

Question	Answer	Marks	Guidance
3(a)	$P(WW) = P(AWW) + P(BWW) =$ $\frac{2}{6} \times \frac{8}{15} \times \frac{7}{14} + \frac{4}{6} \times \frac{6}{15} \times \frac{5}{14}$	M1	Either $\frac{2}{6} \times \frac{8}{15} \times \frac{7}{14}$ or $\frac{4}{6} \times \frac{6}{15} \times \frac{5}{14}$ seen, accept unsimplified.
		M1	$\frac{q}{6} \times \frac{r}{15} \times \frac{r-1}{14} + \frac{6-q}{6} \times \frac{s}{15} \times \frac{s-1}{14}$ seen, no additional terms, accept unsimplified. Condone $\frac{q}{6} \times \frac{r}{15} \times \frac{r}{15} + \frac{6-q}{6} \times \frac{s}{15} \times \frac{s}{15}$, $1 \leq q \leq 5, 1 < r, s < 9$.
	$\left[= \frac{56}{630} + \frac{60}{630} = \frac{4}{45} + \frac{2}{21} \right] = \frac{58}{315}$ or 0.184	A1	SC B1 for 58/315 if either M mark withheld.
		3	

Question	Answer	Marks	Guidance
3(b)	$\left[P(B WR \text{ or } RW) = \frac{P(W \& R \text{ from bag B})}{P(W \text{ and } R)} = \right]$ $\frac{\frac{4}{6} \times \frac{6}{15} \times \frac{7}{14} + \frac{4}{6} \times \frac{7}{15} \times \frac{6}{14}}{\frac{2}{6} \times \frac{8}{15} \times \frac{4}{14} + \frac{2}{6} \times \frac{4}{15} \times \frac{8}{14} + \frac{4}{6} \times \frac{6}{15} \times \frac{7}{14} + \frac{4}{6} \times \frac{7}{15} \times \frac{6}{14}}$ or $\frac{2 \times \frac{4}{6} \times \frac{6}{15} \times \frac{7}{14}}{2 \times \frac{2}{6} \times \frac{8}{15} \times \frac{4}{14} + 2 \times \frac{4}{6} \times \frac{6}{15} \times \frac{7}{14}}$	B1	P(W & R from bag B) $= \frac{2}{3} \times \frac{6}{15} \times \frac{7}{14} + \frac{2}{3} \times \frac{7}{15} \times \frac{6}{14}$ or $2 \times \frac{2}{3} \times \frac{6}{15} \times \frac{7}{14} [= \frac{4}{15} \text{ or } 0.267]$ Seen alone or as numerator/denominator of conditional probability.
		M1	P(WR or RW) = P(W & R from bag A) + P(W & R from bag B) $= a \times \frac{2}{6} \times \frac{8}{15} \times \frac{4}{14} + a \times \frac{4}{6} \times \frac{6}{15} \times \frac{7}{14}$ or $= a \times \frac{2}{6} \times \frac{8}{15} \times \frac{4}{14} + \text{their } P(W \& R \text{ from bag B})$ $a = 1 \text{ or } 2$. [expect $\frac{116}{315}$ or 0.368] Seen alone or as numerator/denominator of conditional probability.
	$\frac{168}{630} \div \frac{232}{630} = \frac{4}{15} \div \frac{116}{315}$	M1	<u>their identified P(W & R from bag B)</u> <u>their identified P(WR or RW)</u> Accept unsimplified.
	$= \frac{168}{232} \div \frac{21}{29}$ or 0.724	A1	0.7241379 to at least 3SF.
		4	

Question	Answer	Marks	Guidance
3(a)	Box A Box B	B1	Correct structure and probabilities for Box A branches.
		B1	Completely correct structure and one correct probability for a Box B branch including label for G or Y.
		B1	Completely correct structure and second correct probability on a Box B branch including label G or Y.
		B1	Completely correct structure and remaining two probabilities correct on Box B branches, including labels for G or Y. SC B1 if correct shape diagram but only four correct algebraic probs for GG, GY, YG and YY.
		4	
3(b)	$P(\text{same colour}) = \frac{6}{9} \times \frac{5}{5+x} + \frac{3}{9} \times \frac{1+x}{5+x}$	M1	$P(GG) + P(YY) =$ $\left(\frac{6}{9} \text{ or } \frac{3}{9} \right) \times \text{their } \left(\frac{5}{5+x} \right) + \left(\frac{3}{9} \text{ or } \frac{6}{9} \right) \times \text{their } \left(\frac{1+x}{5+x} \right)$
	$\frac{6}{9} \times \frac{5}{5+x} + \frac{3}{9} \times \frac{1+x}{5+x} = \frac{8}{15}$ and arrange as a linear equation	M1	$15(x+11) = 24(x+5)$ OE Accept sum of their products equated to $\frac{8}{15}$ and rearranged to form a linear equation.
	Solve: $x = 5$	A1	
		3	

