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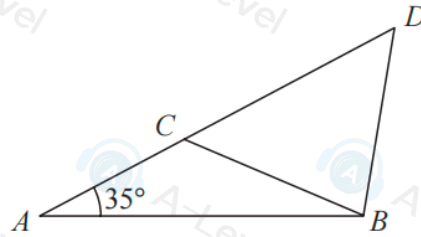


Figure 3

Not to scale

Figure 3 shows the design for a structure used to support a roof.

The structure consists of four wooden beams,  $AB$ ,  $BD$ ,  $BC$  and  $AD$ .

Given  $AB = 6.5$  m,  $BC = BD = 4.7$  m and angle  $BAC = 35^\circ$

(a) find, to one decimal place, the size of angle  $ACB$ ,

(3)

(b) find, to the nearest metre, the total length of wood required to make this structure.

(3)

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4. The curve  $C$  has equation

$$y = \frac{2}{x} + 3x - 4 \quad x \neq 0$$

The straight line  $l$  has equation

$$y = kx + 2$$

where  $k$  is a constant.

(a) Show that  $l$  meets  $C$  when

$$(k - 3)x^2 + 6x - 2 = 0$$

(2)

(b) Hence find the value of  $k$  for which  $l$  is a tangent to  $C$

(3)

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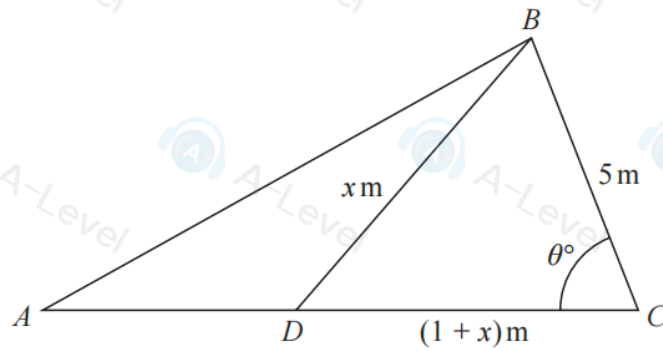


Diagram NOT  
accurately drawn

Figure 2

Figure 2 shows the plan view of a frame for a flat roof.

The shape of the frame consists of triangle  $ABD$  joined to triangle  $BCD$ .

Given that

- $BD = x$  m
- $CD = (1 + x)$  m
- $BC = 5$  m
- angle  $BCD = \theta^\circ$

(a) show that  $\cos \theta^\circ = \frac{13 + x}{5 + 5x}$

(2)

Given also that

- $x = 2\sqrt{3}$
- angle  $BAC = 30^\circ$
- $ADC$  is a straight line

(b) find the area of triangle  $ABC$ , giving your answer, in  $\text{m}^2$ , to one decimal place.

(5)

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DC

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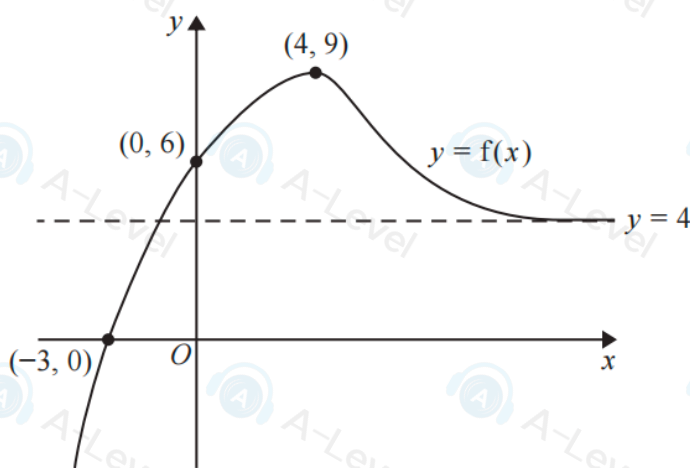


Figure 4

The curve  $C$  with equation  $y = f(x)$  is shown in Figure 4.

The curve  $C$

- has a single turning point, a maximum at  $(4, 9)$
- crosses the coordinate axes at only two places,  $(-3, 0)$  and  $(0, 6)$
- has a single asymptote with equation  $y = 4$

as shown in Figure 4.

(a) State the equation of the asymptote to the curve with equation  $y = f(-x)$ . (1)

(b) State the coordinates of the turning point on the curve with equation  $y = f\left(\frac{1}{4}x\right)$ . (1)

Given that the line with equation  $y = k$ , where  $k$  is a constant, intersects  $C$  at exactly one point,

(c) state the possible values for  $k$ . (2)

The curve  $C$  is transformed to a new curve that passes through the origin.

