

Question Number	Scheme	Marks
10 (a)	$P = \left(-\frac{1}{2}, 0\right)$	B1 (1)
(b)	$f(x) = (x-4)(2x+1)^2 \Rightarrow f(x) = ax^3 + bx^2 + cx + d$ $= 4x^3 - 12x^2 - 15x - 4$ oe $f'(x) = 12x^2 - 24x - 15$	M1 A1 dM1 A1 (4)
(c)	Attempts $f'(2.5) = 12 \times 2.5^2 - 24 \times 2.5 - 15 = 0$ Finds y coordinate for $x = 2.5$ $y = -54$	M1A1 A1 (3)
(d)	$a = -\frac{1}{2}, (+) 4$	B1, B1 (2) (10 marks)

Question Number	Scheme	Marks
3(i)	$\sqrt{8} = 2\sqrt{2}$ seen anywhere in the solution (see notes)	B1
	$(x + \sqrt{2})^2 + (3x - 5\sqrt{8})^2$ $= x^2 + 2x\sqrt{2} + 2 + 9x^2 - 30x\sqrt{8} + 25 \times 8$	M1
	$= 10x^2 - 58x\sqrt{2} + 202$	A1
		(3)
(ii)	$\sqrt{3}(4y - 3\sqrt{3}) = 5y + \sqrt{3}$ $\Rightarrow 4\sqrt{3}y - 9 = 5y + \sqrt{3}$ $\Rightarrow 4\sqrt{3}y - 5y = 9 + \sqrt{3}$	M1
	$\Rightarrow y = \dots \text{ or } \Rightarrow ky = \dots$ eg $y = \frac{9 + \sqrt{3}}{4\sqrt{3} - 5}$ " or "23" $y = \frac{9 + \sqrt{3}}{4\sqrt{3} - 5}$ "	dM1
	$y = \frac{9 + \sqrt{3}}{4\sqrt{3} - 5} \times \frac{4\sqrt{3} + 5}{4\sqrt{3} + 5} \Rightarrow y = \frac{\dots}{\text{"23"}}$	ddM1
	$y = \frac{57}{23} + \frac{41}{23}\sqrt{3} \text{ (or } y = 2\frac{11}{23} + 1\frac{18}{23}\sqrt{3})$	A1
		(4)
	(ii) Alternative 1:	
	$\sqrt{3}(4p + 4q\sqrt{3} - 3\sqrt{3}) = 5(p + q\sqrt{3}) + \sqrt{3}$ $\Rightarrow 4p\sqrt{3} + 12q - 9 = 5p + 5q\sqrt{3} + \sqrt{3}$ $\Rightarrow 4p = 5q + 1, 12q - 9 = 5p$	M1 dM1
	$\Rightarrow 4p = 5q + 1, 12q - 9 = 5p$ $\Rightarrow p = \dots, q = \dots$	ddM1
	$y = \frac{57}{23} + \frac{41}{23}\sqrt{3} \text{ (or } y = 2\frac{11}{23} + 1\frac{18}{23}\sqrt{3})$	A1
		Total 7

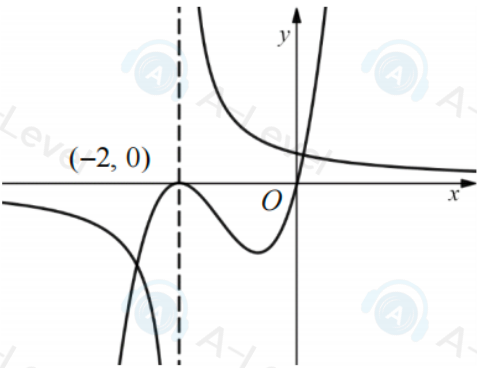
Question Number	Scheme	Marks
1.	$\int \frac{2}{3}x^3 - \frac{1}{2x^3} + 5 \, dx = \frac{2}{3} \times \frac{x^4}{4} - \frac{1}{2} \times \frac{x^{-2}}{-2} + 5x + c$	M1 A1
	$= \frac{1}{6}x^4 + \frac{1}{4}x^{-2} + 5x + c$	A1 A1 (4 marks)

