

Question Number	Scheme	Marks
6.	$s_A = 35t + \frac{1}{2} 0.4 t^2; s_B = 44t + \frac{1}{2} 0.5 t^2$ $44t + \frac{1}{2} 0.5 t^2 = 200 + 35t + \frac{1}{2} 0.4 t^2$ $\frac{1}{20} t^2 + 9t - 200 = 0$ $(t - 20)(t + 200) = 0$ $t = 20$ $v = 44 + \frac{1}{2} \cdot 20 = 54 \text{ ms}^{-1}$	M1 A1 A1 M1 A1 M1 A1 DM1 A1 9
	Notes	
	First M1 for use of $s = ut + \frac{1}{2} at^2$ for either A or B First A1 for a correct equation for A Second A1 for a correct equation for B Second M1 for producing a quadratic in t only from their $s_A =$ their $s_B \pm 200$ Third A1 for a correct '3 term = 0' equation Third M1 (can be implied by one correct answer) for attempt to solve their quadratic (M0 if linear). Must include 200, must be 3 terms and must have come from using both distance expressions. Fourth A1 for $t = 20$ Fourth M1 dependent on third M1 for correctly using their t value to find v Fifth A1 for 54 N.B. SC for trial and error to find t ; can score max M1A1A1M1A0M0A0M1A1 6/9	

QUESTION NUMBER	SCHEME	MARKS
3(a)	A to B : $s = \left(\frac{u+v}{2} \right) t \quad : \quad 400 = \left(\frac{u+28}{2} \right) 20$ Other possible equations: $28 = u + 20a$ $400 = 20u + \frac{1}{2} a \times 20^2$ $28^2 = u^2 + 2 \times 400a$ $400 = (28 \times 20) - \frac{1}{2} a \times 20^2$	M1
	$u = 12^*$	A1* cso
		(2)
3(b)	A to B : Any of the above equations with $u = 12$ e.g. $v = u + at$ $28 = 12 + 20a$ (leads to $a = 0.8$)	M1 A1
	A to midpoint: $200 = 12t + \frac{1}{2} 0.8t^2$ OR: find v and use it to find t e.g. $v^2 = 12^2 + (2 \times 0.8 \times 200) \Rightarrow v = \sqrt{464}$ and then one of : $\sqrt{464} = 12 + 0.8t$ $200 = \left(\frac{12 + \sqrt{464}}{2} \right) t$ $200 = \sqrt{464}t - \frac{1}{2} \times 0.8t^2$	M1 A1
	$t = 12$ (s) or better (11.9258..), $5\sqrt{29} - 15$	A1
		(5)
3(c)	$D - 260 = 1200(0.8)$	M1A1ft
	$D = 1220$ (N)	A1
		(3)
		(10)
	Notes for question 3	
(a) M1 A1*	Complete method to find the value of u. (they may use two equations, eliminate a and solve for u) Correctly reaches the given answer. N.B. If they use 2 equations, we need to see a eliminated and u found correctly for this A mark. N.B. No marks if they use $u = 12$ in (b) to find a and then use it in (a) to show that $u = 12$.	

7 (a)		M1 A1 (2)
(b)	$108 \times 1000 / 3600 = 30 \text{ m s}^{-1}$ 	B1 shape DB1 ft figs (2)
(c)	$12000 = \frac{1}{2} \times 30(480 + 480 - 4T)$ $T = 40$ $a = 30/40 = 0.75 \text{ m s}^{-2}$	M1 A2 A1 M1 A1 (6) 10
NOTES Question 7(a) M1 for $108 \times 1000 / 3600$ oe A1 for 30 Question 7(b) First B1 for trapezium (B0 for triangle), from the origin, finishing on the t-axis. Second dependent B1 ft on their '30' and 480 or 108 and (8/60 oe). Question 7(c) First M1 for clear attempt at equating <i>total</i> area under a trapezium to distance travelled oe (equation must include at least one '1/2') to give equation in ONE unknown. A2 for a correct equation, -1 each error. N.B. Repeated use of an incorrect v from part (a) is ONE error. Third A1 for $T = 40$ (or 120) N.B. (First M1 only for $\frac{1}{2}(480 + x).30 = 12000$ First A1 for $480 - x = 160$; Second A1 if they divide 160 in ratio 1:3) (First M0 if they use s = the full distance in any single <i>suvat</i> equation) Second M1 (independent) for a complete method to find a. Fourth A1 for 0.75		

