

Please write clearly in block capitals.

Centre number

Candidate number

Surname _____

Forename(s) _____

Candidate signature _____

I declare this is my own work.

INTERNATIONAL A-LEVEL MATHEMATICS

(9660/MA04) Unit S2 Statistics

Tuesday 13 June 2023 07:00 GMT Time allowed: 1 hour 30 minutes

Materials

- For this paper you must have the Oxford International AQA Booklet of Formulae and Statistical Tables (enclosed).
- You may use a graphical calculator.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- Show all necessary working; otherwise marks may be lost.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
TOTAL	



Answer **all** questions in the spaces provided.

1 (a) The random variable W has a Poisson distribution with a mean of 15

1 (a) (i) State the value of the standard deviation of W

[1 mark]

Answer _____

1 (a) (ii) It is given that $P(W \leq a) > 0.9$

Find the smallest possible value of a

[2 marks]

Answer _____

1 (a) (iii) It is given that $P(W > b) < 0.01$

Find the smallest possible value of b

[2 marks]

Answer _____



1 (b) The random variable X has a Poisson distribution with a mean of 3

Find $P(3 \leq X < 5)$ giving your answer to three significant figures.

[2 marks]

Answer _____

1 (c) The random variable T is defined as $T \sim B(500, 0.02)$

1 (c) (i) Explain why T can be approximated by the random variable $Y \sim \text{Po}(\lambda)$

[1 mark]

1 (c) (ii) State the value of λ in **part 1(c)(i)**.

[1 mark]

1 (c) (iii) The random variable C is defined as

$$C = W + X + Y$$

It is given that W , X and Y are independent.

Find $P(C < 3)$ giving your answer in the form $p e^{-q}$ where p and q are integers.

[3 marks]

Answer _____



3 The lifetime (in thousands of hours) of a component for a photocopier is modelled as T where $P(T \leq t) = 1 - e^{-\frac{t}{8}}$

3 (a) State the distribution model and the parameter of T

[1 mark]

Model _____

Parameter _____

3 (b) Find the probability of a component lasting longer than 7 thousand hours, giving your answer to four significant figures.

[2 marks]

Answer _____

3 (c) Only 5% of components have lifetimes greater than L hours.

Find the value of L giving your answer to four significant figures.

[2 marks]

Answer _____



- 3 (d)** Given that a component still works after 7 thousand hours of use, find the probability that the component has a lifetime of less than 10 thousand hours.

Give your answer to four significant figures.

[2 marks]

Answer _____

- 3 (e)** Explain why your answer in **part 3(d)** is not likely to be representative of a real-life component.

[1 mark]

8

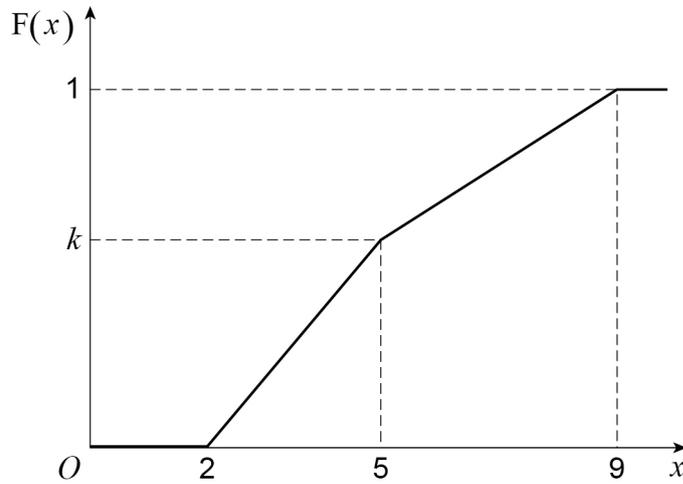
Turn over for the next question

Turn over ►



- 4 The continuous random variable X has cumulative distribution function $F(x)$ as shown in the graph below.

The graph is made up from line segments where $F(2) = 0$, $F(5) = k$ and $F(9) = 1$



It is given that $P(X \leq 4) = 0.4$

- 4 (a) Find the value of k

[2 marks]

Answer _____



7 The continuous random variable X has probability density function $f(x)$ defined by

$$f(x) = \begin{cases} \frac{3\sqrt{x} + k}{6} & 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

where k is a constant.

7 (a) Show that $k = 4$

[2 marks]

7 (b) Find the exact value of $E(X)$

[3 marks]

Answer _____



- 7 (d) The continuous random variable Y has $E(Y) = 2$ and $\text{Var}(Y) = \frac{5}{7}$.
It is given that X and Y are independent random variables.

