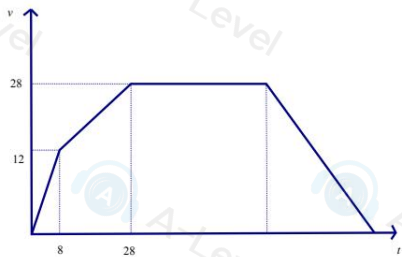


Question	Scheme	Marks	Notes
6. (a)	$\mathbf{v} = (10\mathbf{i} + 4\mathbf{j}) + 6(-2\mathbf{i} + 3\mathbf{j})$	M1	Use of $\mathbf{v} = \mathbf{u} + \mathbf{a}t$ with $t = 6$
	$= -2\mathbf{i} + 22\mathbf{j}$	A1	
	$\tan \theta = \pm \frac{22}{2}$ or $\tan \theta = \pm \frac{2}{22}$	M1	Correct use of trig to find a relevant angle for their $\mathbf{v}$
	$\theta = 85^\circ$ or 5°	A1	Seen or implied
	bearing is 355°	A1	
		(5)	
(b)	$\mathbf{v} = (10\mathbf{i} + 4\mathbf{j}) + t(-2\mathbf{i} + 3\mathbf{j})$	M1	Use of $\mathbf{v} = \mathbf{u} + \mathbf{a}t$
	$(= (10 - 2t)\mathbf{i} + (4 + 3t)\mathbf{j})$	A1	Correct unsimplified
	$(10 - 2t) = (4 + 3t)$	DM1	Equate coefficients to give equation in t only
	$t = 1.2$	A1	
		(4)	
		[9]	

QUESTION NUMBER	SCHEME	MARKS
	N.B. They may do (ii) first using the OR method to find α (and possibly β) and then use either angle to do (i), using the Sine Rule or Cosine Rule.	
4		
4(i)	Complete method to find an equation in X only: - Using correct vector triangle with cosine rule: $129 = X^2 + (5\sqrt{3})^2 - 2X \times 5\sqrt{3} \cos 30^\circ$ - Using correct vector triangle with sine rule to find α: $\frac{\sqrt{129}}{\sin 30^\circ} = \frac{5\sqrt{3}}{\sin \alpha}$ $\alpha = 22.4109..^\circ \Rightarrow \beta = 180^\circ - 30^\circ - 22.4109..^\circ = 127.589..^\circ$ Then sine rule: $\frac{X}{\sin \beta} = \frac{\sqrt{129}}{\sin 30^\circ} = \frac{5\sqrt{3}}{\sin \alpha}$ or cosine rule: $(5\sqrt{3})^2 = X^2 + 129 - 2X\sqrt{129} \cos \alpha$ or $X^2 = (5\sqrt{3})^2 + 129 - 2 \times 5\sqrt{3} \times \sqrt{129} \cos \beta$ to find X. - Using components with magnitude: $\sqrt{129} = \sqrt{(X \cos 30^\circ - 5\sqrt{3})^2 + (X \sin 30^\circ)^2}$	M1 A1
	Solves their equation (if quadratic, must include an X term) to find an X value.	M1
	$X = 18$	A1
4(ii)	EITHER Finds an equation in β only using their X: e.g. $\frac{18}{\sin \beta} = \frac{\sqrt{129}}{\sin 30^\circ}$	M2

	or $18^2 = (5\sqrt{3})^2 + 129 - 2 \times 5\sqrt{3} \times \sqrt{129} \cos \beta$ or $\cos \beta = \frac{\mathbf{R} \cdot \mathbf{Q}}{ \mathbf{R} \mathbf{Q} }$ where R is the resultant (β) = 128° to nearest degree OR Finds a relevant angle (not β) first - Using triangle of forces: $\alpha = \sin^{-1} \left(\frac{\sin 30^\circ \times 5\sqrt{3}}{\sqrt{129}} \right) = 22.4109^\circ$ Or: $\alpha = \cos^{-1} \left(\frac{18^2 + 129 - (5\sqrt{3})^2}{2 \times 18 \times \sqrt{129}} \right) = 22.4109^\circ$ - Using components: Resultant force = $(18 \cos 30^\circ - 5\sqrt{3})\mathbf{i} + (18 \sin 30^\circ)\mathbf{j}$ Leading to $\tan^{-1} \left(\frac{4\sqrt{3}}{9} \right) = 37.589^\circ$ or $\tan^{-1} \left(\frac{9}{4\sqrt{3}} \right) = 52.411^\circ$ or e.g. $\sin^{-1} \left(\frac{9}{\sqrt{129}} \right) = 52.411^\circ$	A1 A1 M1 A1
	Completes the method to find required angle (β) eg $150^\circ - \alpha$ or $210^\circ + \alpha$ $180^\circ - 52.411^\circ$ or $180^\circ + 52.411^\circ$ $90^\circ + 37.859^\circ$ or $270^\circ - 37.859^\circ$	M1
	(β) = 128° to nearest degree Accept 232°	A1
		(8)
	Notes for question 4	
	N.B. If 150° is used in either the sine or cosine rule, they are using an incorrect vector triangle and no M marks are available.	
(i) M1	Complete method to form an equation in X only. This could involve cosine rule and/or sine rule or components. Note the component forms: $\mathbf{P} = X \cos 30^\circ \mathbf{i} + X \sin 30^\circ \mathbf{j}$, condone cos/sin confusion $\mathbf{Q} = -5\sqrt{3}\mathbf{i}$ oe (they could have chosen different + directions)	
A1	Correct equation	

