

Question Number	Scheme	Marks
7ai	$f'(4) = \frac{4(4)^2 + 10 - 7(4)^{\frac{1}{2}}}{4(4)^{\frac{1}{2}}} = \frac{15}{2}$	B1
ii	$-\frac{15}{2} \rightarrow -\frac{2}{15}$	M1
	$y+1 = -\frac{2}{15}(x-4)$	M1
	$2x+15y+7=0$	A1
		(4)
b	$\frac{4x^2 + 10 - 7x^{\frac{1}{2}}}{4x^{\frac{1}{2}}} = \pm \dots x^{\frac{3}{2}} \pm \dots x^{-\frac{1}{2}} \pm \dots$	M1
	Two of the terms of $x^{\frac{3}{2}} + \frac{5}{2}x^{-\frac{1}{2}} - \frac{7}{4}$	A1
	$\int \left(x^{\frac{3}{2}} + \frac{5}{2}x^{-\frac{1}{2}} - \frac{7}{4} \right) dx = \frac{2}{5}x^{\frac{5}{2}} + 5x^{\frac{1}{2}} - \frac{7}{4}x (+c)$	dM1A1ft
	$\frac{2}{5}(4)^{\frac{5}{2}} + 5(4)^{\frac{1}{2}} - \frac{7}{4}(4) + c = -1 \Rightarrow c = \dots$	ddM1
	$(f(x)) = \frac{2}{5}x^{\frac{5}{2}} + 5x^{\frac{1}{2}} - \frac{7}{4}x - \frac{84}{5}$	A1
		(6)
		(10 marks)

Question	Answer	Marks	Guidance
7(c)	$gf(x) = 2\left(\frac{3}{x-2} + 1\right) - 2$ or $2\left(\frac{x+1}{x-2}\right) - 2$	M1	Substitute f(x) into g(x).
	$\frac{6}{x-2}$	A1	
		2	

Question	Answer	Marks
5	$\cos POA = \frac{5}{13} \rightarrow POA = 1.17(6)$ Allow 67.4° or $\sin = \frac{12}{13}$ or $\tan = \frac{12}{5}$	M1 A1
	Reflex $AOB = 2\pi - 2 \times \text{their } 1.17(6)$ OE in degrees or minor arc $AB = 5 \times 2 \times \text{their } 1.17(6)$	M1
	Major arc $= 5 \times \text{their } 3.93(1)$ or $2\pi \times 5 - \text{their } 11.7(6)$	M1
	AP (or BP) $= \sqrt{13^2 - 5^2} = 12$	B1
	Cord length = 43.7	A1
		6

Question Number	Scheme	Marks
3. (a)	$\int f(x) dx = \int x^{\frac{3}{2}} + 10x^{\frac{1}{2}} + 25x^{-\frac{1}{2}} dx = \frac{2}{5}x^{\frac{5}{2}} + \frac{20}{3}x^{\frac{3}{2}} + 50x^{\frac{1}{2}} + c$	M1 A1 A1 A1
(b) (i)	$f'(x) = \frac{3}{2}x^{\frac{1}{2}} + 5x^{-\frac{1}{2}} - \frac{25}{2}x^{-\frac{3}{2}}$	(4) M1 A1
	$f'(x) = 0 \Rightarrow \frac{3}{2}x^{\frac{1}{2}} + 5x^{-\frac{1}{2}} - \frac{25}{2}x^{-\frac{3}{2}} = 0 \text{ AND } \times x^{\frac{3}{2}}$	dM1
	$\frac{3}{2}x^2 + 5x^1 - \frac{25}{2} = 0 \Rightarrow 3x^2 + 10x - 25 = 0 *$	A1*
(ii)	$(x = \frac{5}{3}) \text{ only}$	B1 (5) (9 marks)

Question	Answer	Marks	Guidance
3(b)	Coefficient of x^4 is $a \times \text{their } -90a^3 + 7 \times \text{their } 15a^4$ [=15a ⁴]	M1	Must select two appropriate terms only.
	$15a^4 = 240$	DM1	Reducing to a simple quartic equation in a .
	$\Rightarrow a^4 = 16 \Rightarrow a = 2$	A1	A0 if $a = -2$ is given as a solution.
		3	

Question	Answer	Marks	Guidance
10(a)	$f'(x) = -(\frac{1}{2}x + k)^{-3}$	B1	
	$f'(2) > 0 \Rightarrow -(1+k)^{-3} > 0$	M1	Allow for solving <i>their</i> $f''(2) > 0$
	$k < -1$	A1	WWW
		3	
10(b)	$[f(x) = \int ((\frac{1}{2}x - 3)^{-2} - (-2)^{-2}) dx] \left\{ \begin{array}{l} (\frac{1}{2}x - 3)^{-1} \\ -1 \times \frac{1}{2} \end{array} \right\} \left\{ \begin{array}{l} -x \\ 4 \end{array} \right\}$	B1 B1	Allow $-2(\frac{1}{2}x + k)^{-1}$ OE for 1 st B1 and $-(1+k)^{-2}x$ OE for 2 nd B1
	$3\frac{1}{2} = 1 - \frac{1}{2} + c$	M1	Substitute $x = 2, y = 3\frac{1}{2}$ into <i>their</i> integral with c present.
	$f(x) = \frac{-2}{(\frac{1}{2}x - 3)} - \frac{x}{4} + 3$	A1	OE
		4	
10(c)	$(\frac{1}{2}x - 3)^{-2} - (-2)^{-2} = 0$	M1	Substitute $k = -3$ and set to zero.
	leading to $(\frac{1}{2}x - 3)^2 = 4$ [$\frac{1}{2}x - 3 = (\pm)2$] leading to $x = 10$	A1	
	$(10, -\frac{1}{2})$	A1	Or when $x = 10, y = -1 - 2\frac{1}{2} + 3 = -\frac{1}{2}$
	$f''(10) = -(-5 - 3)^{-3} \rightarrow < 0 \rightarrow \text{MAXIMUM}$	A1	WWW
		4	

