

Question	Scheme	Marks
2(a)	$AB = 21 \text{ cm}, BC = 13 \text{ cm}, \angle BAC = 25^\circ, \angle ACB = x^\circ$	
	$\frac{\sin x^\circ}{21} = \frac{\sin 25^\circ}{13}$ o.e	M1
	$\sin x^\circ = 0.6827$ (awrt)	A1
		(2)
(b)	$\sin^{-1}(0.6827) = \dots (43.05^\circ)$	M1
	$(AC < AB \text{ so } \angle ABC < \angle ACB \text{ so) required angle is } 180^\circ - \sin^{-1}(0.6827) = \dots$	M1
	So $x =$ awrt 136.95	A1
		(3)
		(5 marks)
Notes:		
Condone the omission of the $^\circ$ symbol. Mark (a) and (b) as one		

Question Number	Scheme	Marks
2. (a)	$5(x+3) > 4(2x-5) \Rightarrow 5x+15 > 8x-20 \Rightarrow ax > b \text{ or } px < q$	M1
	$\Rightarrow x < \frac{35}{3}$	A1
		(2)
(b) (i)	$x^2 - 6x + 1 = (x-3)^2 \pm \dots = (x-3)^2 - 8$	M1, A1
	(ii) $(x-3)^2 - 8 = 0 \Rightarrow x = 3 + \sqrt{8} \text{ or } 3 - \sqrt{8}$	M1
(c)	$x^2 - 6x + 1 \geq 0 \Rightarrow x \leq 3 - \sqrt{8}, x \geq 3 + \sqrt{8}$	A1
	$x \leq 3 - \sqrt{8}, 3 + \sqrt{8} \leq x < \frac{35}{3}$	B1
		(1)
		(7 marks)

Question Number	Scheme	Marks
2 (a)	$3^{3x} = (3^x)^3 = y^3$	B1
(b)	$\frac{1}{3^{x-2}} = \frac{1}{3^x \times 3^{-2}} = \frac{9}{y}$	M1 A1
		(2)
(c)	$\frac{81}{9^{2-3x}} = \frac{9^2}{9^{2-3x}} = 9^{2-(2-3x)} = 9^{3x} = 3^{6x} = y^6$	M1 A1
		(2)
		(5 marks)

Question Number	Scheme	Marks
1.	$\int (2x-5)(3x+2)(2x+5) dx$ $(2x-5)(3x+2)(2x+5) = (6x^2 - 11x - 10)(2x+5) = \dots$ $= 12x^3 + 8x^2 - 75x - 50$ $\int (2x-5)(3x+2)(2x+5) dx = 3x^4 + \frac{8}{3}x^3 - \frac{75}{2}x^2 - 50x + c$	M1 A1 M1, A1ft, A1 (5 marks)

Question Number	Scheme	Marks
4(i)	<p>Uses a correct law of indices on 2^{4k-3} or 8^{1-k}</p> <p>The possibilities are endless but some more common examples are:</p> <p>For 2^{4k-3}: $2^{4k} \times 2^{-3}$, $\frac{2^{4k}}{8}$, $8^{\frac{4k-3}{3}}$, $4^{\frac{4k-3}{2}}$, $(\sqrt{2})^{8k-6}$</p> <p>For 8^{1-k}: 8×8^{-k}, $\frac{8}{8^k}$, $2^{3(1-k)}$, $4^{\frac{2(1-k)}{3}}$, $(\sqrt{2})^{6-6k}$</p> <p>These may be seen in isolation e.g. not in an equation. But not just e.g. $8 = 2^3$</p>	M1
	<p>e.g.</p> $2^{4k-3} = \frac{8^{1-k}}{4\sqrt{2}} \Rightarrow 2^{4k-3} = \frac{2^{3(1-k)}}{2^{\frac{5}{2}}} \Rightarrow 2^{4k-3} = 2^{3(1-k)-\frac{5}{2}}$ $\Rightarrow 4k-3 = 3(1-k) - \frac{5}{2} \Rightarrow k = \dots$	dM1
	$k = \frac{1}{2}$	A1
		(3)

(ii)	$\frac{x\sqrt{3}+2}{\sqrt{3}-1} = x\sqrt{3}-4 \Rightarrow x\sqrt{3}+2 = (x\sqrt{3}-4)(\sqrt{3}-1)$ $\Rightarrow x\sqrt{3}+2 = 3x+4-4\sqrt{3}-x\sqrt{3}$ $\Rightarrow 2\sqrt{3}x-3x = 2-4\sqrt{3}$	M1
	$\Rightarrow x(2\sqrt{3}-3) = 2-4\sqrt{3}$	A1
	$\Rightarrow x = \frac{2-4\sqrt{3}}{2\sqrt{3}-3} \times \frac{2\sqrt{3}+3}{2\sqrt{3}+3}$	dM1
	$= -6 - \frac{8}{3}\sqrt{3}$	A1
		(4)

Question Number	Scheme	Marks
4	$\int \frac{3x^{\frac{3}{2}} - 15x^{\frac{1}{2}} + 2x - 10}{4\sqrt{x}} dx = \int \frac{3}{4}x - \frac{15}{4} + \frac{1}{2}x^{\frac{1}{2}} - \frac{5}{2}x^{-\frac{1}{2}} dx$ $x^n \rightarrow x^{n+1}$ $\frac{3}{8}x^2 - \frac{15}{4}x + \frac{1}{3}x^{\frac{3}{2}} - 5x^{\frac{1}{2}} + C$	M1A1A1 dM1 A1A1
		(6 marks)