Question Number	Scheme	Marks	Notes
6(a)	$v_1 = 8 \times 1.5 (= 12)$ $v_2 = 12 + 0.8 \times 20$ $v_2 = 28 \text{ m s}^{-1}$	M1 M1 A1 (3)	Use of $v = u + at$ or equivalent for $t = 8$ Follow their 12
(b)		B1 B1ft (2) M1 A1ft A1ft A1 (4)	shape nos: 8,28; 12,28 indicated. Follow their 12, 28 Correct method for distance for the triangle (0-8) or the trapezium (8-28) Follow their 12 Follow their 12, 28 Correct answer only (cao)
(c)	first 8 s: $\text{dist} = \frac{1}{2} \times 8 \times 12 (= 48)$ next 20 s: $\text{dist} = \frac{1}{2} \times (12 + 28) \times 20 (= 400)$ Total dist = 448 m	M1 A1ft A1ft A1 (4)	Find area of right hand triangle or an expression in T for the trapezium (rectangle + triangle). Follow their 28 Form an equation in T for their 16, 448 and 140
(d)	$0 = 28^2 - 2 \times 2.8s$ $s = \frac{28^2}{2 \times 2.8} (= 140)$ $448 + 140 + 28T = 2000$ $T = \frac{2000 - 448 - 140}{28} = 50.4$	M1 A1ft DM1 A1 (4)	Or better (50.42857...) Accept 50.
		[13]	

Question Number	Scheme	Marks
6(a)	Speed = $\sqrt{4^2 + 5^2} = \sqrt{41}$ or 6.4031...m s ⁻¹ (Accept 6.4 or better)	M1A1 (2)
(b)	$(\mathbf{r} =)(3\mathbf{i} - 2\mathbf{j}) + t(4\mathbf{i} + 5\mathbf{j})$.	M1A1 (2)
(c)	$\mathbf{j}$ comp = 6 $5T - 2 = 6$ $T = \frac{8}{5}$ (=1.6)	M1 A1 (2)
(d)	$t = 1.6 \Rightarrow (\mathbf{r} =)(3 + (4 \times 1.6))\mathbf{i} (+6\mathbf{j})$ boy travels $9.4 - 1 = 8.4$ m (allow 8.4i) $\frac{8.4}{1.6}$ or $\frac{8.4\mathbf{i}}{1.6}$ $v = 5.25$	M1A1ft A1 DM1 A1 (5) [11]
Notes for qu 6		
6a	M1 for attempt to find magnitude of velocity A1 6.4 or better	
6b	M1 for attempt at pv with correct structure i.e. $\mathbf{r}_0 + t\mathbf{v}$ A1 for a correct expression seen (ie use isw)	
6c	M1 for equating $\mathbf{j}$ cpt of their $\mathbf{r}$ to 6 (Must be of form: $a + bT = 6$ oe) A1 for 1.6 oe	
6d	First M1 for substituting their answer for (c), their T , into $\mathbf{i}$ cpt of their answer for (b) oe First A1 ft, with or without $\mathbf{i}$ Second A1 for 8.4 or 8.4i cao Second DM1, dependent on first M1, for dividing their distance or vector (ci) by their T (> 0) value to find the value of v . (9.4/ T oe is DM0) Third A1 for 5.25 cao	

3.(a) (b) (c)	$\tan \alpha = 1/3 \Rightarrow \alpha = 18.4^\circ$ Bearing is 288° (nearest degree) $\mathbf{r} = (21\mathbf{i} + 5\mathbf{j}) + t(-6\mathbf{i} + 2\mathbf{j})$ $21 - 6t = -(5 + 2t)$ $t = 6.5$	M1 A1 A1 (3) B1 (1) M1 A1 A1 (3) 7
	<u>NOTES</u> <u>Question 3(a)</u> First M1 for $\arctan(\frac{+2}{\pm 6})$ First A1 for a correct value from their expression, usually 18.4° or 71.6° Second A1 for 288 (nearest degree) <u>Question 3(b)</u> B1 for $(21\mathbf{i} + 5\mathbf{j}) + t(-6\mathbf{i} + 2\mathbf{j})$ <u>Question 3(c)</u> M1 for equating the negative of their $\mathbf{i}$-component to their $\mathbf{j}$-component or Allow equating the components for the M mark. First A1 for a correct equation. Second A1 for $t = 6.5$	