

Please write clearly in block capitals.

Centre number

Candidate number

Surname \_\_\_\_\_

Forename(s) \_\_\_\_\_

Candidate signature \_\_\_\_\_

I declare this is my own work.

## INTERNATIONAL A-LEVEL FURTHER MATHEMATICS

(9665/FM04) Unit FS2 Statistics

Wednesday 4 June 2025    07:00 GMT    Time allowed: 1 hour 30 minutes

### Materials

- For this paper you must have the OxfordAQA Booklet of Formulae and Statistical Tables (enclosed).
- You may use a graphical calculator.

### Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.

### Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- Show all necessary working; otherwise marks may be lost.

For Examiner's Use	
Question	Mark
1	
2	
3	
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5	
6	
7	
8	
9	
<b>TOTAL</b>	



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outside the  
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ANSWER IN THE SPACES PROVIDED**







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- 2 (b) The random variable  $Y$  has moment generating function

$$M_Y(t) = \frac{e^{5t} - 1}{5t}$$

The random variables  $X$  and  $Y$  are independent.

Find  $M_{X+Y}(t)$ , the moment generating function of  $X + Y$

Give your answer in the form

$$M_{X+Y}(t) = \frac{ae^{10t} + be^{9t} + ce^{5t} + de^{4t} - 1}{50t^3}$$

where  $a$ ,  $b$ ,  $c$  and  $d$  are integers.

[3 marks]

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Answer \_\_\_\_\_

Turn over ►



**3** The total distance in miles that a particular type of electric car can travel on one complete charge is known to have a normal distribution.

A random sample of 5 electric cars of this type is taken.

The total distance travelled on one complete charge by each car is measured on two days: one hot day and one cold day.

The cars are driven by the same drivers and follow the same route on each day.

The results are given in the table below.

Car	Total distance travelled (miles)	
	Hot	Cold
A	218	210
B	291	298
C	193	187
D	232	230
E	208	197

The producer of the car claims that the car can travel a greater distance on one complete charge on a hot day than on a cold day.

Test the producer's claim using the 5% level of significance.

**[10 marks]**

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- 4 (b)** The confidence interval supports the claim that the population mean of  $X$  is 2.7  
Find the smallest possible value for the sample mean of the random sample.  
Give your answer to three significant figures.

**[2 marks]**

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Answer \_\_\_\_\_

6

**Turn over for the next question**

**Turn over ►**





**5 (b)** Find the power of the test.

Give your answer to three decimal places.

**[1 mark]**

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Answer \_\_\_\_\_

6

**Turn over for the next question**

**Turn over ►**







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**7 (b)** Jenna takes a random sample of 6 films released in cinemas in country  $A$  and their length  $U$  minutes is recorded.

She also takes a random sample of 7 films released in cinemas in country  $B$  and their length  $V$  minutes is recorded.

The difference between Jenna's sample mean for country  $A$  and her sample mean for country  $B$  is 10.2 minutes.

She uses her sample to calculate unbiased estimates for the population variances.

$$s_U^2 = 3005 \quad \text{and} \quad s_V^2 = 2939$$

She assumes that the population variances for the lengths of films released in cinemas are the same for both countries.

Jenna uses her sample to test Gan's claim using the 5% level of significance.

Determine whether Jenna reaches the same conclusion as Gan.

**[5 marks]**

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- 9** A company records how many online chat questions per hour they receive from customers over a randomly selected sample period of 38 hours.

The results are shown in the following table.

<b>Questions per hour</b>	0	1	2	3 or more
<b>Frequency</b>	11	7	8	12

The sample mean number of questions per hour is 1.5

The company's data manager claims that the number of online chat questions per hour follows a Poisson distribution.

- 9 (a)** Explain why the test statistic for a hypothesis test investigating the data manager's claim has 2 degrees of freedom.

**[2 marks]**

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- 9 (b)** Test the data manager's claim using the 5% level of significance.

**[8 marks]**

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- 9 (c) A member of the data manager's team claims that the number of on-line chat questions per hour follows a Poisson distribution with mean 1.5

The team member carries out a hypothesis test with the hypotheses

$H_0$  : Number of online chat questions per hour follows a Poisson distribution with mean 1.5

$H_1$  : Number of online chat questions per hour does not follow a Poisson distribution with mean 1.5

The team member uses the 5% level of significance and the same data as the manager.

Determine whether the team member rejects their null hypothesis.

**[3 marks]**

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**END OF QUESTIONS**