Question	Answer	Marks	Guidance
7(a)	Probabilities: $\frac{x+1}{x+10}$, $\frac{9}{x+10}$, $\frac{x}{x+10}$, $\frac{10}{x+10}$	B1	One probability correct in correct position.
		B1	Another probability correct in correct position.
		B1	Other two probabilities correct in correct positions.
		3	
7(b)	$\frac{4}{10} \times \text{their } \frac{10}{x+10}$	M1	Method consistent with <i>their</i> tree diagram.
	$\frac{4}{x+10}$	A1	AG
		2	

Question	Answer	Marks	Guidance
7(c)	$\frac{4}{x+10} = \frac{1}{6}$ $x+10=24$, $x=14$	B1	Find value of x. Can be implied by correct probabilities in calculation.
	$P(\text{ARed} \text{BRed}) = P(\text{ARed} \cap \text{BRed}) \div P(\text{BRed})$ $\frac{\frac{6}{10} \times \text{their } \frac{x+1}{x+10}}{\frac{6}{10} \times \text{their } \frac{x+1}{x+10} + \frac{4}{10} \times \text{their } \frac{x}{x+10}} = \frac{\frac{6}{10} \times \frac{15}{24}}{\frac{6}{10} \times \frac{15}{24} + \frac{4}{10} \times \frac{14}{24}} = \frac{3}{8}$	B1 FT	$\frac{6}{10} \times \text{their } \frac{x+1}{x+10}$ as numerator or denominator of fraction.
		M1	$\frac{6}{10} \times \text{their } \frac{x+1}{x+10} + \frac{4}{10} \times \text{their } \frac{x}{x+10}$ seen anywhere.
		A1 FT	Seen as denominator of fraction.
	$\frac{45}{73}$, 0.616[4...]	A1	If B0 M0: SC B1 for $\frac{3}{8}$ or $\frac{0.375}{0.6083}$ SC B1 $\frac{45}{73}$ or 0.616.
		5	

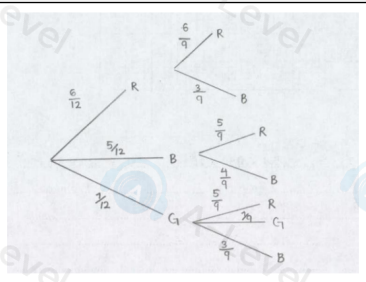
Question	Answer	Marks	Guidance
4(a)	[Possible cases: 1 1 2, 1 2 1, 2 1 1] Probability = $\left(\frac{1}{6}\right)^3 \times 3$	M1	$\left(\frac{1}{6}\right)^3 \times k$, where k is an integer.
		M1	Multiply a probability by 3, not +, – or ÷
	$\frac{1}{72}$	A1	Accept $\frac{3}{216}$ or 0.0138 or 0.0139
		3	
4(b)	$P(18) = \left(\frac{1}{6}\right)^3 \left[= \frac{1}{216} \right]$	B1	
	$P(18 \text{ on } 5\text{th throw}) = \left(\frac{215}{216}\right)^4 \times \frac{1}{216}$	M1	$(1-p)^4 p$, $0 < \text{their } p < 1$
	0.00454	A1	
		3	

Question	Answer	Marks	Guidance
7(a)	$[P(SR \text{ TR}) + P(SW \text{ TR})] = \frac{3}{8} \times \frac{2}{7} + \frac{5}{8} \times \frac{3}{7}$	M1	$\frac{3}{8} \times \frac{2}{7} + k$ or $l + \frac{5}{8} \times \frac{3}{7}$ $0 < k, l < 1$
	$= \frac{21}{56} + \frac{15}{56}, 0.375$	A1	SC B1 for $\frac{3}{8}$ with no explanation.
		2	
7(b)	$[RRWR, WRRR, WRWR]$ $\frac{3}{8} \times \frac{2}{7} \times \frac{5}{6} \times \frac{1}{5} + \frac{5}{8} \times \frac{3}{7} \times \frac{2}{6} \times \frac{1}{5} + \frac{5}{8} \times \frac{3}{7} \times \frac{4}{6} \times \frac{2}{5}$ $[\frac{1}{56} + \frac{1}{56} + \frac{1}{14}]$	M1	$\frac{m}{8} \times \frac{n}{7} \times \frac{o}{6} \times \frac{q}{5}$ $1 \leq m, n, o, q \leq 5, m \neq n \neq o \neq q$
		A1	Probability for one scenario correct, accept unsimplified.
		M1	Adding probabilities for 3 correct scenarios and no incorrect.
	$= \frac{180}{1680} + \frac{3}{28}, 0.107$	A1	Or 0.1071428... to 4SF or better. SC B1 for 3/28 with inadequate explanation.
		4	

Question	Answer	Marks	Guidance
7(c)	$[P(S \text{ first disc R } T2) = \frac{30}{3} = \frac{1}{3}]$ $\frac{1680}{28} = \frac{56}{3}$	M1	their $P(RRWR)$ or $\frac{3}{8} \times \frac{2}{7} \times \frac{5}{6} \times \frac{1}{5}$ their 7(b) – must be a prob or $\frac{3}{28}$
	$\frac{1}{6}, 0.167$	A1	
		2	