Question Number	Scheme	Marks	Notes
6(a)	$v_1 = 8 \times 1.5 (= 12)$ $v_2 = 12 + 0.8 \times 20$ $v_2 = 28 \text{ m s}^{-1}$	M1 M1 A1 (3)	Use of $v = u + at$ or equivalent for $t = 8$ Follow their 12
(b)		B1 B1ft (2) M1 A1ft A1ft A1 (4)	shape nos: 8,28; 12,28 indicated. Follow their 12, 28 Correct method for distance for the triangle (0-8) or the trapezium (8-28) Follow their 12 Follow their 12, 28 Correct answer only (cao)
(c)	first 8 s: $\text{dist} = \frac{1}{2} \times 8 \times 12 (= 48)$ next 20 s: $\text{dist} = \frac{1}{2} \times (12 + 28) \times 20 (= 400)$ Total dist = 448 m	M1 A1ft A1ft A1 (4)	Find area of right hand triangle or an expression in T for the trapezium (rectangle + triangle). Follow their 28 Form an equation in T for their 16, 448 and 140
(d)	$0 = 28^2 - 2 \times 2.8s$ $s = \frac{28^2}{2 \times 2.8} (= 140)$ $448 + 140 + 28T = 2000$ $T = \frac{2000 - 448 - 140}{28} = 50.4$	M1 A1ft DM1 A1 (4)	Or better (50.42857...) Accept 50.
		[13]	

Question Number	Scheme	Marks	Notes
1.	$(2\mathbf{i} + 3a\mathbf{j}) + (2a\mathbf{i} + b\mathbf{j}) + (b\mathbf{i} + 4\mathbf{j}) = \mathbf{0}$	M1	Use of resultant force = 0 (Seen or implied)
	$2a + b + 2 = 0; 3a + b + 4 = 0$	M1	In an equation involving all three forces once and once only, compare $\mathbf{i}$ or $\mathbf{j}$ components to form an equation in a and b . Allow with $\mathbf{i}$ or $\mathbf{j}$. $\lambda\mathbf{i} = \mu\mathbf{j}$ is M0
		A1	Two correct scalar equations. No $\mathbf{i}/\mathbf{j}$
	$a = -2; b = 2$	DM1	Solve simultaneous equations to find a or b . Dependent on the previous M1
		A1	a correct
		A1	b correct
		6	
2(a)	$2mu - km3u = -2m\frac{1}{2}u + kmv$	M1	Conservation of momentum. Must have all four terms but condone sign errors and consistent omission of m or g included in all terms
	$(3u = kv + 3ku)$	A2,1,0	-1 for each error. All correct A1A1, one error A1A0, two or more errors A0A0
	$v = (1-k)\frac{3u}{k}$ or $k = \frac{3u}{v+3u}$	A1	Correct expression for v or for kv or for k
	$v > 0 \Rightarrow$	M1	Correct inequality for their v
	$\Rightarrow k < 1$ *	A1	Reach given answer correctly
		(6)	
(b)	$I = 2m(\frac{1}{2}u - -u)$	M1	Impulse = <u>change</u> in momentum for A or for B . Condone sign errors.
		A1	Correct unsimplified expression in terms of m and u . Allow +/-
	$= 3mu$	A1	Correct answer only.
		(3)	
		9	

