

Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

I declare this is my own work.

INTERNATIONAL A-LEVEL MATHEMATICS

(9660/MA04) Unit S2 Statistics

Tuesday 18 January 2022 07:00 GMT Time allowed: 1 hour 30 minutes

Materials

- For this paper you must have the Oxford International AQA Booklet of Formulae and Statistical Tables (enclosed).
- You may use a graphical calculator.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- Show all necessary working; otherwise marks may be lost.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
TOTAL	



2 (a) The random variable X has a Poisson distribution with parameter λ

The standard deviation of X is 3

The random variable X represents the number of times in one hour a road crossing is used.

2 (a) (i) State the value of λ

[1 mark]

Answer _____

2 (a) (ii) Find $P(X < 8)$, giving your answer to three significant figures.

[2 marks]

Answer _____

2 (a) (iii) Find $P(X = E[X])$, giving your answer to three significant figures.

[3 marks]

Answer _____



2 (b) The random variable T represents the time in hours between two successive people using the road crossing.

2 (b) (i) State the distribution and parameter for T

[2 marks]

Distribution _____

Parameter _____

2 (b) (ii) State the mean of T

[1 mark]

Answer _____

2 (b) (iii) Find the probability that the time between two successive crossings is more than 30 minutes, giving your answer to four decimal places.

[3 marks]

Answer _____

2 (b) (iv) Find the value of t such that $P(T < t) = 0.9$, giving your answer in hours to three significant figures.

[2 marks]

Answer _____



3 A supplier of cabbage seeds claims that 40% of their cabbage seeds germinate after being planted.

A student carries out a hypothesis test at the 10% level of significance to determine whether there is evidence to support the supplier's claim.

A random sample of 14 cabbage seeds is used for the test.

The number of cabbage seeds which germinate after being planted is assumed to be binomially distributed.

The first five stages of the student's hypothesis test are shown below.
There are errors in **two** of these stages.

	Statement
Stage 1	$H_0 : p = 0.4$ $H_1 : p \neq 0.4$ where p is the probability that a cabbage seed germinates after being planted
Stage 2	Under H_0 $X \sim B(0.4, 14)$ where X is the number of cabbage seeds which germinate
Stage 3	$P(X \leq 2) = 0.0398$ (< 0.05) $P(X \leq 3) = 0.1243$ (> 0.05) (to four decimal places)
Stage 4	$P(X \geq 9) = 0.0583$ (> 0.05) $P(X \geq 10) = 0.0175$ (< 0.05) (to four decimal places)
Stage 5	The critical region is $\{0, 1, 2, 9, 10, 11, 12, 13, 14\}$

3 (a) Identify the **two** stages which have errors.

Write down a correct statement for each of these stages.

[3 marks]

Error 1 Stage _____

Correct statement _____

Error 2 Stage _____

Correct statement _____



3 (b) Of the 14 cabbage seeds used for the test, 8 germinate after being planted.

Determine the conclusion of the hypothesis test.

[2 marks]

3 (c) (i) Find the probability of a Type I error for this hypothesis test.

[1 mark]

Answer _____

3 (c) (ii) For this hypothesis test describe, in context, the meaning of a Type I error.

[1 mark]

3 (d) The level of significance used for this hypothesis test is now changed to $k\%$

3 (d) (i) In the case where $k > 10$ explain how the acceptance region for this hypothesis test may change.

[1 mark]

3 (d) (ii) In the case where $k < 10$ explain how the acceptance region for this hypothesis test may change.

[1 mark]



4 The continuous random variable T has probability density function

$$f(t) = \begin{cases} ct^2 & 0 < t \leq 1 \\ \frac{1}{2}t & 1 < t \leq 2 \\ 0 & \text{otherwise} \end{cases}$$

where c is a constant.

4 (a) Show that $c = \frac{3}{4}$

[3 marks]

4 (b) (i) Find the exact value of $E(T)$

[3 marks]

Answer _____



4 (b) (ii) It is given that $E(T^2) = \frac{81}{40}$

Find the exact value of $\text{Var}(T)$

[2 marks]

Answer _____

4 (c) (i) Find the exact value of $E(3T+1)$

[2 marks]

Answer _____

4 (c) (ii) Find the exact value of $\text{Var}(3T+1)$

[2 marks]

Answer _____

12

Turn over ►



5 To make a cake there are three processes: mixing, baking and decorating.

The times taken, in minutes, for these processes can be modelled as independent normal distributions.

Mixing	$X_M \sim N(8, 1.3^2)$
Baking	$X_B \sim N(\mu, 1.5^2)$
Decorating	$X_D \sim N(20, 2.5^2)$

5 (a) Find the probability that it takes less than 6 minutes to complete the mixing process, giving your answer to three significant figures.

[3 marks]

Answer _____

5 (b) It is given that $P(X_B < 26.3) = 0.8$

Show that $\mu = 25$ correct to two significant figures.

