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Centre number

Candidate number

Surname _____

Forename(s) _____

Candidate signature _____

I declare this is my own work.

INTERNATIONAL AS MATHEMATICS

(9660/MA01) Unit P1 Pure Mathematics

Tuesday 3 January 2023 07:00 GMT Time allowed: 1 hour 30 minutes

Materials

- For this paper you must have the Oxford International AQA Booklet of Formulae and Statistical Tables (enclosed).
- You may use a graphical calculator.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- Show all necessary working; otherwise marks may be lost.

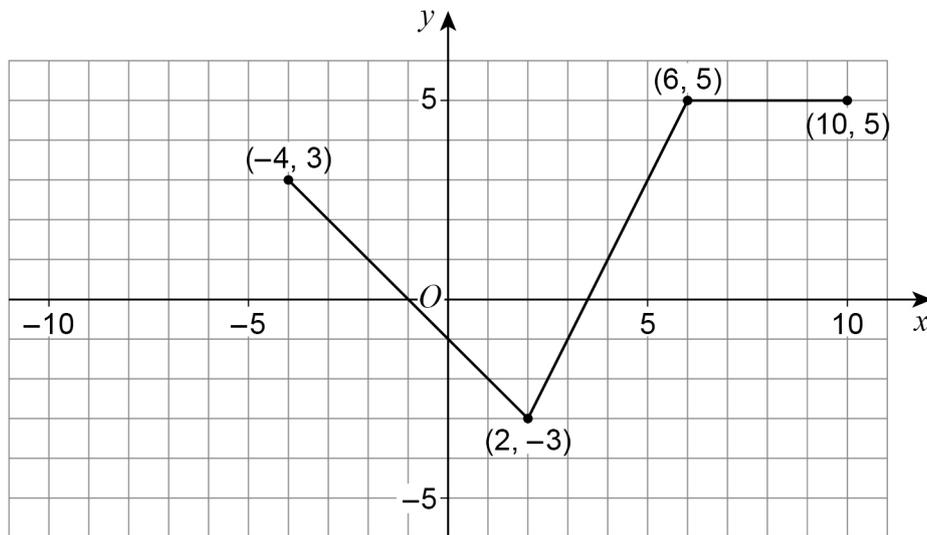
For Examiner's Use	
Question	Mark
1	
2	
3	
4	
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8	
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10	
TOTAL	



Answer **all** questions in the spaces provided.

- 1 The graph of a function with equation $y = f(x)$ is shown in **Figure 1**

Figure 1

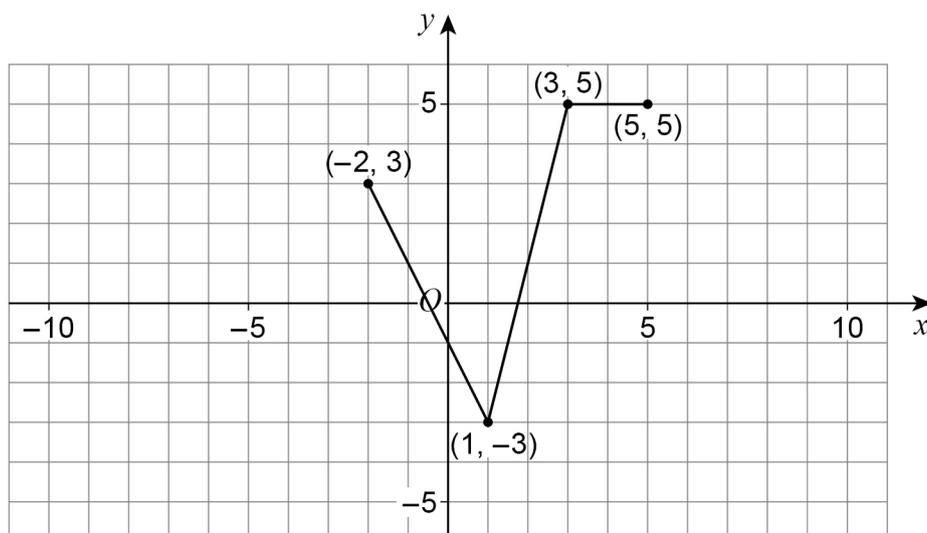


- 1 (a) (i) State the equation of the graph of the function shown in **Figure 2**

Circle your answer.

