

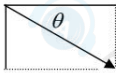
3.(a) (b) (c)	$\tan \alpha = 1/3 \Rightarrow \alpha = 18.4^\circ$ Bearing is 288° (nearest degree) $\mathbf{r} = (21\mathbf{i} + 5\mathbf{j}) + t(-6\mathbf{i} + 2\mathbf{j})$ $21 - 6t = -(5 + 2t)$ $t = 6.5$	M1 A1 A1 (3) B1 (1) M1 A1 A1 (3) 7
	<u>NOTES</u> <u>Question 3(a)</u> First M1 for $\arctan\left(\frac{+2}{\pm 6}\right)$ First A1 for a correct value from their expression, usually 18.4° or 71.6° Second A1 for 288 (nearest degree) <u>Question 3(b)</u> B1 for $(21\mathbf{i} + 5\mathbf{j}) + t(-6\mathbf{i} + 2\mathbf{j})$ <u>Question 3(c)</u> M1 for equating the negative of their $\mathbf{i}$-component to their $\mathbf{j}$-component oe Allow equating the components for the M mark. First A1 for a correct equation. Second A1 for $t = 6.5$	

Question Number	Scheme	Marks
4.(a)	$\mathbf{p} = (-5\mathbf{i} + 9\mathbf{j}) + t(\mathbf{i} - 2\mathbf{j})$	M1 A1 (2)
(b)	$2 = 9 - 2t$ $t = 3.5$ $\mathbf{p} = (-5\mathbf{i} + 9\mathbf{j}) + 3.5(\mathbf{i} - 2\mathbf{j}) = (-1.5\mathbf{i} + 2\mathbf{j})$	M1 A1 M1 A1 (4)
(c)	$\frac{2b-1}{5-2b} = \frac{1}{-2}$ $b = -1.5$	M1 A1 DM1 A1 (4) 10
Notes		
4.(a)	M1 for clear attempt at $\mathbf{p} = (-5\mathbf{i} + 9\mathbf{j}) + t(\mathbf{i} - 2\mathbf{j})$ (allow slips but must be ' + ') A1 if correct	
(b)	First M1 for equating the j component of their p to 2 First A1 for $t = 3.5$ Second M1 (independent) for substituting their t value into their p Second A1 for $(-1.5\mathbf{i} + 2\mathbf{j})$	
(c)	First M1 for $\frac{2b-1}{5-2b} = \pm \frac{1}{2}$ or $\frac{2b-1}{5-2b} = \pm \frac{2}{1}$ (must be in b only but allow slips) First A1 for a correct equation in b only Second M1 (dependent on first M1) for solving for b Second A1 for $b = -1.5$	

Question Number	Scheme	Marks
	N.B. Answers to (a) and (b) should be in terms of i and j , but only penalise once. Column vectors can be used in working.	
7(a)	$\mathbf{v}_B = (20 \sin \alpha)\mathbf{i} + (20 \cos \alpha)\mathbf{j}$ oe e.g. use of Pythagoras but must get to an answer $= 16\mathbf{i} + 12\mathbf{j} \text{ (km h}^{-1}\text{)}$	M1 A1 (2)
7(b)	$(\mathbf{s} =) (10\mathbf{i} + 5\mathbf{j}) + t(16\mathbf{i} + 12\mathbf{j})$ or $(10 + 16t)\mathbf{i} + (5 + 12t)\mathbf{j}$	M1 A1 ft (2)
7(c)	$\overrightarrow{AB} = \mathbf{s} - \mathbf{r} = (10\mathbf{i} + 5\mathbf{j}) + t(16\mathbf{i} + 12\mathbf{j}) - [20\mathbf{j} + 40t\mathbf{i}]$ $\overrightarrow{AB} = [(10 - 24t)\mathbf{i} + (12t - 15)\mathbf{j}] \text{ km}^*$	M1 A1* (2)
7(d)	$10 - 24t = 0$ and $12t - 15 = 0$ OR $40t = 10 + 16t$ and $20 = 5 + 12t$	M1
	$t = \frac{5}{12}$ and $\frac{5}{4}$ or one correct t value which is then used in the other equation correctly to show that the equation is not true.	A1
	Different t values oe so never collide*	A1* (3)
	ALT 1:	
	$(10 - 24t)^2 + (12t - 15)^2 = 0$ (i.e. $720t^2 - 840t + 325 = 0$)	M1
	$(-840)^2 - 4 \times 720 \times 325 (= -230,400) < 0$ Or roots $\frac{7 \pm 4i}{12}$ (calculator)	A1
	No real roots oe so never collide* N.B. Must see justification for 'no real roots' to score either of the A marks.	A1*
	ALT 2:	
	Finds minimum value of $720t^2 - 840t + 325$ or its square root using derivative or completing the square or calculator	M1
	80 or $\sqrt{80}$ or $\overrightarrow{AB} = -4\mathbf{i} - 8\mathbf{j}$ (at $t = \frac{7}{12}$)	A1
	so never collide*	A1*
7(e)	$10 - 24t = 12t - 15$ oe $t = \frac{25}{36}$ or 0.69 or better	M1 A1
	$\overrightarrow{AB} = \left[(10 - 24 \times \frac{25}{36})\mathbf{i} + (12 \times \frac{25}{36} - 15)\mathbf{j} \right] \text{ (km)}$	M1
	$AB = 20 \frac{\sqrt{2}}{3}, 9.4$ or better (km)	A1 (4)
		(13)