Question Number	Scheme	Marks
8(a)	$\mathbf{v}_B = (40 \cos 60)\mathbf{i} + (-40 \sin 60)\mathbf{j}$ $= 20\mathbf{i} - 20\sqrt{3}\mathbf{j}$	M1A1 A1 (3)
8(b)	$\mathbf{r} = 60\mathbf{i} + t(-20\mathbf{i})$ $\mathbf{s} = t(20\mathbf{i} - 20\sqrt{3}\mathbf{j})$	M1 A1 B1ft (3)
8(c)	$\overline{AB} = \mathbf{s} - \mathbf{r} = t(20\mathbf{i} - 20\sqrt{3}\mathbf{j}) - [60\mathbf{i} + t(-20\mathbf{i})]$ $\sqrt{(40t - 60)^2 + (-20t\sqrt{3})^2} = 60$ OR $(40t - 60)^2 + (-20t\sqrt{3})^2 = 60^2$ $2800t^2 - 4800t = 0$ $t = \frac{12}{7}$	M1 M1 A2ft M1 A1 A1
	13 43 OR 1 43 pm (nearest minute)	A1 cso (8)
		(14)
	Notes for qu 8	
	For (a) and (b) allow working in column vector form	
8(a)	M1 for 40 resolved in both components but allow sin/cos confusion and sign errors First A1 for two correct unsimplified components Second A1 for a correct vector, allow 2SF or better for the $\mathbf{j}$ component N.B. Need to see a complete velocity vector not just $p = , q =$	
8(b)	M1 for $\mathbf{r} = 60\mathbf{i} \pm 20\mathbf{i}$ A1 for $\mathbf{r} = 60\mathbf{i} + t(-20\mathbf{i})$ B1 ft on their answer for (a)	
8(c)	M1 for finding either $\mathbf{s} - \mathbf{r}$ or $\mathbf{r} - \mathbf{s}$. Allow missing brackets if they recover. Second M1 for obtaining an equation in t only by using the magnitude of their $\mathbf{s} - \mathbf{r}$ or $\mathbf{r} - \mathbf{s}$ and equating it to 60 (allow the square on both sides). Must be a clear attempt to use Pythagoras First and Second A1 ft for a correct equation, ft on their $\mathbf{s} - \mathbf{r}$ or $\mathbf{r} - \mathbf{s}$ Third M1 for a simplified quadratic equation $= 0$ with at least a t^2 and a t term Third A1 for a correct equation from correct working (N.B. Coefficient of t^2 must be in range $[2797, 2825]$) Fourth A1 for a correct value of t (allow AWRT 1.7) from correct working Fifth A1 for a correct time to the nearest minute cso	
	SC: If using $+20\sqrt{3}$ oe for the coefficient of $\mathbf{j}$ in part (a), can score for (c) max M1M1A2 M1A1A1A0	

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6(a)	$\frac{(20\mathbf{i} + 34\mathbf{j}) - (15\mathbf{i} + 36\mathbf{j})}{0.5}$ oe	M1
	$(10\mathbf{i} - 4\mathbf{j})^*$	A1*
		(2)
6(b)	$(15\mathbf{i} + 36\mathbf{j}) + t(10\mathbf{i} - 4\mathbf{j})$	M1 A1
		(2)
6(c)(i)	Verify using $t = 1.5$ in p or q $\mathbf{p} = (15\mathbf{i} + 36\mathbf{j}) + 1.5(10\mathbf{i} - 4\mathbf{j}) = 30\mathbf{i} + 30\mathbf{j}$ $\mathbf{q} = (42 - 8 \times 1.5)\mathbf{i} + (9 + 14 \times 1.5)\mathbf{j} = 30\mathbf{i} + 30\mathbf{j}$	M1 A1 A1
(ii)	$30\mathbf{i} + 30\mathbf{j}$	A1 (B1)
	N.B. The A mark for (ii) is now to be treated as a B mark.	
		(4)
ALT1 (i)	Find t by equating i or j components of p and q Equate i 's $15 + 10t = 42 - 8t \rightarrow t = 1.5$ j 's $36 - 4t = 9 + 14t \rightarrow t = 1.5$	M1 A1 A1
(ii)	$30\mathbf{i} + 30\mathbf{j}$	A1 (B1)
ALT2 (i)	Uses ratio: $\frac{15 + 10t}{36 - 4t} = \frac{42 - 8t}{9 + 14t}$ $\rightarrow t = 1.5$ or -8.5 verifies that components are both 30 at $t = 1.5$	M1 A1 A1
(ii)	$30\mathbf{i} + 30\mathbf{j}$	A1 (B1)
		(4)
6(d)	Position of P at 14:30 is $40\mathbf{i} + 26\mathbf{j}$	B1
	Position of Q when $t = 0.5$ $\mathbf{q} = (42 - 8 \times 0.5)\mathbf{i} + (9 + 14 \times 0.5)\mathbf{j}$ $(= (38\mathbf{i} + 16\mathbf{j}))$	M1
	$15\mathbf{j}$ seen or implied	B1
	New position of Q at time 14:30 $\mathbf{q} = (38\mathbf{i} + 16\mathbf{j}) + 2(15\mathbf{j})$ N.B. M0 if 2.5 is used.	M1
	$\mathbf{q} = 38\mathbf{i} + 46\mathbf{j}$	A1
	$ PQ = \sqrt{(40 - 38)^2 + (26 - 46)^2}$	dM1
	$= \sqrt{404}$ or $2\sqrt{101}$ (km)	A1
		(7)
		(15)