

Please write clearly in block capitals.

Centre number

Candidate number

Surname _____

Forename(s) _____

Candidate signature _____

I declare this is my own work.

INTERNATIONAL AS FURTHER MATHEMATICS

(9665/FM01) Unit FP1 Pure Mathematics

Monday 13 May 2024

07:00 GMT

Time allowed: 1 hour 30 minutes

Materials

- For this paper you must have the OxfordAQA Booklet of Formulae and Statistical Tables (enclosed).
- You may use a graphical calculator.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- Show all necessary working; otherwise marks may be lost.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
TOTAL	



Answer **all** questions in the spaces provided.

1 The complex number z is given by

$$z = 2 + i\sqrt{5}$$

1 (a) Express z in the form $r(\cos\theta + i\sin\theta)$ where $r > 0$ and $-\pi < \theta \leq \pi$

Give your value of θ to three significant figures.

[2 marks]

Answer _____

1 (b) Write down the complex number z^* in the form $r(\cos\theta + i\sin\theta)$ where $r > 0$
and $-\pi < \theta \leq \pi$

[2 marks]

Answer _____

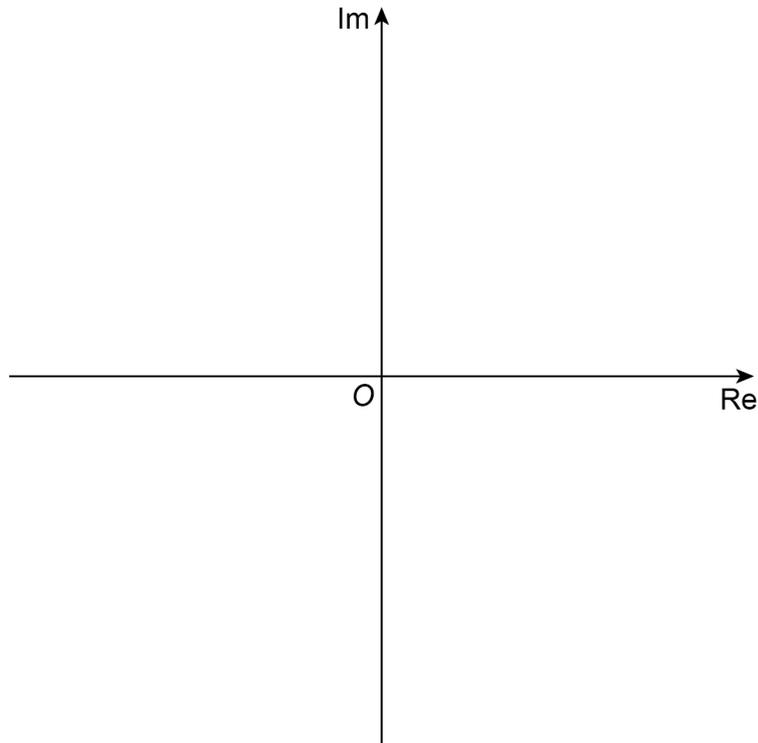


- 1 (c)** On an Argand diagram, the complex number z is represented by the point P and the complex number z^* is represented by the point Q

The point R is such that $OPRQ$ is a rhombus, where O is the origin.

- 1 (c) (i)** Sketch the rhombus $OPRQ$ on the Argand diagram below.

[2 marks]



- 1 (c) (ii)** Find the number represented by point R

[1 mark]

Answer _____

- 1 (c) (iii)** Find the area of rhombus $OPRQ$

Give your answer in exact form.

[2 marks]

Answer _____



2 (b) (ii) Use your answer to **part (b) (i)** to find the gradient of the curve at the point where $x = 4$

Show the limiting process used.

[2 marks]

Answer _____

7

Turn over for the next question

Turn over ►



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outside the
box

Answer _____

5

Turn over for the next question

Turn over ►



6 (b) Write down the value of

$$\sum_{r=1}^{\infty} \frac{1}{r(r+1)}$$

[1 mark]

Answer _____

6 (c) Find the exact value of

$$\sum_{r=1001}^{2000} \frac{1}{r(r+1)}$$

[2 marks]

Answer _____

8

Turn over ►



7 The curve C has equation

$$y = \frac{x^2}{x^2 + ax + 3}$$

where a is a constant such that C has exactly one asymptote.

7 (a) Write down the equation of the asymptote of C

[1 mark]

Answer _____

7 (b) Show that

$$a^2 < p$$

where p is an integer.

[2 marks]

7 (c) Show that if the line $y = k$ does **not** intersect C then

$$k^2(12 - a^2) - 12k > 0$$

[4 marks]



- 7 (d) In the case when $a = \sqrt{5}$, use the result from **part (c)** to find the y -coordinate of each of the stationary points of C

[3 marks]

Answer _____

10

Turn over ►



8 (a) Expand and simplify $(\alpha + \beta)^4$

[2 marks]

Answer _____

8 (b) Hence, or otherwise, express $\alpha^4 + \beta^4$ in terms of $\alpha + \beta$ and $\alpha\beta$

[3 marks]

Answer _____



8 (c) The quadratic equation $2x^2 - x + 6 = 0$ has roots α and β

8 (c) (i) Write down the value of $\alpha + \beta$ and the value of $\alpha\beta$

[2 marks]

$\alpha + \beta =$ _____ $\alpha\beta =$ _____

8 (c) (ii) Find a quadratic equation, with integer coefficients, which has roots $\frac{\alpha^2}{\beta^2}$ and $\frac{\beta^2}{\alpha^2}$

[5 marks]

Answer _____



9 The line L is the locus of points on an Argand diagram such that

$$|z - 2| = |z - 4i|$$

9 (a) Line L passes through the point representing the complex number $z = 1 + ci$ where c is a real constant.

