

Question Number	Scheme	Marks	
7(a)	<p style="text-align: center;">$x = -6$</p>	Correct shape and position	B1
		Correct equation of vertical asymptote. E.g. $x = -6$ or e.g. $x + 6 = 0$	B1
		Correct y intercept $\left(0, \frac{1}{6}\right)$	B1
		(3)	

(b)(i)	$mx - 4 = \frac{1}{x+6} \Rightarrow (mx - 4)(x + 6) = 1$	M1
	$\Rightarrow mx^2 + (6m - 4)x - 25 = 0$ or $mx^2 + 6mx - 4x - 25 = 0$	A1
	" $b^2 - 4ac$ " = $(6m - 4)^2 - 4 \times m \times (-25)$	dM1
	$\Rightarrow (6m - 4)^2 + 100m \dots 0$ $\Rightarrow 36m^2 + 52m + 16 \dots 0 \Rightarrow 9m^2 + 13m + 4 \dots 0 *$	A1*
(ii)	$(m + 1)(9m + 4) \dots 0 \Rightarrow m = -1, m = -\frac{4}{9}$	M1 A1
		(6)

(b)		B1B1B1
		(3)
		Total 6

3(a)		B1B1B1
		(3)

Question Number	Scheme	Marks
6.(a)	$f'(x) = 5x^{\frac{3}{2}} - 40$	M1A1
	Attempts $5x^{\frac{3}{2}} - 40 = 0 \Rightarrow x^{\frac{3}{2}} = \dots$ $x = 4$	M1 A1 cao (4)
(b)	$f''(x) = \frac{15}{2}x^{\frac{1}{2}} = 5$	M1
	$\Rightarrow x^{\frac{1}{2}} = \dots \Rightarrow x = \dots^2$ $x = \frac{4}{9}$	M1 A1 (3) (7 marks)

Question	Scheme	Marks
4(a)	$x^2 + kx - 9 = -3x^2 - 5x + k \Rightarrow 4x^2 + kx + 5x - 9 - k (= 0)$	M1
	$b^2 - 4ac = 0 \Rightarrow (k+5)^2 - 4 \times 4(-9-k) = 0$	M1
	$k^2 + 26k + 169 = 0^*$	A1* (3)
(b)	$k^2 + 26k + 169 = 0 \Rightarrow k = -13$	B1
	$k = -13 \Rightarrow 4x^2 - 8x + 4 = 0 \Rightarrow x = \dots$	M1
	$(1, -21)$	A1 (3)
		Total 6

Question Number	Scheme	Marks
11(a)	States or implies that the gradient of the normal is $-\frac{1}{3}$	M1
	Correct equation of normal e.g. $y - 16 = -\frac{1}{3}(x - 4)$	A1 (2)
(b)	$f''(x) = 4x + x^{-\frac{1}{2}} \Rightarrow f'(x) = 2x^2 + 2x^{\frac{1}{2}} + c$	M1
	$x = 4, f'(x) = 3 \Rightarrow 3 = 32 + 4 + c \Rightarrow c = \dots(-33)$	dM1
	$f'(x) = 2x^2 + 2x^{\frac{1}{2}} - 33$	A1
	$f'(x) = 2x^2 + 2x^{\frac{1}{2}} - 33 \Rightarrow f(x) = \frac{2}{3}x^3 + \frac{4}{3}x^{\frac{3}{2}} - 33x + d$	dM1
	$x = 4, f(x) = 16 \Rightarrow (f(x)) = \frac{2}{3}x^3 + \frac{4}{3}x^{\frac{3}{2}} - 33x + \frac{284}{3}$	ddM1A1 (6)
		(8 marks)

