\mathbf{r} = 0.3\cos(3t)\mathbf{i} + 0.3\sin(3t)\mathbf{j}$ $\mathbf{v} = -0.9\sin(3t)\mathbf{i} + 0.9\cos(3t)\mathbf{j}$	M1 A1	<b>M1:</b> At least one component correct <b>A1:</b> Both components correct
		2	

Q	Answer	Marks	Comments
3(b)(ii)	$\mathbf{v} = -0.9\sin(3t)\mathbf{i} + 0.9\cos(3t)\mathbf{j}$ $\mathbf{a} = -2.7\cos(3t)\mathbf{i} - 2.7\sin(3t)\mathbf{j}$ $\mathbf{F} = -54\cos(3t)\mathbf{i} - 54\sin(3t)\mathbf{j}$	M1 A1  A1ft	<b>M1:</b> At least one component correct <b>ft</b> their velocity vector <b>A1:</b> Both components correct  <b>ft</b> their acceleration vector
		3	

	<b>Question 3 Total</b>	<b>9</b>	
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Q	Answer	Marks	Comments
4(a)	$x = (u \cos \alpha)t$ $y = (u \sin \alpha)t - \frac{1}{2}gt^2$ $t = \frac{x}{u \cos \alpha}$ $y = (u \sin \alpha) \times \frac{x}{u \cos \alpha} - \frac{1}{2}g \times \left(\frac{x}{u \cos \alpha}\right)^2$ $(u \sin \alpha) \times \frac{x}{u \cos \alpha} = x \tan \alpha$ $-\frac{1}{2}g \times \left(\frac{x}{u \cos \alpha}\right)^2 = -\frac{gx^2}{2u^2} \times \frac{1}{\cos^2 \alpha}$ $-\frac{gx^2}{2u^2} \times \frac{1}{\cos^2 \alpha} = -\frac{gx^2}{2u^2} \sec^2 \alpha$ $y = x \tan \alpha - \frac{gx^2}{2u^2} \sec^2 \alpha$ $\frac{g \sec^2 \alpha}{2u^2} x^2 - x \tan \alpha + y = 0$	<p><b>B1</b></p> <p><b>B1</b></p> <p><b>M1 A1</b></p> <p><b>A1</b></p>	<p><b>oe</b></p> <p><b>M1:</b> Eliminates <math>t</math> in both terms with at least one term correct  <b>A1:</b> All correct</p> <p><b>AG</b> Must be convincingly shown</p>
		<b>5</b>	

Q	Answer	Marks	Comments
4(b)(i)	$\frac{9.8 \sec^2(60^\circ)}{2 \times 15^2} x^2 - x \tan(60^\circ) + 7 = 0$	M1	Forms a three-term quadratic equation by substituting in the values of $g$ , $u$ and $\alpha$ PI by two correct times, <b>AWRT</b> 1.9 and <b>AWRT</b> 0.75
	$\frac{98}{1125} x^2 - \sqrt{3} x + 7 = 0$		0.087111... $x^2 - 1.732...x + 7 = 0$
	$x = 5.64 \text{ [m]}$	A1	<b>AWRT</b> 5.64
	$x = 14.2 \text{ [m]}$	A1	<b>AWRT</b> 14.2
		3	

Q	Answer	Marks	Comments
4(b)(ii)	$T = \frac{x_1}{u \cos \alpha} - \frac{x_2}{u \cos \alpha}$	M1	$T = 1.89... - 0.752$ Possible <b>ft</b> from 4(b)(i) PI by correct final answer
	$T = \frac{14.2 - 5.64}{15 \cos(60^\circ)}$		Unrounded answer is 1.1463... seconds
	$T = 1.1 \text{ [seconds]}$	A1	<b>AWRT</b> 1.1 Condone 1.15 but not 1.2
		2	

	<b>Question 4 Total</b>	<b>10</b>	
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Q	Answer	Marks	Comments
5(a)	40 [newtons]	<b>B1</b>	Condone omission of units
	There is zero resultant force on the rod in the horizontal direction	<b>E1</b>	Any correct reason
		<b>2</b>	

Q	Answer	Marks	Comments
5(b)	Anticlockwise moments about X		
	$25gd\cos(65^\circ) + 40 \times 3$	<b>B1</b>	Correct two-term anticlockwise moment expression
	Clockwise moments about X		
	$40 \times 11\sin(65^\circ) + 0.4 \times 40 \times 11\cos(65^\circ)$	<b>B1</b>	Correct two-term clockwise moment expression <b>PI</b> by 473.156... [N m]
	Principle of Moments		
	$25gd\cos(65^\circ) + 40 \times 3$ $= 40 \times 11\sin(65^\circ) + 0.4 \times 40 \times 11\cos(65^\circ)$	<b>M1</b>	Sets their anticlockwise moments equal to their clockwise moments <b>PI</b> by correct final answer
	$d = \frac{11 \times (40 \sin(65^\circ) + 16 \cos(65^\circ)) - 120}{25 \times 9.8 \times \cos(65^\circ)}$		
	$d = 3.4$ [m]	<b>A1</b>	Note: unrounded answer is 3.410770837 [m]
		<b>4</b>	

	<b>Question 5 Total</b>	<b>6</b>	
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Q	Answer	Marks	Comments
6(a)	The mass per unit area of the lamina is constant throughout the entire lamina	E1	Any valid explanation
		1	

Q	Answer	Marks	Comments
6(b)(i)	$\bar{X} = \frac{2 \times -5 + 4 \times 5 [+7 \times 0 + 6 \times 0]}{2 + 4 + 7 + 6}$	M1	Allow one error eg omission of lamina
	$\bar{X} = \frac{10}{19}$	A1	CAO in exact form
		2	

