

Question Number	Scheme	Marks
<b>2 (a)</b>	Strip width = 1.5	B1
	$\frac{3}{4}\{4.16 + 2.28 + 2 \times (2.91 + a + 1.73 + 1.37 + 1.43)\} = 19.3 \Rightarrow a = \dots$ $a = \text{awrt } 2.21$	M1 A1
		<b>(3)</b>
<b>(b)</b>	$\int_{-4}^5 (2f(x) - 3) dx = 2 \times 19.3 - [3x]_{-4}^5$ $= 11.6$	M1 A1
		<b>Total 5</b>

Question	Answer	Marks	Guidance
1	Use correct logarithm property to simplify left-hand side	<b>M1</b>	Or equivalent method
	Use correct process to obtain equation without logarithms	<b>M1</b>	
	Obtain $\frac{2x+1}{x-3} = e^2$	<b>A1</b>	OE
	Obtain $x = \frac{3e^2 + 1}{e^2 - 2}$	<b>A1</b>	OE
		<b>4</b>	

Question Number	Scheme	Notes	Marks
<b>3(a)</b>	$a(-4)^3 - (-4)^2 + b(-4) + 4 = -108$ <p>Attempts to set <math>f(-4) = -108</math> to obtain an equation in <math>a</math> and <math>b</math>. Score when you see “-4” embedded in the equation or 2 correct terms (excluding the “+4”) on lhs. May be implied by e.g. <math>-64a - 16 - 4b + 4 = -108</math> Condone minor slips on the lhs e.g. one sign error between terms but must use -108</p>		M1
	<p>As an alternative for the first mark we will condone an attempt at long division. This requires a complete method to divide <math>(ax^3 - x^2 + bx + 4)</math> by <math>(x + 4)</math> to obtain a remainder in terms of <math>a</math> and <math>b</math> which is then equated to -108 For reference, the quotient is <math>ax^2 - (1+4a)x + 16a + b + 4</math> and the remainder is <math>-4b - 64a - 12</math></p>		
	$-64a - 16 - 4b + 4 = -108$ $\Rightarrow 16a + b = 24^*$	<p>Correct equation obtained with no errors and at least one line of intermediate working if starting with e.g. <math>a(-4)^3 - (-4)^2 + b(-4) + 4 = -108</math></p>	A1*
			(2)
<b>(b)</b>	$a\left(\frac{1}{2}\right)^3 - \left(\frac{1}{2}\right)^2 + b\left(\frac{1}{2}\right) + 4 = 0$ <p>Attempts to set <math>f\left(\frac{1}{2}\right) = 0</math> to obtain an equation in <math>a</math> and <math>b</math>. Condone slips. Score when you see “<math>\frac{1}{2}</math>” embedded in the equation or 2 correct terms (excluding the “+4”) on lhs. May be implied by e.g. <math>\frac{a}{8} - \frac{1}{4} + \frac{b}{2} + 4 = 0</math> The “=0” may be implied when they attempt to solve simultaneously below</p>		M1
	<p>An alternative for the first mark is to attempt long division. This requires a complete method to divide <math>(ax^3 - x^2 + bx + 4)</math> by <math>(2x - 1)</math> to obtain a remainder in <math>a</math> and <math>b</math> which is then equated to 0 For reference, the quotient is <math>\frac{a}{2}x^2 + \left(\frac{a}{4} - \frac{1}{2}\right)x + \left(\frac{b}{2} - \frac{1}{4} + \frac{a}{8}\right)</math> and the remainder is <math>\frac{15}{4} + \frac{b}{2} + \frac{a}{8}</math></p>		
	$16a + b = 24, a + 4b = -30$ $\Rightarrow a = \dots, b = \dots$	<p>Attempts to solve <math>16a + b = 24</math> simultaneously with their equation in <math>a</math> and <math>b</math>. This may be implied if values of <math>a</math> and <math>b</math> are obtained (e.g. calculator)</p>	M1
	$a = 2, b = -8$	<p>Correct values</p>	A1
			(3)
<b>(c)</b>	$f(x) = 2x^3 - x^2 - 8x + 4$ $\Rightarrow f'(x) = 6x^2 - 2x - 8$	<p>Correct derivative (follow through their <math>a</math> and <math>b</math>). Allow unsimplified and apply isw if necessary. Allow with the letters “<math>a</math>” and “<math>b</math>” and a “made up” “<math>a</math>” and “<math>b</math>”.</p>	B1ft
			(1)

Question Number	Scheme	Marks
<b>2a</b>	$\left(f\left(\frac{3}{2}\right) = 4\left(\frac{3}{2}\right)^3 - 8\left(\frac{3}{2}\right)^2 + 5\left(\frac{3}{2}\right) + a = 0 \Rightarrow a = \dots\right.$ $\Rightarrow \frac{27}{2} - 18 + \frac{15}{2} + a = 0 \Rightarrow a = -3 \quad *$	M1 A1*
(2)		
<b>b</b>	<p>Example where <math>2x-3</math> is a linear factor:</p> $\begin{array}{r} 2x^2 - x + 1 \\ 2x-3 \overline{) 4x^3 - 8x^2 + 5x - 3} \\ \underline{4x^3 - 6x^2} \phantom{+ 5x - 3} \\ -2x^2 + 5x \phantom{- 3} \\ \underline{-2x^2 + 3x} \phantom{- 3} \\ +2x - 3 \\ \underline{+2x - 3} \\ 0 \end{array}$ <p><math>(-1)^2 - 4 \times 2 \times 1 = -7 &lt; 0 \Rightarrow</math> no real roots so <math>x = \frac{3}{2}</math> is the only one real root *</p>	M1A1  dM1A1*
(4)		
		<b>(6 marks)</b>