

Question	Answer	Marks
8(a)	$r = \cos^2 \theta$ SOI	M1
	$S_{\infty} = \frac{\sin^2 \theta}{1 - \cos^2 \theta}$	M1
	1	A1
		3
8(b)(i)	$d = \sin^2 \theta \cos^2 \theta - \sin^2 \theta$	M1
	$\sin^2 \theta (\cos^2 \theta - 1)$	M1
	$-\sin^4 \theta$	A1
		3

Question	Answer	Marks
8(b)(ii)	Use of $S_{16} = \frac{16}{2}[2a + 15d]$	M1
	With <u>both</u> $a = \frac{3}{4}$ and $d = -\frac{9}{16}$	A1
	$S_{16} = -55\frac{1}{2}$	A1
		3

Question	Answer	Marks	Guidance
3(a)	State $2r + r\theta = 65$ and $\frac{1}{2}r^2\theta = 225$	B1	
	Form a 3-term quadratic or cubic in r or θ or $r\theta$ from correct arc and sector formula	*M1	Condone sign errors.
	Solve <i>their</i> 3 term quadratic or cubic to obtain values of r or θ	DM1	Expect $2r^2 - 65r + 450 = (2r - 45)(r - 10)$ or $18\theta^2 - 97\theta + 72 = (9\theta - 8)(2\theta - 9)$.
	$r = 10$ and $\theta = 4.5$ ignore $r = 22.5$ and $\theta = \frac{8}{9}$, do not ignore $r = 0$	A1	B1 SC if no quadratic or cubic solution. If $r = 0$ included A0 or B0 SC.
		4	
3(b)	Use correct formula for area of triangle with clear use of angle being $2\pi - \text{their } \theta$	M1	Expect 1.783 or 102.2° , <i>their</i> θ must be reflex.
	48.9	A1	AWRT, WWW or a second answer. Or greater accuracy; condone absence of units.
		2	

Question	Answer	Marks	Guidance
8(a)	$[fg(x) =]1/(2x+1)^2 - 1$	B1	SOI
	$1/(2x+1)^2 - 1 = 3$ leading to $4(2x+1)^2 = 1$ or $\frac{1}{(2x+1)} = [\pm]2$ or $16x^2 + 16x + 3 = 0$	M1	Setting $fg(x) = 3$ and reaching a stage before $2x+1 = \pm\frac{1}{2}$ or reaching a 3 term quadratic in x
	$2x+1 = \pm\frac{1}{2}$ or $2x+1 = -\frac{1}{2}$ or $(4x+1)(4x+3) = 0$	A1	Or formula or completing square on quadratic
	$x = -\frac{3}{4}$ only	A1	
	Alternative method for Question 8(a)		
	$x^2 - 1 = 3$	M1	
	$g(x) = -2$	A1	
	$\frac{1}{(2x+1)} = -2$	M1	
	$x = -\frac{3}{4}$ only	A1	
		4	

Question	Answer	Marks	Guidance
8(b)	$y = \frac{1}{(2x+1)^2} - 1$ leading to $(2x+1)^2 = \frac{1}{y+1}$ leading to $2x+1 = [\pm] \frac{1}{\sqrt{y+1}}$	*M1	Obtain $2x+1$ or $2y+1$ as the subject
	$x = [\pm] \frac{1}{2\sqrt{y+1}} - \frac{1}{2}$	DM1	Make x (or y) the subject
	$-\frac{1}{2\sqrt{x+1}} - \frac{1}{2}$	A1	OE e.g. $-\frac{\sqrt{x+1}}{2x+2} - \frac{1}{2}, -\left(\sqrt{\frac{-x}{4x+4} + \frac{1}{4} + \frac{1}{2}}\right)$
		3	

Question	Answer	Marks	Guidance
5	Replace $\tan \theta$ with $\frac{\sin \theta}{\cos \theta}$	M1	
	Replace $\sin^2 \theta$ with $1 - \cos^2 \theta$ leading to a 3-term quadratic	*M1	To obtain a 3-term quadratic in $\cos \theta$. Accept a cubic that has a common factor of $\cos \theta$. Condone +/- sign errors during simplification.
	$9 \cos^2 \theta + \cos \theta - 4 = 0$	A1	OE
	Attempt to solve (<i>their</i> quadratic in $\cos \theta$) using a valid method	DM1	Only available for solution of a three-term quadratic. Correct values of $\cos \theta$ are 0.6134 and -0.7245 .
	Any two of $\pm 52.2, \pm 136.4$	A1	AWRT as final answers. Any two correct answers between -180° and 180° as <i>their</i> final answers.
	All four values	A1	Condone other answers outside the range but no others between -180° and 180° . SC after M1 *M1 A1 DM0, correct answers can score B1 B1.
		6	