Q	Answer	Marks	Comments
6(b)(ii)	$\bar{Y} = \frac{7 \times d + 6 \times \frac{d}{3} [+2 \times 0 + 4 \times 0]}{2 + 4 + 7 + 6}$	M1	Allow one error eg omission of lamina
	$\bar{Y} = \frac{9d}{19}$	A1	CAO in exact form
		2	

Q	Answer	Marks	Comments
6(c)	$\tan(5^\circ) = \frac{\left(\frac{10}{19}\right)}{\left(\frac{9d}{19}\right)}$	M1 A1ft	M1: Correct LHS or their $\bar{X}$ divided by their $\bar{Y}$ A1ft: Fully correct, ft their $\bar{X}$ and their $\bar{Y}$
	$\tan(5^\circ) = \frac{10}{9d} \Rightarrow d = \frac{10}{9 \tan(5^\circ)}$		
	$d = 13$	A1	Note: unrounded answer is 12.70005811 AWRT 13 CSO
		3	

	<b>Question 6 Total</b>	<b>8</b>	
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Q	Answer	Marks	Comments
8(a)	Magnitude of Y's momentum if X <b>does not</b> change direction during the collision  Conservation of Momentum $19.2 + 7.5 = 2.4 + P_Y$ $P_Y = 24.3 \text{ [kg m s}^{-1}\text{]}$	<b>M1</b>  <b>A1</b>	Either conservation of momentum equation correct  <b>AWRT 24</b>
	Magnitude of Y's momentum if X <b>does</b> change direction during the collision  Conservation of Momentum $19.2 + 7.5 = -2.4 + P_Y$ $P_Y = 29.1 \text{ [kg m s}^{-1}\text{]}$	<b>A1</b>	<b>AWRT 29</b>
		<b>3</b>	

Q	Answer	Marks	Comments
8(b)	KE of Sphere X before collision  $KE = \frac{1}{2}mv^2 = \frac{1}{2} \times 2 \times \left(\frac{19.2}{2}\right)^2$ $KE = 92.16 \text{ [J]}$	<b>M1</b>	$KE = \frac{1}{2} \times 2 \times 9.6^2$
	KE of Sphere Y before collision  $KE = \frac{1}{2}mv^2 = \frac{1}{2} \times 5 \times \left(\frac{7.5}{5}\right)^2$ $KE = 5.625 \text{ [J]}$  Sum of KE before collision $E = 92.16 + 5.625$ $E = 97.785$	<b>M1</b>  <b>A1</b>	$KE = \frac{1}{2} \times 2 \times 1.5^2$  <b>AG</b> Must be convincingly shown
		<b>3</b>	



Q	Answer	Marks	Comments
9	$\mathbf{F} = (36t^2 - 18t)\mathbf{i} + (6\cos t - 24\sin 2t)\mathbf{j}$ $+ 3e^{-\frac{t}{3}}\mathbf{k}$ $\mathbf{a} = (12t^2 - 6t)\mathbf{i} + (2\cos t - 8\sin 2t)\mathbf{j}$ $+ e^{-\frac{t}{3}}\mathbf{k}$ $\mathbf{v} = (4t^3 - 3t^2)\mathbf{i} + (2\sin t + 4\cos 2t)\mathbf{j}$ $- 3e^{-\frac{t}{3}}\mathbf{k} + \mathbf{c}$ $\mathbf{v}(0) = 0\mathbf{i} + 4\mathbf{j} - 3\mathbf{k} + \mathbf{c} = \mathbf{0}$ $\mathbf{v} = (4t^3 - 3t^2)\mathbf{i} + (2\sin t + 4\cos 2t - 4)\mathbf{j}$ $+ \left(3 - 3e^{-\frac{t}{3}}\right)\mathbf{k}$ $\mathbf{r} = (t^4 - t^3)\mathbf{i} + (-2\cos t + 2\sin 2t - 4t)\mathbf{j}$ $+ \left(3t + 9e^{-\frac{t}{3}}\right)\mathbf{k} + \mathbf{c}$ $\mathbf{r}(0) = 0\mathbf{i} - 2\mathbf{j} + 9\mathbf{k} + \mathbf{c} = \mathbf{0}$ $\mathbf{r} = (t^4 - t^3)\mathbf{i} + (-2\cos t + 2\sin 2t - 4t + 2)\mathbf{j}$ $+ \left(3t + 9e^{-\frac{t}{3}} - 9\right)\mathbf{k}$ $\mathbf{r}(2) = 8\mathbf{i} - 6.681\dots\mathbf{j} + 1.620\dots\mathbf{k}$ $ \mathbf{r}(2)  = \sqrt{8^2 + (-6.681\dots)^2 + (1.620\dots)^2}$ $ \mathbf{r}(2)  = 10.5 \text{ [m]}$	<p><b>B1</b></p> <p><b>M1 A1ft</b></p> <p><b>M1</b></p> <p><b>A1</b></p> <p><b>M1 A1ft</b></p> <p><b>A1</b></p> <p><b>M1</b></p> <p><b>A1</b></p>	<p>Correct acceleration vector</p> <p><b>M1:</b> At least one component correct from their acceleration vector  <b>A1ft:</b> All components correct from their acceleration vector                      Condone omission of constant(s) of integration                      Substitutes <math>t = 0</math> into their velocity vector and sets equal to zero vector, <b>oe</b></p> <p>Correct velocity vector</p> <p><b>M1:</b> At least one component correct from their velocity vector  <b>A1ft:</b> All components correct from their velocity vector                      Condone omission of constant(s) of integration</p> <p>Correct position vector</p> <p>Substitutes <math>t = 2</math> into their 3-dimensional position vector</p> <p>Note: unrounded answer is 10.54830625 [m]</p>
<b>Question 9 Total</b>		<b>10</b>	