- 7 (d) (i) Find the value of $E(15X - 9Y)$

[2 marks]

Answer _____

- 7 (d) (ii) Find the value of $\text{Var}(15X - 9Y)$

[2 marks]

Answer _____



Turn over for the next question

*Do not write
outside the
box*

**DO NOT WRITE ON THIS PAGE
ANSWER IN THE SPACES PROVIDED**

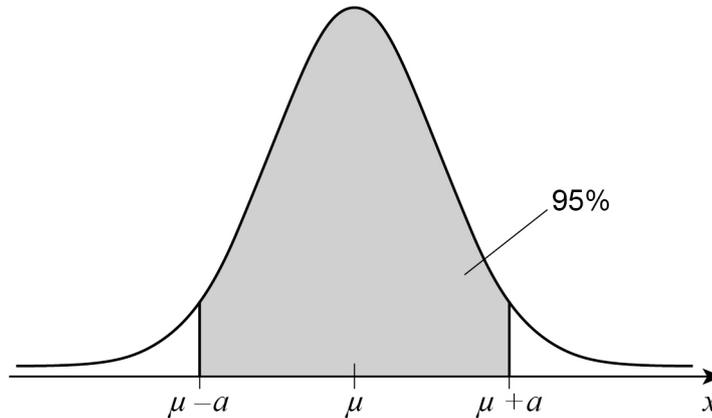
Turn over ►



8 The random variable X is defined as $X \sim N(\mu, \sigma^2)$ and graphs of its probability distribution function are shown in **Figures 1–3** below.

8 (a) (i) The shaded region between the lines $x = \mu - a$ and $x = \mu + a$ in **Figure 1** is 95% of the total area between the graph and the x -axis.

Figure 1



Find an expression for a in terms of σ

Give the coefficient of σ to four decimal places.

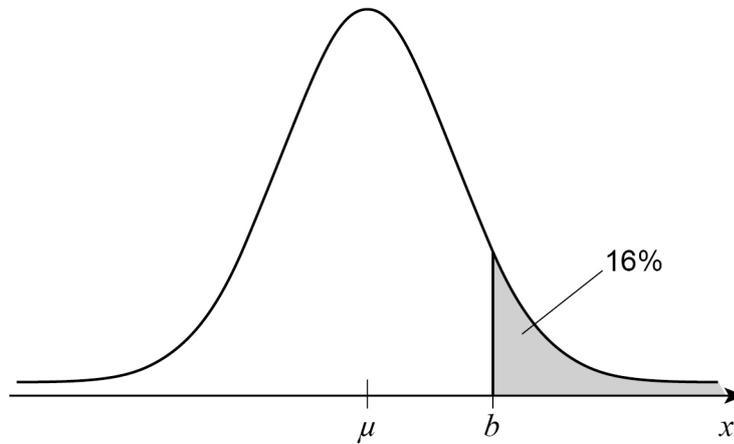
[1 mark]

Answer _____



- 8 (a) (ii) The shaded region to the right of the line $x = b$ in **Figure 2** is 16% of the total area between the graph and the x -axis.

Figure 2



Find an expression for b in terms of μ and σ

Give the coefficient of σ to four decimal places.

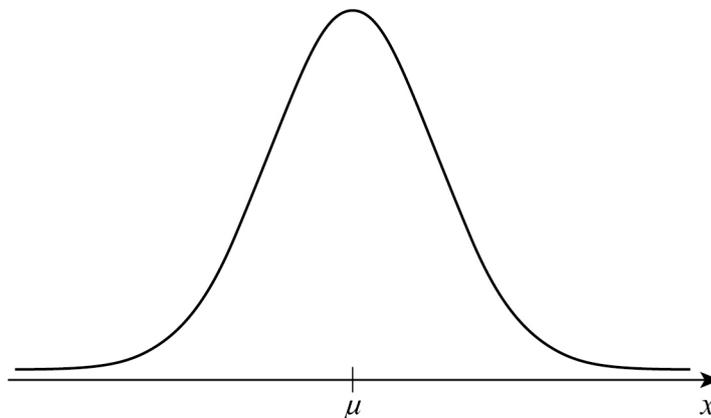
[1 mark]

Answer _____

- 8 (a) (iii) Sketch on **Figure 3** the total region represented by $P((X - \mu)^2 > c^2)$ where c is a positive constant by shading the appropriate area and labelling the x -axis.

[1 mark]

Figure 3



Question 8 continues on the next page

Turn over ►



There are no questions printed on this page

*Do not write
outside the
box*

**DO NOT WRITE ON THIS PAGE
ANSWER IN THE SPACES PROVIDED**



