

- 2 (a) Find the coefficient of x^2 in the Maclaurin's series for $-\ln \cos x$.

[4]

- (b) Find the length of the arc of the curve with equation $y = -\ln \cos x$ from the point where $x = 0$ to the point where $x = \frac{1}{4}\pi$.

[4]

- 4 The curve C has equation

$$4y^3 + (x+y)^6 = 109.$$

- (a) Show that, at the point $(-4, 3)$ on C , $\frac{dy}{dx} = \frac{1}{17}$.

[3]

(b) Find the value of $\frac{d^2y}{dx^2}$ at the point $(-4, 3)$.

[5]

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3 Find the first three terms in the Maclaurin's series for $\tanh^{-1}\left(\frac{1}{2}e^x\right)$ in the form $\frac{1}{2}\ln a + bx + cx^2$, giving the exact values of the constants a , b and c . [6]

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5 It is given that

$$x = \sinh^{-1}t, \quad y = \cos^{-1}t,$$

where $-1 < t < 1$.

(a) By differentiating $\cos y$ with respect to t , show that $\frac{dy}{dt} = -\frac{1}{\sqrt{1-t^2}}$. [4]

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(b) Find $\frac{d^2y}{dx^2}$ in terms of t , simplifying your answer. [5]

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2 The curve C has parametric equations

$$x = \sinh t \quad \text{and} \quad y = t + \cosh t.$$

- (a) Find $\frac{dy}{dx}$ in terms of t . [2]

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- (b) Show that $\frac{d^2y}{dx^2} = \frac{1 - \sinh t}{\cosh^3 t}$. [4]

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- (c) Find the Maclaurin's series for y in terms of x up to and including the term in x^2 . [2]

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2 It is given that

$$x = 1 + \frac{1}{t} \quad \text{and} \quad y = \cos^{-1} t \quad \text{for } 0 < t < 1.$$

- (a) Show that $\frac{dy}{dx} = \frac{t^2}{\sqrt{1-t^2}}$. [2]

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- (b) Show that $\frac{d^2y}{dx^2} = -t^a(1-t^2)^b(2-t^2)$, where a and b are constants to be determined. [4]

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