- (d) (i) Given that the new curve has equation  $y = f(x) - a$ , state the value of the constant  $a$ . (2)
- (ii) Write down an equation for another single transformation of  $C$  that also passes through the origin. (2)



1.

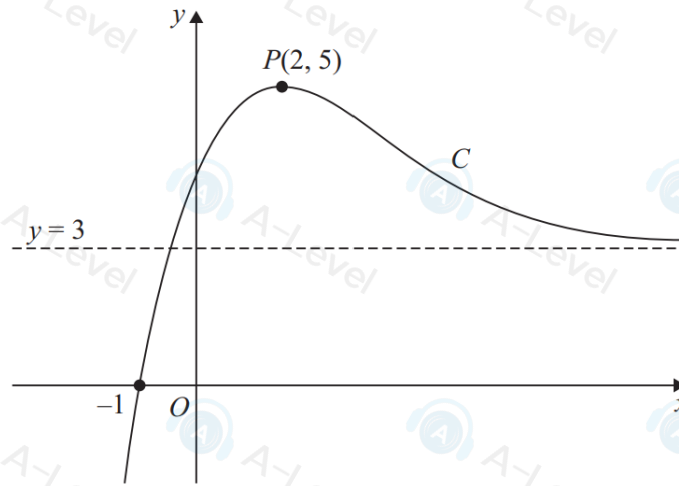


Figure 1

The curve  $C$ , shown in Figure 1,

- has equation  $y = f(x)$ ,  $x \in \mathbb{R}$
- cuts the  $x$ -axis at  $-1$
- has a maximum turning point at  $P(2, 5)$
- has a horizontal asymptote with equation  $y = 3$

The curve  $C$  has no other turning points or asymptotes.

- (a) Find the coordinates of the point to which  $P$  is transformed when the curve with equation  $y = f(x)$  is transformed to the curve with equation
- (i)  $y = f(x) + 7$
  - (ii)  $y = 3f(x)$
- (2)

Given that the line with equation  $y = k$ , where  $k$  is a constant, cuts or meets  $C$  exactly once,

- (b) state the range of possible values of  $k$ . (2)
- (c) Write down the solution of the equation

$$f(x + 4) = 0$$

(1)

6.

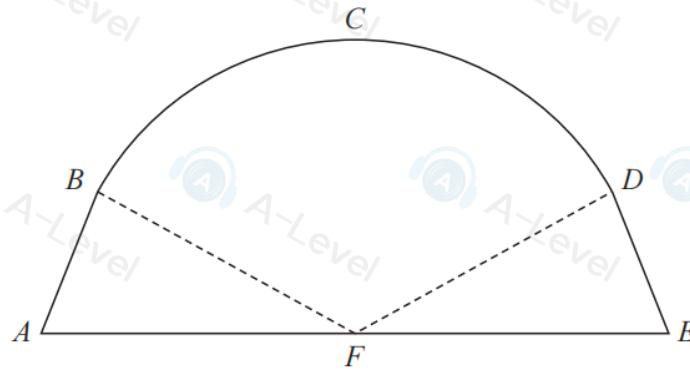
Diagram not  
drawn to scale**Figure 1**

Figure 1 shows a sketch of the entrance to a tunnel.

The shape of the entrance consists of a sector  $BCDF$ , of a circle centre  $F$ , joined to two congruent (identical) triangles  $ABF$  and  $EDF$ .

Given that

$AFE$  is a straight line

$$AF = FE = 6.4 \text{ m}$$

$$FB = FD = 6.2 \text{ m}$$

$$\text{angle } BFD = 2.275 \text{ radians}$$

- (a) Show that angle  $AFB = 0.433$  radians to 3 decimal places. (1)
- (b) Find the perimeter of the entrance to the tunnel,  $ABCDEF$ , in metres, to one decimal place. (4)
- (c) Find the cross-sectional area of the entrance to the tunnel,  $ABCDEF$ , in  $\text{m}^2$ , to one decimal place. (4)

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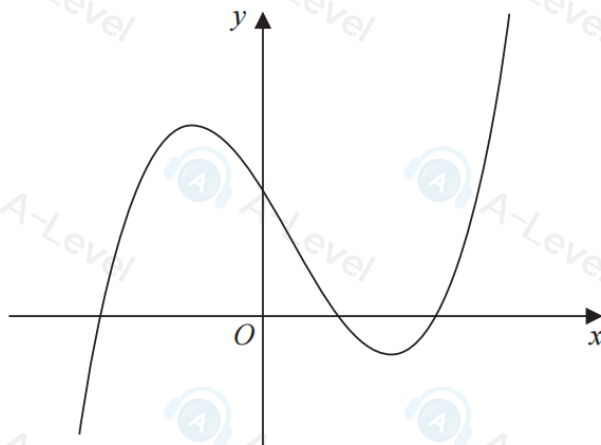