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Question	Answer	Marks
1(a)	Fully correct labelled tree for method of transport with correct probabilities.	B1
	Fully correct labelled branches with correct probabilities for lateness with either 1 branch after W or 2 branches with the probability 0.	B1
		2
1(b)	$P(C E) = \frac{P(C \cap E)}{P(E)} = \frac{0.2 \times 0.6}{0.2 \times 0.6 + 0.45 \times 0.1 + 0.35 \times 1}$	M1
	Summing three appropriate 2-factor probabilities	M1
	$\frac{0.12}{0.515}$	A1
	0.233 or $\frac{12}{515}$	A1
		4

Question	Answer	Marks	Guidance
5(a)	 Probabilities for Bag A selection R,B,G ($\frac{6}{12}, \frac{5}{12}, \frac{1}{12}$) Probabilities for Bag B selection: $\frac{6}{9}, \frac{3}{9}, [0]$ $\frac{5}{9}, \frac{4}{9}, [0]$ $\frac{5}{9}, \frac{3}{9}, \frac{1}{9}$	B1	Correct structure and probabilities for Bag A branches which must be the first set of branches, including labels R, B, G.
		B1	Correct structure and probabilities for one Bag B branch, including labels R, B, [G]. Condone inclusion of branches with 0 probability.
		B1	Correct structure and probabilities for remaining Bag B branches, including labels R, B, [G]. Condone inclusion of branches with 0 probability. Additional branches without a probability of zero lose this mark.
		3	
5(b)	$[P(RR) + P(BB) + P(GG)] = \frac{6}{12} \times \frac{6}{9} + \frac{5}{12} \times \frac{4}{9} + \frac{1}{12} \times \frac{1}{9}$	M1	Correct or FT tree diagram probabilities with all 3 (R, B and G) branches. Note: working may be by tree diagram.
	$= \frac{57}{108}, \frac{19}{36}$	A1	Accept 0.5278, 0.528.
		2	

Question	Answer	Marks	Guidance
5(c)	$P(A \text{ blue} B \text{ blue}) = \frac{\frac{5}{12} \times \frac{4}{9}}{\frac{6}{12} \times \frac{3}{9} + \frac{5}{12} \times \frac{4}{9} + \frac{1}{12} \times \frac{3}{9}}$	M1	$\frac{5}{12} \times \frac{4}{9}$ or $\frac{20}{108}$ or $\frac{5}{27}$ or <i>their</i> P(BB) from Q5(b) seen as a numerator of a single fraction. FT tree diagram with values from only 2 bags.
		B1 FT	$\frac{6}{12} \times \frac{3}{9} + \frac{5}{12} \times \frac{4}{9} + \frac{1}{12} \times \frac{3}{9}$ seen as the denominator of a single fraction. $\frac{5}{27}$ or <i>their</i> P(BB) may be seen from Q5b in place of $\frac{5}{12} \times \frac{4}{9}$ FT tree diagram with values from only 2 bags.
	$= \frac{20}{41}$	A1	Accept 0.488, 0.4878. SCB1 if either M or B mark not scored $\frac{20}{41}$ or 0.4878.
		3	

Question	Answer	Marks	Guidance
6(a)		B1	First and second jumps correct with probabilities and outcomes identified.
		B1	Third jump correct with probabilities and outcomes identified.
		2	
6(b)	SFF $0.2 \times 0.7 \times 0.9 = 0.126$ FSF $0.8 \times 0.1 \times 0.7 = 0.056$ FFS $0.8 \times 0.9 \times 0.1 = 0.072$	M1	Two or three correct 3 factor probabilities added, correct or FT from part 6(a). Accept unsimplified.
	[Total = probability of 1 success =] $0.254 \left(\frac{127}{500} \right)$	A1	Accept unsimplified.
	[Probability of at least 1 success = $1 - 0.8 \times 0.9 \times 0.9 = 0.352 \left(\frac{44}{125} \right)$	B1 FT	Accept unsimplified.
	$P(\text{exactly 1 success} \mid \text{at least 1 success}) = \frac{\text{their } 0.254}{\text{their } 0.352}$	M1	Accept unsimplified.
	$0.722, \frac{127}{176}$	A1	$0.7215 < p \leq 0.722$
		5	

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Question	Answer	Marks	Guidance
6(c)	$0.8 \times 0.9 \times 0.9 \times 0.1 \times 0.3 \times 0.3 = 0.005832$ [FFFSSS] $0.2 \times 0.3 \times 0.3 \times 0.7 \times 0.9 \times 0.9 = 0.010206$ [SSSFFF]	M1	$a \times b \times c \times d \times e \times f$ FT from <i>their</i> tree diagram. Either a, b and c all = 0.8 or 0.9 (at least one of each) and d, e and f all = 0.1 or 0.3 (at least one of each). Or $a, b, c = 0.2$ or 0.3 (at least one of each) and $d, e, f = 0.7$ or 0.9 (at least one of each).
		A1	Either correct. Accept unsimplified.
	[Total =] 0.0160[38]	A1	
		3	