

7.

In this question you must show all stages of your working.
Solutions relying entirely on calculator technology are not acceptable.

(a) Sketch the curve C with equation

$$y = \frac{1}{x + 6}$$

State on your sketch

- the equation of the vertical asymptote
- the coordinates of the point of intersection of C with the y -axis

(3)

The straight line l has equation $y = mx - 4$, where m is a constant.

Given that l cuts C at least once,

(b) (i) show that

$$9m^2 + 13m + 4 \geq 0$$

(ii) find the range of values of m .

(6)

DO NOT WRITE IN THIS AREA

DO NOT

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

3.

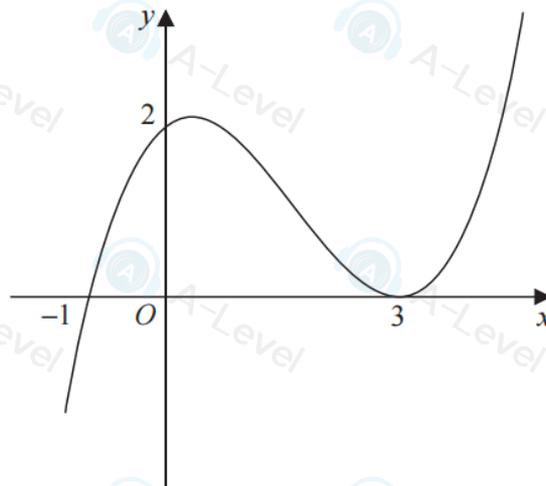


Figure 1

Figure 1 shows a sketch of the curve with equation $y = f(x)$.

The curve passes through the points $(-1, 0)$ and $(0, 2)$ and touches the x -axis at the point $(3, 0)$.

On separate diagrams, sketch the curve with equation

(a) $y = f(x + 3)$

(3)

(b) $y = f(-3x)$

(3)

On each diagram, show clearly the coordinates of all the points where the curve cuts or touches the coordinate axes.

6. (Solutions based entirely on graphical or numerical methods are not acceptable.)

Given

$$f(x) = 2x^{\frac{5}{2}} - 40x + 8 \quad x > 0$$

(a) solve the equation $f'(x) = 0$

(4)

(b) solve the equation $f''(x) = 5$

(3)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

4. The curve C_1 has equation

$$y = x^2 + kx - 9$$

and the curve C_2 has equation

$$y = -3x^2 - 5x + k$$

where k is a constant.

Given that C_1 and C_2 meet at a single point P

(a) show that

$$k^2 + 26k + 169 = 0$$

(3)

(b) Hence find the coordinates of P

(3)

DO NOT WRITE IN THIS AREA

10.

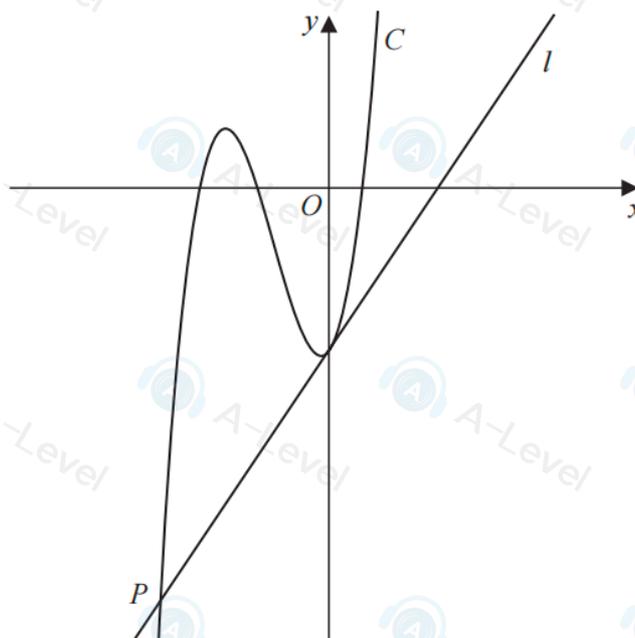


Figure 4

Figure 4 shows a sketch of part of the curve C with equation $y = f(x)$, where

$$f(x) = (3x + 20)(x + 6)(2x - 3)$$

(a) Use the given information to state the values of x for which

$$f(x) > 0$$

(2)

(b) Expand $(3x + 20)(x + 6)(2x - 3)$, writing your answer as a polynomial in simplest form.