Question	Scheme	Marks
5(a)	$\frac{1}{2} \times 6^2 \times 1.3 = \dots$	M1
	$= 23.4 \text{ (m}^2\text{)}$	A1
		(2)
(b)	$12.2^2 = 6^2 + 10.8^2 - 2 \times 6 \times 10.8 \cos(ABE)$	M1
	$\cos(ABE) = \frac{6^2 + 10.8^2 - 12.2^2}{2 \times 6 \times 10.8} \left(= \frac{19}{648} \right)$	A1
	$ABE = 1.54$	(2)
(c)	$\text{Area } ABE = \frac{1}{2} \times 10.8 \times 6 \sin(ABE)$	M1
	$\text{Area } BCD = \frac{1}{2} \times 6 \cos(\pi - 1.3 - "1.54") \times 6 \sin(\pi - 1.3 - "1.54")$ or e.g.	M1
	$\text{Area } BCD = \frac{1}{2} \times 6 \sin(\pi - 1.3 - "1.54") \times \sqrt{6^2 - (6 \sin(\pi - 1.3 - "1.54"))^2}$	
	$\text{Total area} = 60.9 \text{ m}^2$	A1
		(3)
		Total 7

Question	Answer	Marks	Guidance
5(b)	Differentiate <i>their</i> first derivative, substitute <i>their</i> x value. Substitution may be implied by a correct inequality or correct value,	M1	Must differentiate one term correctly. Expect $4 - x^{-3} = 12$ at $x = -\frac{1}{2}$ Alternative: substitute values of x into $\frac{dy}{dx}$. One value $x < -\frac{1}{2}$ and one value $-\frac{1}{2} < x < 0$.
	conclude minimum	A1	Following correct work only
5(c)	State increasing ...	B1	
	... with clear reference to first derivative always being positive [for $x > 0$]	B1	Dependent on first derivative being correct. It is not sufficient to substitute values of x .
		2	

Question	Answer	Marks	Guidance
5	$[7C1a^6b(x)], [7C2a^5b^2(x^2)], [7C4a^3b^4(x^4)]$	B2, 1, 0	SOI, can be seen in an expansion.
	$\frac{7C2a^5b^2(x^2)}{7C1a^6b(x)} = \frac{7C4a^3b^4(x^4)}{7C2a^5b^2(x^2)} \rightarrow \frac{21a^5b^2}{7a^6b} = \frac{35a^3b^4}{21a^5b^2}$	M1 A1	M1 for a correct relationship OE (Ft from <i>their</i> 3 terms). For A1 binomial coefficients must be correct & evaluated.
	$\frac{a}{b} = \frac{5}{9}$	A1	OE
		5	

Question	Answer	Marks	Guidance
8(a)	$r = \frac{a}{a+2}$	B1	OE SOI
	$\frac{a}{1 - \frac{a}{a+2}} = 264$	M1	Use of ∞ formula.
	$\frac{a(a+2)}{a+2-a} = 264$ leading to $\frac{a(a+2)}{2} = 264$ leading to $a^2 + 2a - 528 [= 0]$	M1*	Process to a 3 term quadratic or a 3 term cubic. May contain terms on LHS and RHS.
	$(a-22)(a+24) [= 0]$	DM1	Attempt to solve.
	$a = 22$ (only)	A1	22 without working SC DB1 (dep on 2 nd M1).
		5	
8(b)	$d = \frac{6^2}{6+2} - 6 = -\frac{3}{2}$	B1	
	$\frac{n}{2} \left\{ 12 + (n-1) \left(\frac{-3}{2} \right) \right\} < -480$	M1*	Forming an inequation with <i>their</i> numerical d . May use an equality.
	$[3](n^2 - 9n - 640) > 0]$	A1	OE May contain terms on LHS and RHS.
	$[n =] \frac{9 \pm \sqrt{81 + 2560}}{2}$	DM1	OE. Expect 30.19 . Working for solution must be shown.
	31 only	A1	Must come from a correct first inequality (or an equality). 31 no working SC DB1 (dep on correct quadratic and correct inequality/equality).
		5	

Question	Answer	Marks	Guidance
5(a)	Angle $XYZ = \sin^{-1}\left(\frac{9}{11}\right) = 0.9582$	B1	AG. OE using cosine rule.
	or $\sin XYZ = \frac{9}{11}$ leading to $XYZ = 0.9582$	1	
5(b)	$XY = \sqrt{11^2 - 9^2} = \sqrt{40}$ or using 0.9582 and trigonometry	*M1 A1	
	$AB = 9 + 11 - \text{their } XY$	B1 FT	OE e.g. $20 - 2\sqrt{10}$, $2 + 9 - 2\sqrt{10} + 11 - 2\sqrt{10}$
	Arc $AC = 11 \times 0.9582$	M1	
	Arc $BC = 9 \times \frac{\pi}{2}$	M1	
	Perimeter = $[13.6(8) + 10.5(4) + 14.1(4) =] 38.4$	A1	AWRT. Answer must be evaluated as a single decimal.
		6	

Question	Answer	Marks
3(a)	$(y) = f(-x)$	B1
		1
3(b)	$(y) = 2f(x)$	B1
		1
3(c)	$(y) = f(x+4) - 3$	B1 B1
		2