[1 mark]

Figure 2



$y = f\left(\frac{1}{2}x\right)$

$y = f(2x)$

$y = \frac{1}{2}f(x)$

$y = 2f(x)$

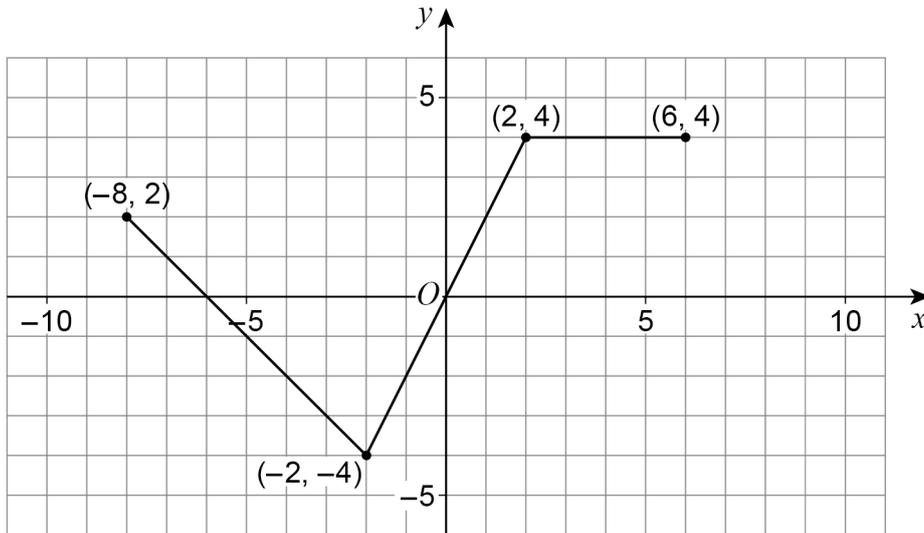


- 1 (a) (ii) State the equation of the graph of the function shown in **Figure 3**

Circle your answer.

[1 mark]

Figure 3



$$y = f(x-4) - 1$$

$$y = f(x-4) + 1$$

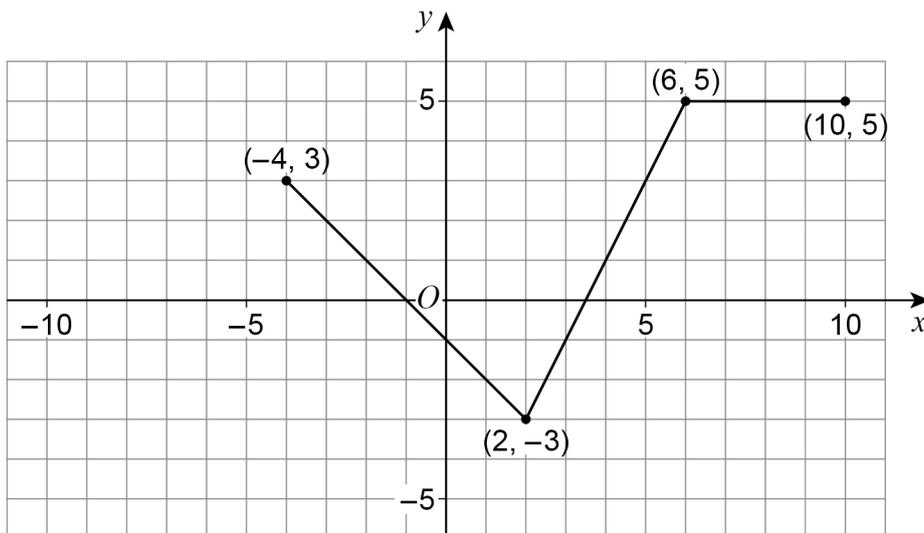
$$y = f(x+4) - 1$$

$$y = f(x+4) + 1$$

- 1 (b) The graph of the function with equation $y = f(x)$ is shown again below.

By drawing a suitable straight line find the roots of the equation $f(x) = x - 3$

[2 marks]