(3)

The straight line l is the tangent to C at the point where C cuts the y -axis.

Given that l cuts C at the point P , as shown in Figure 4,

(c) find, using algebra, the x coordinate of P

(Solutions based on calculator technology are not acceptable.)

(5)

9. Given that

- the point A has coordinates $(4, 2)$
 - the point B has coordinates $(15, 7)$
 - the line l_1 passes through A and B
- (a) find an equation for l_1 , giving your answer in the form $px + qy + r = 0$ where p, q and r are integers to be found.

(3)

The line l_2 passes through A and is parallel to the x -axis.

The point C lies on l_2 so that the length of BC is $5\sqrt{5}$.

- (b) Find both possible pairs of coordinates of the point C .

(4)

- (c) Hence find the minimum possible area of triangle ABC .

(2)

7.

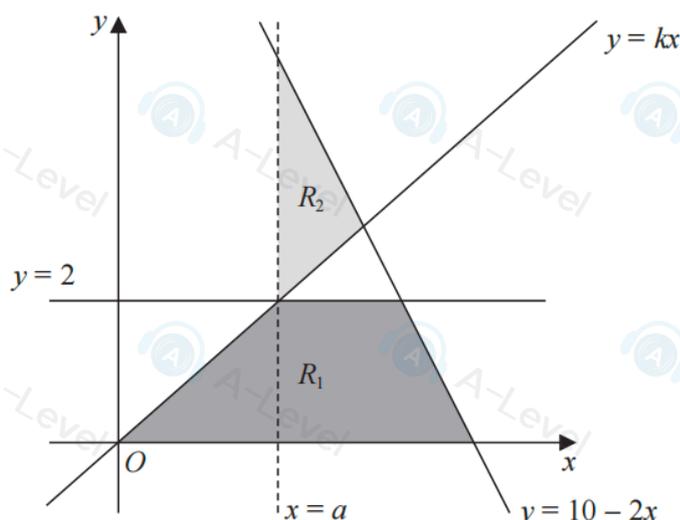


Figure 2

The region R_1 , shown shaded in Figure 2, is defined by the inequalities

$$0 \leq y \leq 2 \quad y \leq 10 - 2x \quad y \leq kx$$

where k is a constant.

The line $x = a$, where a is a constant, passes through the intersection of the lines $y = 2$ and $y = kx$

Given that the area of R_1 is $\frac{27}{4}$ square units,

(a) find

(i) the value of a

(ii) the value of k

(4)

(b) Define the region R_2 , also shown shaded in Figure 2, using inequalities.

(2)

2. Given that

$$a = \frac{1}{64}x^2 \quad b = \frac{16}{\sqrt{x}}$$

express each of the following in the form kx^n where k and n are simplified constants.

(a) $a^{\frac{1}{2}}$

(1)

(b) $\frac{16}{b^3}$

(1)

(c) $\left(\frac{ab}{2}\right)^{-\frac{4}{3}}$

(2)

Answer all questions. Write your answers in the spaces provided.

1. The curve C has equation $y = \frac{1}{8}x^3 - \frac{24}{\sqrt{x}} + 1$

(a) Find $\frac{dy}{dx}$, giving the answer in its simplest form.

(3)

The point $P(4, -3)$ lies on C .

(b) Find the equation of the tangent to C at the point P . Write your answer in the form $y = mx + c$, where m and c are constants to be found.

(3)