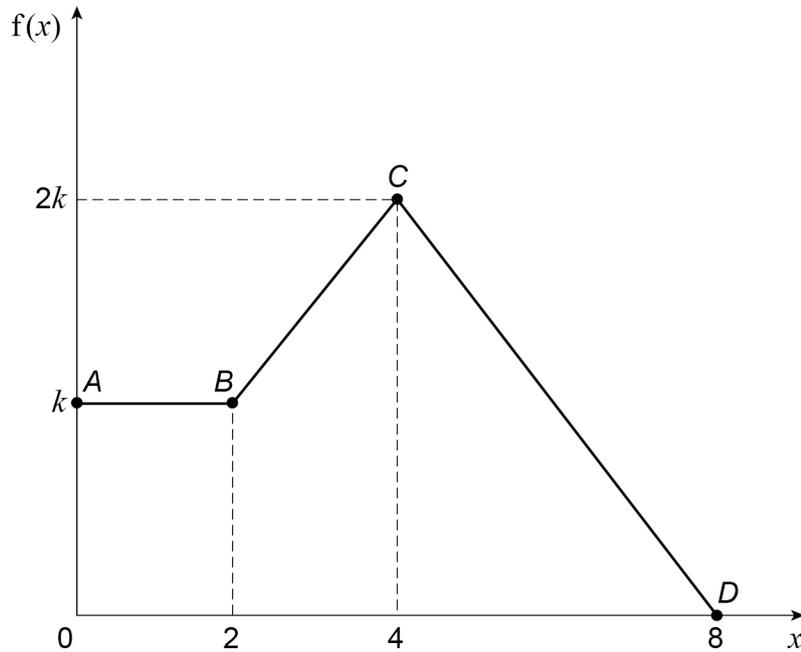
[3 marks]



6 A continuous random variable X has probability density function f

The graph of $f(x)$ consists of three line segments: AB , BC and CD for $0 \leq x \leq 8$ where k is a constant. For all other values of x , $f(x) = 0$ as shown in **Figure 1**

Figure 1



6 (a) Show that $k = \frac{1}{9}$

[2 marks]

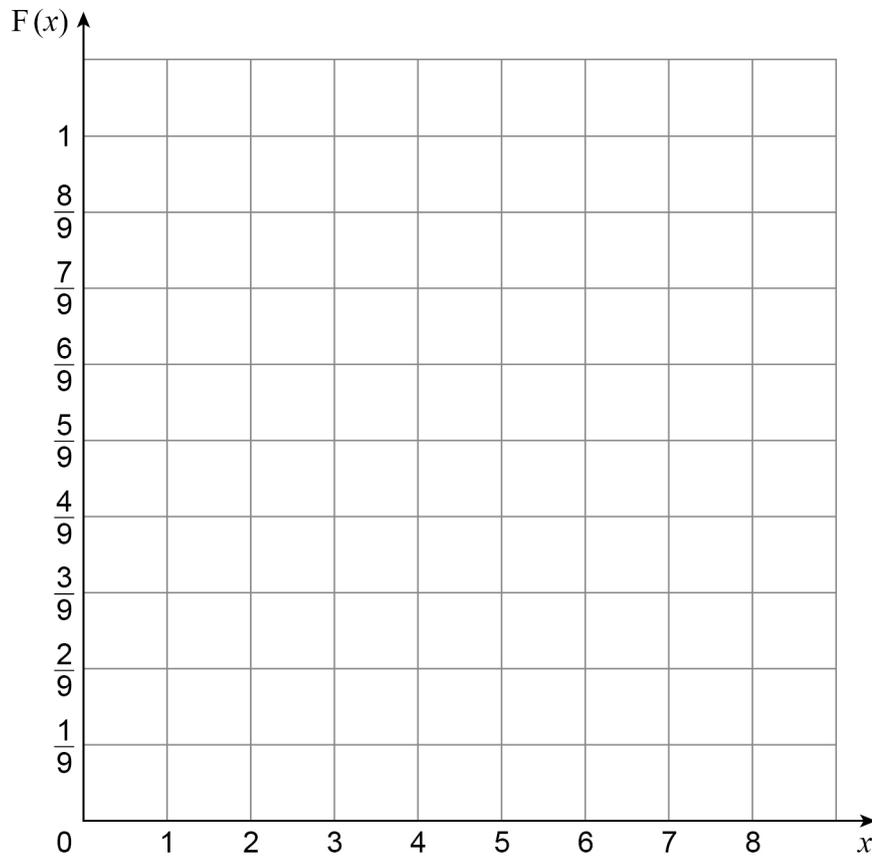
6 (b) Given that $P(X < c) = 0.5$ show that $2 < c < 4$

[2 marks]



- 6 (c)** Draw the cumulative distribution function F , stating the values of $F(x)$ when $x = 2$, $x = 4$, $x = 6$, and $x = 8$ on **Figure 2**

[4 marks]

Figure 2

8

Turn over for the next question

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- 7 (b) Lottie wants to do further calculations with the sample collected for her hypothesis test in **part (a)** but two of these heights are now missing.

The heights in cm of the 10 students in her sample are

123 125 128 124 122 129 126 119 q r

where q and r are the missing heights.

- 7 (b) (i) Show that $q + r = 254$

[2 marks]

- 7 (b) (ii) It is given that $q > r$

Find the value of q and the value of r , giving your answers to three significant figures.

[6 marks]

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