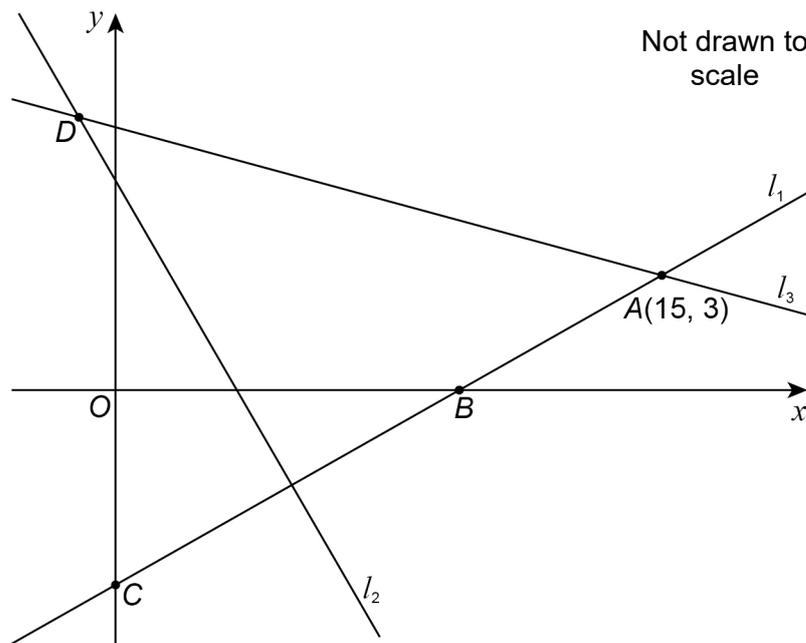
$x =$ _____

4

Turn over ►



- 2 The points A , B , C and D , and the lines l_1 , l_2 and l_3 are shown in the diagram.



The lines l_1 and l_3 intersect at $A(15, 3)$

- 2 (a) The line l_1 has gradient $\frac{3}{5}$

Show that l_1 has the equation $3x - 5y - 30 = 0$

[1 mark]

- 2 (b) l_1 intersects the x -axis at B and the y -axis at C

l_2 passes through the mid-point of the line segment BC

l_1 and l_2 are perpendicular.

Find the equation of l_2 giving your answer in the form $ax + by + c = 0$
where a , b and c are integers.

[5 marks]



Answer _____

2 (c) l_3 has the equation $x + 4y - 27 = 0$

l_2 and l_3 intersect at D

Find the coordinates of D

[1 mark]

Answer _____

2 (d) Find the length of the line segment AD

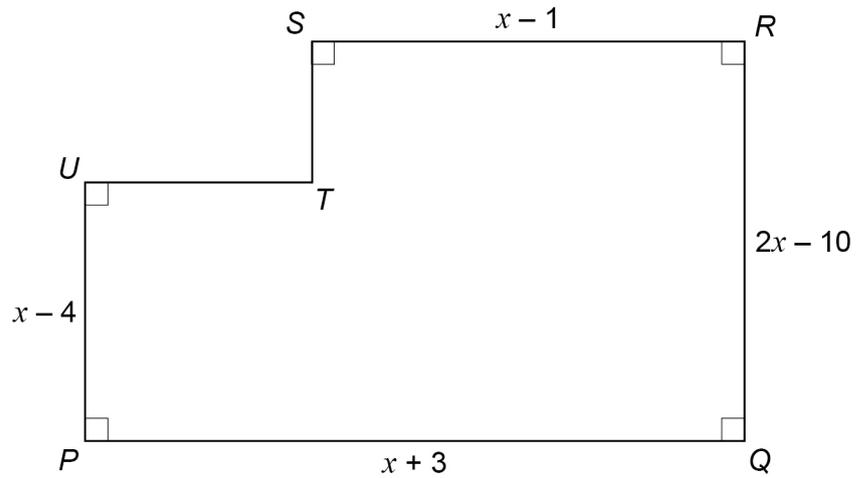
Give your answer in the form $n\sqrt{p}$ where p is a prime number.

[2 marks]

Answer _____



- 3 The diagram shows the plan of a garden.



The angle at each corner of the garden is a right-angle.

The lengths of the sides in metres are

$$PQ = x + 3, \quad QR = 2x - 10, \quad RS = x - 1 \quad \text{and} \quad PU = x - 4$$

- 3 (a) The perimeter of the garden is greater than 31 metres.

Show that $x > 7.5$

[1 mark]

- 3 (b) The area of the garden is less than 58 m^2

Show that $x^2 - 4x - 32 < 0$

[3 marks]



3 (c) Solve the inequality $x^2 - 4x - 32 < 0$

Show clearly each step of your working.

[2 marks]

Answer _____

3 (d) The length of the side ST is y metres.

Using your answers to **parts (a) and (c)** find the possible values of y

[2 marks]

Answer _____

8

Turn over ►



- 5 The n th term of the sequence A is u_n and the sequence is defined by

$$u_{n+1} = u_n + 8(1 + 3^n)$$

The second, third and fourth terms of this sequence are

$$u_2 = 61 \quad u_3 = 141 \quad \text{and} \quad u_4 = 365$$

- 5 (a) (i) Find the first term u_1 of sequence A

[1 mark]

Answer _____

- 5 (a) (ii) Find the fifth term u_5 of sequence A

[1 mark]

Answer _____

- 5 (b) The sequence A can be found using the formula

$$\begin{array}{ccccc} n\text{th term of} & = & n\text{th term of} & + & n\text{th term of} \\ \text{sequence } A & & \text{sequence } B & & \text{sequence } C \end{array}$$

where sequence B and sequence C are two different sequences.