Find the value of c

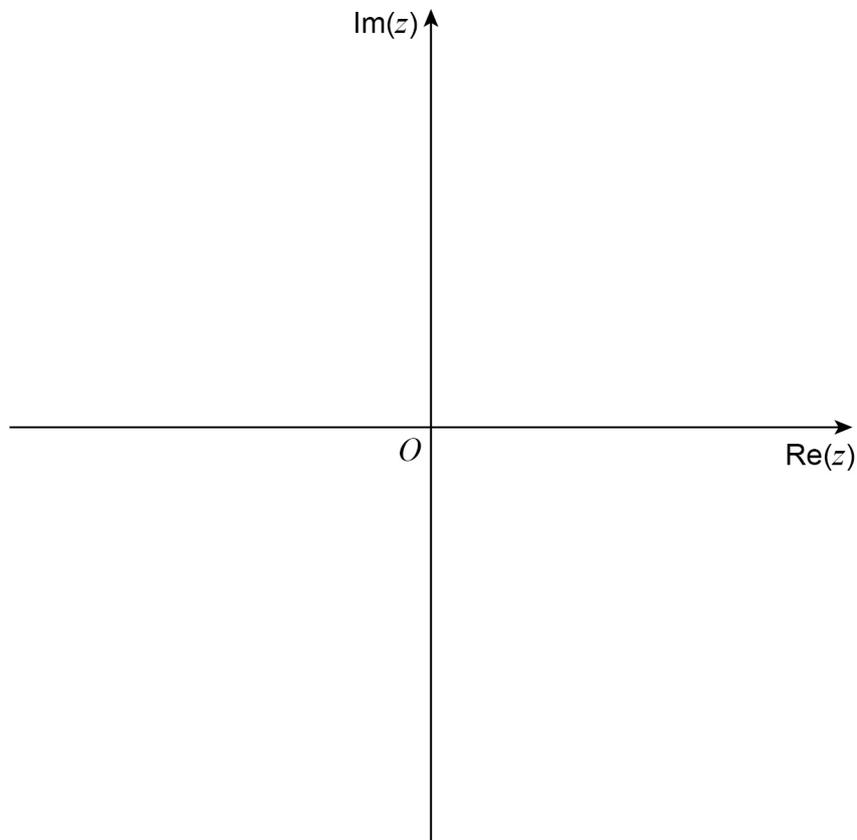
[1 mark]

Answer _____

9 (b) Sketch L on the Argand diagram below.

Include the values where L intersects the real and imaginary axes.

[4 marks]



- 9 (c) The half-line H is the locus of points on an Argand diagram such that

$$\arg(z + a) = \tan^{-1}(b)$$

where a and b are real constants.

Every point on H also lies on L

- 9 (c) (i) Find the value of a

[1 mark]

Answer _____

- 9 (c) (ii) Find the value of b

[1 mark]

Answer _____

7

Turn over for the next question

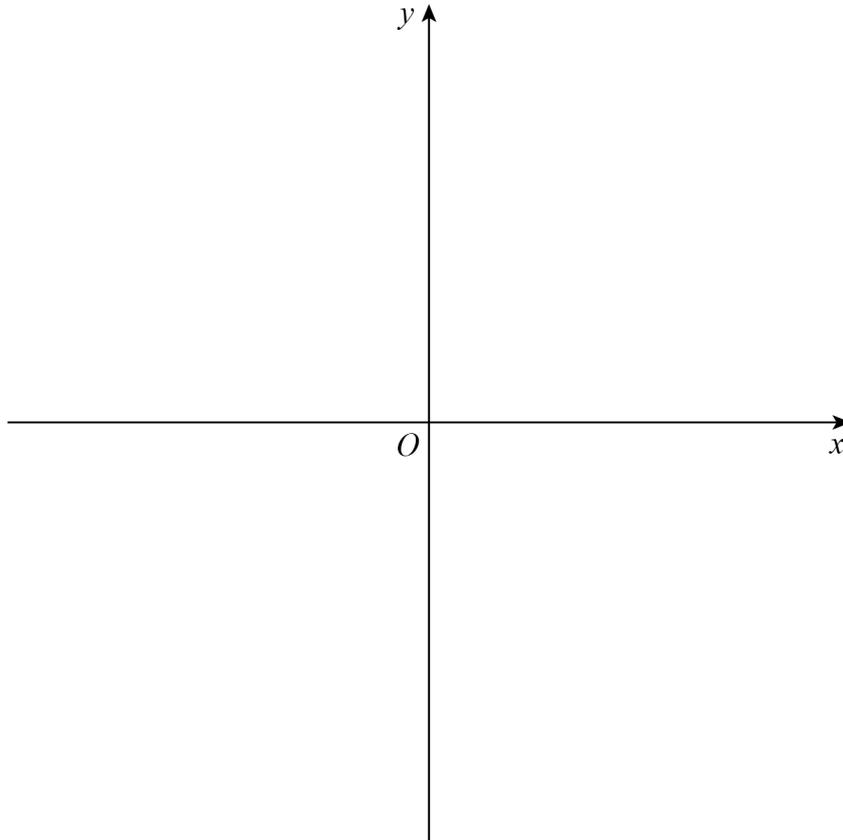
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10 (b) (ii) Sketch the graph of C_2

Include the value of any axis intercepts.

[2 marks]



10 (b) (iii) The line with equation $y = mx$ intersects C_2 twice.

Find the range of possible values for m

[5 marks]

Turn over ►



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ANSWER IN THE SPACES PROVIDED**