Figure 3

Figure 3 shows a sketch of part of the curve with equation  $y = f(x)$ , where

$$f(x) = (x + 4)(x - 2)(2x - 9)$$

Given that the curve with equation  $y = f(x) - p$  passes through the point with coordinates  $(0, 50)$

(a) find the value of the constant  $p$ .

(2)

Given that the curve with equation  $y = f(x + q)$  passes through the origin,

(b) write down the possible values of the constant  $q$ .

(2)

(c) Find  $f'(x)$ .

(4)

(d) Hence find the range of values of  $x$  for which the gradient of the curve with equation  $y = f(x)$  is less than  $-18$

(3)

4.

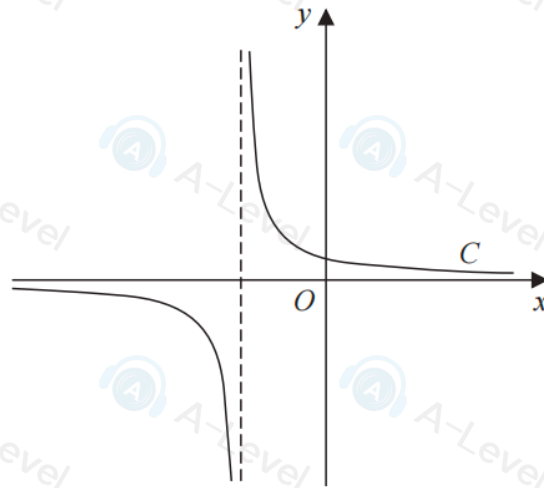


Figure 1

Figure 1 shows a sketch of part of the curve  $C$  with equation  $y = \frac{1}{x+2}$

(a) State the equation of the asymptote of  $C$  that is parallel to the  $y$ -axis.

(1)

(b) Factorise fully  $x^3 + 4x^2 + 4x$

(2)

A copy of Figure 1, labelled Diagram 1, is shown on the next page.

(c) On Diagram 1, add a sketch of the curve with equation

$$y = x^3 + 4x^2 + 4x$$

On your sketch, state clearly the coordinates of each point where this curve cuts or meets the coordinate axes.

(3)

(d) Hence state the number of real solutions of the equation

$$(x+2)(x^3 + 4x^2 + 4x) = 1$$

giving a reason for your answer.

(1)

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8.

In this question you must show all stages of your working.

Solutions relying on calculator technology are not acceptable.

The curve  $C_1$  has equation

$$xy = \frac{15}{2} - 5x \quad x \neq 0$$

The curve  $C_2$  has equation

$$y = x^3 - \frac{7}{2}x - 5$$

(a) Show that  $C_1$  and  $C_2$  meet when

$$2x^4 - 7x^2 - 15 = 0 \quad (2)$$

Given that  $C_1$  and  $C_2$  meet at points  $P$  and  $Q$

(b) find, using algebra, the exact distance  $PQ$

(5)

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6.

In this question you must show all stages of your working.

Solutions relying on calculator technology are not acceptable.

The equation

$$4(p - 2x) = \frac{12 + 15p}{x + p} \quad x \neq -p$$

where  $p$  is a constant, has two distinct real roots.

(a) Show that

$$3p^2 - 10p - 8 > 0 \quad (3)$$

(b) Hence, using algebra, find the range of possible values of  $p$

(3)

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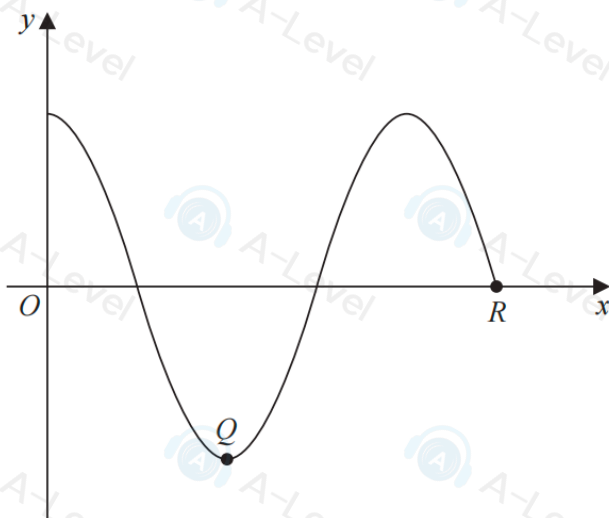


Figure 2

Figure 2 shows a sketch of the curve with equation  $y = f(x)$ , where

$$f(x) = \cos 2x^\circ \quad 0 \leq x \leq k$$

The point  $Q$  and the point  $R(k, 0)$  lie on the curve and are shown in Figure 2.