Question	Scheme	Marks	
9(a)	$m = \frac{7-2}{15-4} \left(= \frac{5}{11} \right)$	M1	
	$y-2 = \frac{5}{11}(x-4)$ or $y-7 = \frac{5}{11}(x-15)$ or $y = \frac{5}{11}x + c \Rightarrow 2 = \frac{5}{11} \times 4 + c \Rightarrow c = \dots \left(\frac{2}{11} \right)$	M1	
	$5x - 11y + 2 = 0$	A1	
		(3)	
(a) ALT	$y = mx + c \Rightarrow \begin{cases} 2 = 4m + c \\ 7 = 15m + c \end{cases}$	M1	
	$\begin{cases} 2 = 4m + c \\ 7 = 15m + c \end{cases} \Rightarrow m = \dots \left(\frac{5}{11} \right), c = \dots \left(\frac{2}{11} \right)$	M1	
	$5x - 11y + 2 = 0$	A1	
(b)	$(15-x)^2 + (7-2)^2 = (5\sqrt{5})^2$ or e.g. $\sqrt{(15-x)^2 + (7-2)^2} = 5\sqrt{5}$ or e.g. $(5\sqrt{5})^2 = 5^2 + CD^2$ oe		M1
	Way 1: $(15-x)^2 + 25 = 125 \Rightarrow (15-x)^2 = 100 \Rightarrow x = \dots$ or e.g. Way 2: $125 = 25 + CD^2 \Rightarrow CD^2 = 100 \Rightarrow CD = 10 \Rightarrow x = \dots$		M1
	(5, 2) or (25, 2)		A1
	(5, 2) and (25, 2)		A1
			(4)
	(c)	Area = $\frac{1}{2} ("5"-4) \times 5$	M1
$= \frac{5}{2}$		A1	
		(2)	
		Total 9	

Question	Scheme	Marks	
7(a)	$0 = 10 - 2x \Rightarrow x = 5$ or $y = 2, y = 10 - 2x \Rightarrow x = 4$	B1	
	<p>Examples:</p> $\frac{1}{2} \times 2(5 + 4 - a) = \frac{27}{4}$ or $\frac{1}{2} \times 2 \left(5 + 4 - \frac{2}{k} \right) = \frac{27}{4}$ <p>Trapezium or</p> $\frac{1}{2} \times 2a + \frac{1}{2} \times 2(5 - a + 4 - a) = \frac{27}{4}$ or $\frac{1}{2} \times 2 \times \frac{2}{k} + \frac{1}{2} \times 2 \left(5 - \frac{2}{k} + 4 - \frac{2}{k} \right) = \frac{27}{4}$ <p>Triangle + Trapezium or</p> $\frac{1}{2} \times 2a + 2(4 - a) + \frac{1}{2} \times 1 \times 2 = \frac{27}{4}$ or $\frac{1}{2} \times 2 \times \frac{2}{k} + 2 \left(4 - \frac{2}{k} \right) + \frac{1}{2} \times 1 \times 2 = \frac{27}{4}$ <p>Triangle + Rectangle + Triangle or</p> $\frac{1}{2} \times 5 \times 2 + \frac{1}{2} (4 - a) \times 2 = \frac{27}{4}$ or $\frac{1}{2} \times 5 \times 2 + \frac{1}{2} \left(4 - \frac{2}{k} \right) \times 2 = \frac{27}{4}$ <p>2 Triangles</p> $\Rightarrow k = \frac{8}{9}, a = \frac{9}{4}$	M1	
			A1 A1ft
			(4)
			(2)
(6 marks)			
(b)	Two of $y \geq \frac{8}{9}x, y \leq 10 - 2x, x > \frac{9}{4}$	M1	
	All three of $y \geq \frac{8}{9}x, y \leq 10 - 2x, x > \frac{9}{4}$	A1	
		(2)	

Question Number	Scheme	Marks
2a	$\frac{1}{8}x$	B1
		(1)
b	$\frac{1}{256}x^{\frac{3}{2}}$	B1
		(1)
c	$\left(\frac{1}{2} \left(\frac{1}{64}x^2 \times \frac{16}{\sqrt{x}} \right) \right)^{\frac{4}{3}} = \left(\frac{1}{8}x^{\frac{3}{2}} \right)^{\frac{4}{3}} = 16x^{-2}$	M1A1
		(2)
(4 marks)		

Question Number	Scheme	Marks
1.(a)	$\frac{dy}{dx} = \frac{1}{8} \times 3x^2 - 24 \times -\frac{1}{2} x^{-\frac{3}{2}}$ $\frac{dy}{dx} = \frac{3}{8} x^2 + 12x^{-\frac{3}{2}}$	M1 A1 A1 (3)
1.(b)	$\left. \frac{dy}{dx} \right _{x=4} = \frac{3}{8} \times 4^2 + 12 \times 4^{-\frac{3}{2}} = (7.5)$ $y + 3 = 7.5(x - 4) \Rightarrow y = 7.5x - 33$	M1 M1 A1 (3) (6 marks)