Question Number	Scheme	Marks
1.	$\int \left(\frac{1}{2}x^3 + \frac{3}{\sqrt{x}} - 4 \right) dx = \frac{1}{2} \times \frac{x^4}{4} + 3 \times \frac{x^{\frac{1}{2}}}{\frac{1}{2}} - 4x + c$ $= \frac{1}{8}x^4 + 6x^{\frac{1}{2}} - 4x + c$	M1, A1 A1, A1 (4 marks)

Question	Scheme	Marks
10(a)	$f'(4) = 6(4) - \frac{7 \times 14}{4} = -\frac{1}{2}$	B1
	$m_T = -\frac{1}{2} \Rightarrow m_N = \frac{-1}{-\frac{1}{2}}$	M1
	$y - 12 = 2(x - 4)$ or $y = mx + c \Rightarrow y = 2x + c \Rightarrow 12 = 2(4) + c \Rightarrow c = \dots$	M1 (A1 on ePen)
	$y = 2x + 4$	A1
		(4)
(b)	$\dots \frac{(2x-1)(3x+2)}{2\sqrt{x}} = \dots \frac{6x^2 + x - 2}{2\sqrt{x}} = \dots 3x^{\frac{3}{2}} + \frac{1}{2}x^{\frac{1}{2}} - x^{-\frac{1}{2}}$	M1
	$f(x) = \frac{6x^2}{2} - \frac{6}{5}x^{\frac{5}{2}} - \frac{1}{3}x^{\frac{3}{2}} + 2x^{\frac{1}{2}} (+c)$ or e.g. $f(x) = \frac{6x^2}{2} - \frac{3}{\frac{5}{2}}x^{\frac{5}{2}} - \frac{1/2}{\frac{3}{2}}x^{\frac{3}{2}} + \frac{x^{\frac{1}{2}}}{\frac{1}{2}} (+c)$ or e.g. $f(x) = \frac{6x^2}{2} - \left(\frac{3}{\frac{5}{2}}x^{\frac{5}{2}} + \frac{1/2}{\frac{3}{2}}x^{\frac{3}{2}} - \frac{x^{\frac{1}{2}}}{\frac{1}{2}} \right) (+c)$	M1A1A1
	$12 = \frac{6(4)^2}{2} - \frac{6}{5}(4)^{\frac{5}{2}} - \frac{1}{3}(4)^{\frac{3}{2}} + 2(4)^{\frac{1}{2}} + c \Rightarrow c = \dots$	M1
	$(f(x) =) 3x^2 - \frac{6}{5}x^{\frac{5}{2}} - \frac{1}{3}x^{\frac{3}{2}} + 2x^{\frac{1}{2}} + \frac{16}{15}$	A1
		(6)
		Total 10

Question	Scheme	Marks
2(i)(a)	$2^{n+3} = 2^n \times 2^3 = 8m$	B1
		(1)
(b)	$16^{3n} = (2^4)^{3n}$	M1
	$= 2^{12n} = (2^n)^{12} = m^{12}$	A1
		(2)

(ii)	$x\sqrt{3} - 3 = x + \sqrt{3} \Rightarrow x\sqrt{3} - x = 3 + \sqrt{3} \Rightarrow x(\sqrt{3} - 1) = 3 + \sqrt{3} \Rightarrow x = \dots$	M1
	$= \frac{3 + \sqrt{3}}{\sqrt{3} - 1} \times \frac{\pm(\sqrt{3} + 1)}{\pm(\sqrt{3} + 1)}$	M1
	$= \frac{\pm(4\sqrt{3} + 6)}{\pm(3 - 1)} = 3 + 2\sqrt{3}$	A1
		(3)

Question Number	Scheme	Marks
4a	$x = -2$	B1
		(1)
b	$x^3 + 4x^2 + 4x = x(x+2)^2$	M1A1
		(2)
c		B1B1B1
		(3)
d	2 as the graphs intersect (each other) twice (since $(x+2)(x^3 + 4x^2 + 4x) = 1$ is the same as $x^3 + 4x^2 + 4x = \frac{1}{x+2}$)	B1
		(1)
		(7 marks)