(a) State

- (i) the coordinates of  $Q$ ,
- (ii) the value of  $k$ .

(3)

(b) Given that there are exactly two solutions to the equation

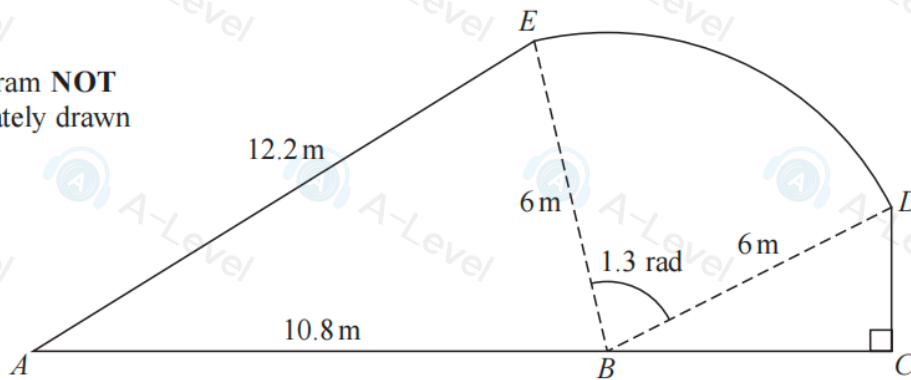
$$\cos 2x^\circ = p \quad \text{in the region } 0 \leq x \leq k$$

find the range of possible values for  $p$ .

(2)

5.

Diagram **NOT**  
accurately drawn



**Figure 2**

Figure 2 shows the plan view of a garden.

The shape of the garden  $ABCDEA$  consists of a triangle  $ABE$  and a right-angled triangle  $BCD$  joined to a sector  $BDE$  of a circle with radius 6 m and centre  $B$ .

The points  $A$ ,  $B$  and  $C$  lie on a straight line with  $AB = 10.8$  m

Angle  $BCD = \frac{\pi}{2}$  radians, angle  $EBD = 1.3$  radians and  $AE = 12.2$  m

- (a) Find the area of the sector  $BDE$ , giving your answer in  $\text{m}^2$  (2)
- (b) Find the size of angle  $ABE$ , giving your answer in radians to 2 decimal places. (2)
- (c) Find the area of the garden, giving your answer in  $\text{m}^2$  to 3 significant figures. (3)

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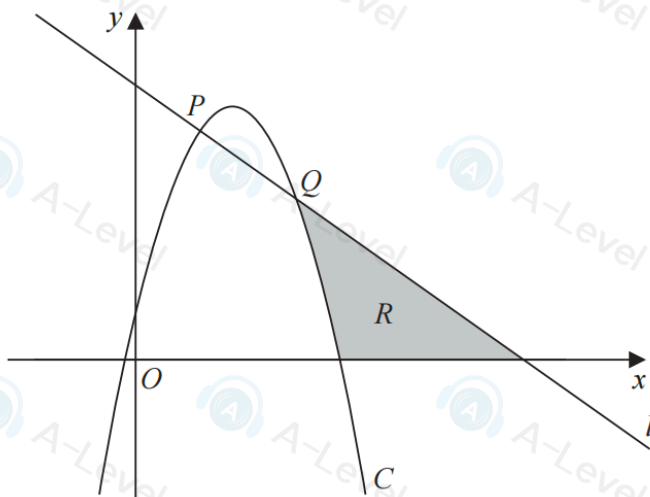


Figure 1

In this question you must show all stages of your working.

Solutions relying on calculator technology are not acceptable.

Figure 1 shows a line  $l$  with equation  $x + y = 6$  and a curve  $C$  with equation  $y = 6x - 2x^2 + 1$

The line  $l$  intersects the curve  $C$  at the points  $P$  and  $Q$  as shown in Figure 1.

- (a) Find, using algebra, the coordinates of  $P$  and the coordinates of  $Q$ . (4)

The region  $R$ , shown shaded in Figure 1, is bounded by  $C$ ,  $l$  and the  $x$ -axis.

- (b) Use inequalities to define the region  $R$ . (3)