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I declare this is my own work.

INTERNATIONAL A-LEVEL MATHEMATICS

(9660/MA03) Unit P2 Pure Mathematics

Friday 17 January 2020 07:00 GMT Time allowed: 2 hours 30 minutes

Materials

- For this paper you must have the Oxford International AQA booklet of formulae and statistical tables (enclosed).
- You may use a graphics calculator.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 120.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- Show all necessary working: otherwise marks may be lost.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
11	
12	
13	
TOTAL	



Answer **all** questions in the spaces provided.

- 1 (a) (i) Express $5 \sin \theta - 12 \cos \theta$ in the form $R \sin(\theta - \alpha)$, where $R > 0$ and $0^\circ < \alpha < 90^\circ$, giving the value of α to the nearest 0.1°

[3 marks]

Answer _____

- 1 (a) (ii) Hence solve the equation

$$5 \sin \theta - 12 \cos \theta = -1$$

in the interval $-180^\circ < \theta < 180^\circ$, giving all solutions to the nearest 0.1°

[3 marks]

Answer _____



2 The function f is defined by

$$f(x) = \sin^{-1}(2x - 1)$$

2 (a) State the largest possible domain of f .

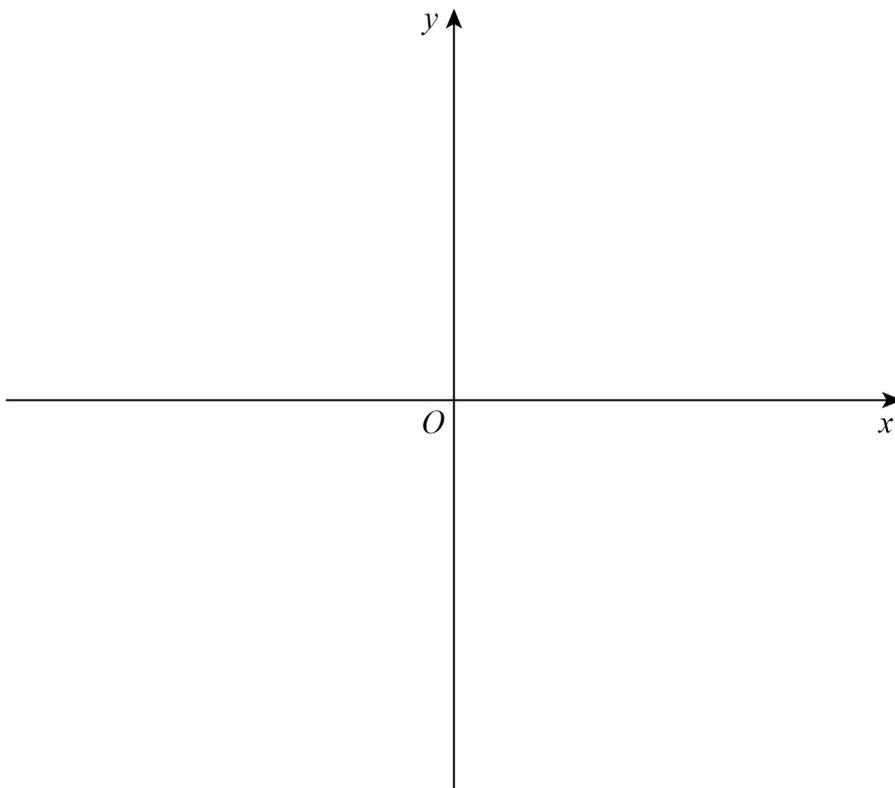
[1 mark]

Answer _____

2 (b) On the axes below, sketch the graph of $y = f(x)$.

Show the coordinates of the end-points on the graph.

[2 marks]



2 (e) Use the iterative formula

$$x_{n+1} = \frac{1 + \sin(1 - x_n)}{2} \quad \text{with } x_1 = 0.6$$

to find the values of x_2 and x_3 , giving your answers to three decimal places.

[2 marks]

Answer _____

11



5 (a) Express $\frac{12}{9-u^2}$ in the form $\frac{A}{3-u} + \frac{B}{3+u}$

[2 marks]

Answer _____



- 6 (a) (i)** Find the binomial expansion of $(1 + 2x)^{0.5}$ in ascending powers of x up to and including the term in x^2

[2 marks]

Answer _____

- 6 (a) (ii)** Find the binomial expansion of $(1 - 4x)^{-0.5}$ in ascending powers of x up to and including the term in x^2

[2 marks]

Answer _____

- 6 (b) (i)** Hence find the binomial expansion of $\sqrt{\frac{1+2x}{1-4x}}$ in ascending powers of x up to and including the term in x^2

[2 marks]

Answer _____



6 (b) (ii) State the values of x for which the expansion of $\sqrt{\frac{1+2x}{1-4x}}$ is valid.

[1 mark]

Answer _____

6 (c) Use your expansion of $\sqrt{\frac{1+2x}{1-4x}}$ to find an estimate for $\sqrt{2}$, giving your answer to three decimal places.

[3 marks]

Answer _____

Turn over ►



7 A curve has equation $y = e^{3x} - 24x$

7 (a) Find an equation of the tangent to the curve at (0, 1)

[3 marks]

Answer _____

7 (b) Find the coordinates of the stationary point of the curve, giving your answer in an exact form.

[3 marks]

Answer _____



8 (c) (i) Find the number of grams of the liquid that has evaporated after 120 minutes.

[2 marks]

Answer _____

8 (c) (ii) Find how many minutes it takes for there to be only 10 grams of the liquid remaining.

[3 marks]

Answer _____



11 The point A has coordinates $(10, 2, -3)$.

The point B has coordinates $(2, -2, 5)$.

11 (a) Find the vector equation of the line AB and hence show that it can be written as

$$\mathbf{r} = \begin{bmatrix} 4 \\ -1 \\ 3 \end{bmatrix} + \lambda \begin{bmatrix} 2 \\ 1 \\ -2 \end{bmatrix}$$

[4 marks]

Answer _____

11 (b) The point D has coordinates $(-2, 1, 7)$.

The point C lies on the line AB .

The line CD is perpendicular to the line AB .

11 (b) (i) Find the coordinates of C .

[5 marks]



Answer _____

11 (b) (ii) Show that the distance $CD = \sqrt{q}$ where q is a constant.

[2 marks]

11 (c) The point $P(4 + 2p, -1 + p, 3 - 2p)$ lies on the line AB such that triangle DCP is isosceles.

Find the possible exact values of p , giving your answers in the form $s + t\sqrt{q}$, where s and t are constants.

[5 marks]

Answer _____



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