	Notes	
7(a)	M1: Condone sign errors and sin/cos confusion but both components must be resolved. Allow if they use $\cos(\frac{3}{5})$ or similar. If $12\mathbf{i} + 16\mathbf{j}$ appears without working, award M1A0. A1: cao	
7(b)	M1: Correct structure, condone slips A1ft: ft on their answer to (a)	
7(c)	M1: Allow $\mathbf{r} - \mathbf{s}$. $\mathbf{r}$ and $\mathbf{s}$ must be substituted. A1*: Correct given answer, correctly obtained N.B. Need to see $\overline{AB}$ at the start or finish for the A1* and answer must be exactly as printed, ignoring $[\]$ and km.	
7(d)	M1: They may use $\mathbf{r} = \mathbf{s}$ with both $\mathbf{i}$ and $\mathbf{j}$ cpts equated. A1: Need both t values. Accept 0.42 or better and 1.25. A1*: Correct conclusion	
7(e)	M1: Correct method A1: cao	
	M1: Sub their calculated t value into $\overline{AB}$ or $\overline{BA}$, seen or implied, oe. Note that this is an independent M mark. A1: cao	

[illegible]

Question Number	Scheme	Marks	Notes
5 (a)	Speed = $\sqrt{3^2 + (-2)^2}$ or $\sqrt{3^2 + 2^2} = \sqrt{13} \text{ m s}^{-1}$	M1 A1(2)	Use Pythagoras Accept 3.6 or better Ignore their diagram if it does not support their working
(b)	 $\tan \theta = \frac{2}{3}, \theta = 33.7$ OR $\tan \theta = \frac{3}{2}, \theta = 56.3$ OR find another useful angle Bearing = 124	M1 A1 A1 (3)	Find a relevant angle Their angle correct (seen or implied) Correct bearing. Accept 124° or awrt $124/124^\circ$ Accept N 124° E or S 56° E
(c)	$\mathbf{r}_B = 10\mathbf{j} + t(3\mathbf{i} - 2\mathbf{j})$ $\mathbf{r}_G = 4\mathbf{i} - 2\mathbf{j} + t\left(\frac{5}{3}\mathbf{i} + 2\mathbf{j}\right)$ $3t = 4 + \frac{5}{3}t$ OR $10 - 2t = -2 + 2t$ (i) $t = 3 \text{ s}$ (ii) $\mathbf{r} = 10\mathbf{j} + 3(3\mathbf{i} - 2\mathbf{j}) = (9\mathbf{i} + 4\mathbf{j}) \text{ m}$ OR $\mathbf{r} = 4\mathbf{i} - 2\mathbf{j} + 3\left(\frac{5}{3}\mathbf{i} + 2\mathbf{j}\right) = (9\mathbf{i} + 4\mathbf{j}) \text{ m}$	M1 A1 A1 DM1 A1 A1 (6)	Find the position vector of B or G at time t Correct for B Correct for G Compare coefficients of $\mathbf{i}$ or of $\mathbf{j}$ to form an equation in t . Correct unambiguous conclusion. Final answer. Accept with no units. Do not ignore subsequent working.
		[11]	