Question Number	Scheme	Marks
8 (a) (i)	$x = 4, f'(x) = 10, f'(x) = 3\sqrt{x} + kx^2 \Rightarrow 10 = 3\sqrt{4} + 4^2k \Rightarrow k = \dots$ $10 = 3 \times 2 + k \times 16 \Rightarrow k = \frac{1}{4} *$	M1 A1*
(ii)	$x = 4, y = 12$ on $y = 10x + c \Rightarrow 12 = 10 \times 4 + c$ $\Rightarrow c = -28$	M1 A1 (4)
(b)	$f''(x) = \frac{3}{2}x^{-\frac{1}{2}} + \frac{1}{2}x$ $\{\Rightarrow f''(4)\} = \frac{11}{4}$	M1 A1ft A1 (3)
(c)	$f(x) = 2x^{\frac{3}{2}} + \frac{1}{12}x^3 + d$ Uses $P(4, 12) \Rightarrow 12 = 2 \times 8 + \frac{1}{12} \times 4^3 + d \Rightarrow d = \dots$ $\{f(x)\} = 2x^{\frac{3}{2}} + \frac{1}{12}x^3 - \frac{28}{3}$	M1, A1ft dM1 A1 (4)
		(11 marks)

Question Number	Scheme	Marks
5.(a)	$\frac{dy}{dx} = \frac{1}{2}x^2 + 2x^{-\frac{1}{2}}$	M1A1 A1 (3)
(b)	$\left. \frac{dy}{dx} \right _{x=4} = \frac{1}{2} \times 4^2 + 2 \times \frac{1}{\sqrt{4}} = (9)$ Gradient of normal is $-\frac{1}{9}$ $y - \frac{11}{3} = -\frac{1}{9}(x - 4) \Rightarrow x + 9y - 37 = 0$	M1 dM1 M1 A1 (4)
		(7 marks)

Question	Scheme	Marks
1	$4x^2 - 3x + 7 \geq 4x + 9$ $\Rightarrow 4x^2 - 7x - 2 \dots 0 \Rightarrow (4x+1)(x-2) \dots 0 \Rightarrow x = \dots$ <p style="text-align: center;">or</p> $\Rightarrow 4x^2 - 7x - 2 \dots 0 \Rightarrow x = \frac{-(-7) \pm \sqrt{(-7)^2 - 4(4)(-2)}}{2 \times 4} \Rightarrow x = \dots$ <p style="text-align: center;">or</p> $\Rightarrow 4x^2 - 7x - 2 \dots 0 \Rightarrow 4 \left(x^2 - \frac{7}{4}x - \frac{1}{2} \right) \dots 0 \Rightarrow 4 \left(\left(x - \frac{7}{8} \right)^2 - \left(\frac{7}{8} \right)^2 - \frac{1}{2} \right) \dots 0 \Rightarrow x = \dots$	M1
	$x = -\frac{1}{4}, 2$	A1
	$x \leq -\frac{1}{4}, x \geq 2$	M1
	$x \leq -\frac{1}{4} \text{ or } x \geq 2 \text{ oe}$	A1
		(4)
(4 marks)		

Question Number	Scheme	Marks
10	$(k-1)x^6 + 4x^3 + (k-4) = 0$	
(a)	$3.5x^6 + 4x^3 + 0.5 = 0 \Rightarrow 7x^6 + 8x^3 + 1 = 0$ $\Rightarrow (x^3 + 1)(7x^3 + 1) = 0$ $\Rightarrow x^3 = -1, x^3 = -\frac{1}{7}$ $\Rightarrow x = -1, x = -\sqrt[3]{\frac{1}{7}}$	M1 A1 A1 (3)
(b)	<p>Attempts $b^2 - 4ac = 16 - 4(k-1)(k-4)$ $= 20k - 4k^2$</p> <p>Solves $b^2 - 4ac < 0 \Rightarrow 4k(5-k) < 0 \Rightarrow k < 0, k > 5$</p>	M1 A1 dM1 A1 (4) (7 marks)

Question	Scheme	Marks
4(i)		Correct shape, translated down. B1
		Correct horizontal asymptote labelled B1
		Correct maximum and minimum points labelled B1
		(3)
(ii)		Correct shape, reflected in y axis B1
		Correct horizontal asymptote labelled B1
		Correct maximum and minimum points labelled. B1
		(3)
		(6 marks)

Notes:

Question Number	Scheme	Marks
5(a)	$f'(x) = 12x^{-\frac{1}{2}} + \frac{x}{3} - 4$	
	One of $x^{-\frac{1}{2}} \rightarrow x^{\frac{1}{2}}$, $-4 \rightarrow -4x$, $x \rightarrow x^2$	M1
	$f(x) = \int 12x^{-\frac{1}{2}} + \frac{x}{3} - 4 \, dx = 24x^{\frac{1}{2}} + \frac{x^2}{6} - 4x + c$	A1A1
	$8 = 24(9)^{\frac{1}{2}} + \frac{(9)^2}{6} - 4(9) + c \Rightarrow c = \dots$	dM1
	$(f(x)) = 24x^{\frac{1}{2}} + \frac{x^2}{6} - 4x - \frac{83}{2}$	A1
		(5)
(b)	$f'(9) = \frac{12}{\sqrt{9}} + \frac{9}{3} - 4 \quad (= 3)$	M1
	$3 \rightarrow -\frac{1}{3}$	dM1
	$y - 8 = -\frac{1}{3}(0 - 9)$	M1
	$(0, 11)$	A1
		(4)
		(9 marks)