Question	Answer	Marks	Guidance
3(a)	1+10x+40x ² May be part of a complete expansion	B2, 1, 0	1 ⁵ must be simplified to 1, allow if the '1' is seen in a more complete expansion but not the final answer. Mis-reads not condoned in this question.
		2	
3(b)	1-12x+54x ² May be part of a complete expansion	B2, 1, 0	1 ⁴ must be simplified to 1, allow if the '1' is seen in a more complete expansion but not the final answer. Mis-reads not condoned in this question.
		2	
3(c)	54-120+40	M1	Forming exactly 3 products correctly using their terms.
	-26	A1	Allow -26x ² If in a list with other terms it must be clear this is the required term otherwise A0.
		2	

Question	Scheme	Marks
6(a)	E.g. $m = \frac{2-11}{8+4}$ or $m = \frac{11-2}{-4-8}$	M1
	$m = -\frac{3}{4}$	A1
		(2)
(b)	M is $\left(2, \frac{13}{2}\right)$	B1
	$m_N = -1 \div -\frac{3}{4}$	M1
	$y - \frac{13}{2} = \frac{4}{3}(x - 2)$	M1
	$8x - 6y + 23 = 0$	A1
		(4)
(c)	$AB = \sqrt{(-4-8)^2 + (11-2)^2} (=15)$ or $AB^2 = (-4-8)^2 + (11-2)^2 (=225)$	M1
	$\frac{1}{2} \times MC \times AB = 37.5 \Rightarrow MC = \frac{75}{15} (=5)$ or $MC^2 = 25$	M1
	$m_N = \frac{4}{3}, MC = 5 \Rightarrow C$ is $\left(2-3, \frac{13}{2}-4\right)$ or $\left(2+3, \frac{13}{2}+4\right)$	dM1
	(-1, 2.5) or (5, 10.5) or $x = -1, x = 5$ or $y = 2.5, y = 10.5$	A1
	(-1, 2.5) and (5, 10.5)	A1
		(5)
		(11 marks)

Question	Answer	Marks	Guidance
6(c)	$(f(x)) > \frac{2}{3}$	B1	Allow $(y) > \frac{2}{3}$. Do not allow $x > \frac{2}{3}$
		1	

Question	Answer	Marks	Guidance
6	Use of $\sin^2\alpha + \cos^2\alpha = 1$ eg $\sin\alpha = [\pm]\sqrt{1 - \left(\frac{8}{17}\right)^2}$	*M1	Or Pythagoras seen (may quote 8, 15, 17 triple).
	$\sin\alpha = \frac{15}{17}$	A1	
	$\tan\alpha = \frac{15}{8}$	A1	
	$\frac{1}{\sin\alpha} + \frac{1}{\tan\alpha} = \frac{17}{15} + \frac{8}{15}$	DM1	Dealing with reciprocals and addition of fractions correctly.
	$= \frac{5}{3}$ oe	A1	Correct answer with no working shown scores 0. Extra answers from $\sin\alpha = -\frac{15}{17}$ are allowed.
		5	

Question	Answer	Marks	Guidance
1	$[f(x)=] 2x^3 + \frac{8}{x} [+c]$	B1	Allow any correct form
	$7 = 16 + 4 + c$	M1	Substitute $f(2) = 7$ into an integral. c must be present. Expect $c = -13$
	$f(x) = 2x^3 + \frac{8}{x} - 13$	A1	Allow $y =$, $f(x)$ or y can appear earlier in answer
		3	

Question	Answer	Marks	Guidance
11(a)	$(5-2p)^2 + (p+2)^2 = (10-2p)^2 + (3-p)^2$	M1 A1	Allow one sign error for M mark only.
	$25 - 20p + 4p^2 + p^2 + 4p + 4 = 100 - 40p + 4p^2 + 9 - 6p + p^2$	A1	Allow 2.67 AWRT.
	$30p = 80 \rightarrow p = \frac{8}{3}$ oe		
		3	

Question	Answer	Marks	Guidance
11(b)(i)	$m_{AC} = \frac{p+2}{2p-5}$ $m_{BC} = \frac{p-3}{2p-10}$	M1	Allow a sign error.
	$\frac{p+2}{2p-5} \times \frac{p-3}{2p-10} = -1$	M1	Use of $m_1 m_2 = -1$ with their m_{AC} and m_{BC} .
	$p^2 - p - 6 = -(4p^2 - 30p + 50) \rightarrow 5p^2 - 31p + 44 (=0)$	A1	
	$p = 4$ (Ignore $p = \frac{11}{5}$)	A1	Factors $(p-4)(5p-11)$, or formula or completing square must be seen.
		4	
11(b)(ii)	Mid-point of $AB = (7\frac{1}{2}, \frac{1}{2})$	B1	SOI
	$r^2 = 2\frac{1}{2}^2 + 2\frac{1}{2}^2 \left[= \frac{50}{4} \right]$ or $r = \sqrt{(2\frac{1}{2})^2 + 2\frac{1}{2}^2} \left[= \frac{5\sqrt{2}}{2} \right]$	*M1	Or $r^2 = \frac{1}{4}(5^2 + 5^2) \left[= \frac{50}{4} \right]$ etc.
	Equation of circle is $(x - \text{their } 7\frac{1}{2})^2 + (y - \text{their } \frac{1}{2})^2 = \text{their } \frac{50}{4}$	DM1	Must use r^2 not r or d or d^2
	$x^2 + y^2 - 15x - y + 44 = 0$	A1	CAO
		4	