- 5 (b) (i) Sequence B is a geometric sequence with first term $a = 12$ and common ratio $r = 3$

Find the first five terms of sequence B

[1 mark]

Answer _____



5 (b) (ii) Hence find the first five terms of sequence C

[2 marks]

Answer _____

5 (c) (i) Sequence C is an arithmetic sequence.

Using your answer to **part (b)(ii)** write down the common difference for sequence C

[1 mark]

Answer _____

5 (c) (ii) Find an expression in terms of n for the n th term of sequence C

[1 mark]

Answer _____

— 7

Turn over ►



6 The curve C has the equation

$$y = 3x^3 + 14x^2 + 17x + 11$$

The point $P(-2, 9)$ lies on C

The line l is the normal to C at the point P

6 (a) (i) Find $\frac{dy}{dx}$

[2 marks]

Answer _____

6 (a) (ii) Show that the equation of l is $y = \frac{1}{3}x + \frac{29}{3}$

[3 marks]

6 (b) The line l intersects C at three distinct points.

Show that the x -coordinates of these points of intersection satisfy the equation

$$9x^3 + 42x^2 + 50x + 4 = 0$$

[2 marks]



6 (c) The equation $9x^3 + 42x^2 + 50x + 4 = 0$ can be written in the form

$$(x + 2)(9x^2 + 24x + 2) = 0$$

6 (c) (i) Express $9x^2 + 24x + 2$ in the form $a(x + b)^2 + c$ where a , b and c are constants.

[3 marks]

Answer _____

6 (c) (ii) The points of intersection of l and C are $P(-2, 9)$, Q and R

Using your answer to **part (c)(i)** find the exact x -coordinates of Q and R

Show clearly each step of your working.

[3 marks]

Answer _____



7 A curve has equation $y = f(x)$ where $x > 0$

It is given that

$$\frac{dy}{dx} = 2x^{\frac{3}{2}} - 9x^{\frac{3}{4}} - 56$$

7 (a) Find $\frac{d^2y}{dx^2}$

[2 marks]

Answer _____

7 (b) By substituting $t = x^{\frac{3}{4}}$ into the given expression for $\frac{dy}{dx}$ show that

$$\frac{dy}{dx} = (at + b)(t - c)$$

where a , b and c are positive integers.

[2 marks]



7 (c) The curve has one stationary point for $x > 0$

7 (c) (i) By writing x as a power of t and then using **part (b)** find the x -coordinate of this stationary point.

[3 marks]

Answer _____

7 (c) (ii) Using **part (a)** show that this stationary point is a minimum.

[1 mark]

7 (d) State the values of x for which f is a decreasing function.

[1 mark]

Answer _____

Turn over ►



8 (a) Show that for any positive real number a

$$(2 + \sqrt{3} - \sqrt{a})(2 + \sqrt{3} + \sqrt{a}) = 7 + b\sqrt{3} - a$$

where b is a constant to be found.

[2 marks]

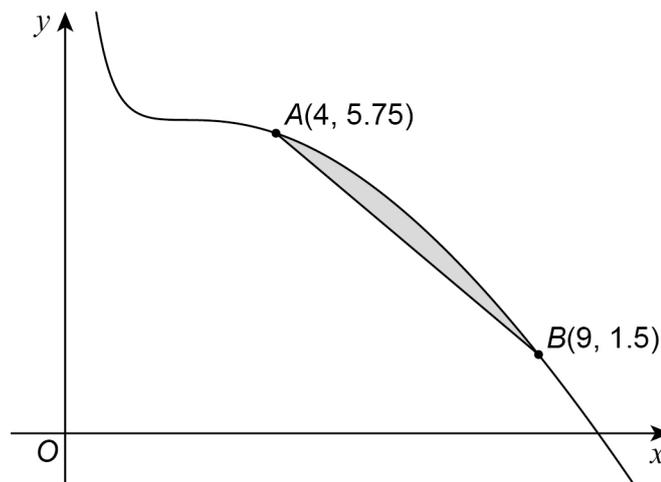


9 (b) (ii) Hence find the value of $\int_4^9 \left(\frac{(3-2\sqrt{x})^3}{\sqrt{x}} + 12 \right) dx$

[2 marks]

Answer _____

9 (c) A curve with equation $y = \frac{(3-2\sqrt{x})^3}{2\sqrt{x}} + 6$ is drawn below.



The points $A(4, 5.75)$ and $B(9, 1.5)$ lie on the curve.

Using your answer to **part (b)(ii)** find the area of the shaded region bounded by the curve and the line segment AB

[2 marks]

Answer _____

Turn over ►



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