

Question Number	Scheme	Marks
3(a)(i)	$a_1 = \frac{1}{4}$	B1
(ii)	$a_2 = \frac{1}{4}$	B1
(iii)	$a_3 = 1$	B1
		(3)
(b)	$\frac{50}{2}[2+49] (=1275) \text{ oe}$	M1A1
	$\sum_{n=1}^{50} \cos^2\left(\frac{n\pi}{3}\right) = 34 \times \frac{1}{4} + 16 \times 1$	M1
	$1275 + \frac{49}{2} = \frac{2599}{2}$	A1
		(4)
		(7 marks)

Question Number	Scheme	Marks
8(i)	Provides a counter example E.g. $\sqrt{2} \times \sqrt{8} = 4$	B1
(ii)	Knows that odd numbers are of the form $2k+1$, ($k \in \mathbb{N}$)	B1
	Attempts $(2k+1)^3 + 3(2k+1) + 2 = \dots$	M1
	$= 8k^3 + 12k^2 + 12k + 6$	A1
	$= 4 \times (2k^3 + 3k^2 + 3k + 1) + 2$	A1*
	Which is even but not a multiple of 4. Hence proven	
		(4)
		(5 marks)

Question Number	Scheme	Marks
6(a)	Sets $f\left(-\frac{3}{2}\right) = 0 \Rightarrow (9p+4q=102)$	M1
	Sets $f(-2) = -5 \Rightarrow (4p+q=43)$	M1
	Solves to get values for p and q	dM1
	(i) $p=10$ * (ii) $q=3$ following two correct equations	A1*, A1
		(5)
(b)	$f'(x) = 12x^2 + 20x + 8$	B1
	Solves $f'(x) = 0 \Rightarrow 4(3x+2)(x+1) = 0 \Rightarrow x = -\frac{2}{3}, -1$	M1, A1
	$-1 < x < -\frac{2}{3}$	A1
		(4)
		Total 9

Question Number	Scheme	Marks
10 (a)	$\left(\frac{dy}{dx} = \right) x - 2187x^{-\frac{5}{2}}$	M1, A1
	Sets $x - 2187x^{-\frac{5}{2}} = 0 \Rightarrow x^{\frac{7}{2}} = 2187$ (or e.g. $x = (\sqrt[7]{2187})^2 \Rightarrow x = 9$ *)	dM1A1*
		(4)
(b)	e.g. $\int \left\{ \frac{1}{2}x^2 + 1458x^{-\frac{3}{2}} - 74 \right\} dx = \frac{1}{6}x^3 - 2916x^{-\frac{1}{2}} - 74x$ or $\int \left\{ \frac{1}{2}x^2 + 1458x^{-\frac{3}{2}} - "94.5" \right\} dx = \frac{1}{6}x^3 - 2916x^{-\frac{1}{2}} - 94.5x$	M1A1ft
	y value at P is 20.5	B1
	e.g. Area R = $\left[\frac{1}{6}x^3 - 2916x^{-\frac{1}{2}} - 74x \right]_4^9 - (9-4) \times "20.5"$ $= \left(\frac{1}{6} \times 9^3 - 2916 \times 9^{-\frac{1}{2}} - 74 \times 9 \right) - \left(\frac{1}{6} \times 4^3 - 2916 \times 4^{-\frac{1}{2}} - 74 \times 4 \right) - (9-4) \times "20.5"$	dM1
	$\left(-1516\frac{1}{2} + 1743\frac{1}{3} - 102\frac{1}{2} \right) = 124\frac{1}{3}$	A1
		(5)
	Total 9	

Question Number	Scheme	Marks	
5(i)	$4 \tan \theta + 5 \sin \theta = 0$ States or uses $\tan \theta = \frac{\sin \theta}{\cos \theta} \rightarrow 4 \frac{\sin \theta}{\cos \theta} + 5 \sin \theta = 0$ $\sin \theta (4 + 5 \cos \theta) = 0$ $\cos \theta = -\frac{4}{5}$ $\cos \theta = -\frac{4}{5} \Rightarrow \theta = \text{awrt } 143^\circ \text{ or awrt } 217^\circ$ $\cos \theta = -\frac{4}{5} \Rightarrow \theta = \text{awrt } 143.1^\circ \text{ and awrt } 216.9^\circ$ $\sin \theta = 0 \Rightarrow \theta = 180^\circ, 360^\circ$	M1 dM1 A1 A1 B1	
		(5)	
	(ii)	$\frac{\sin x}{\cos x} + \frac{\cos x}{\sin x} = \frac{5}{\cos x} \xrightarrow{\times \sin x \cos x} \sin^2 x + \cos^2 x = 5 \sin x$ $5 \sin x = 1$ $x = \text{awrt } 0.201, 2.94$	M1, A1 dM1, A1
			(4)
			(9 marks)

Question	Answer	Marks	Guidance
5	Use product rule to differentiate $4e^{2x}y$	M1	
	Obtain correct $8e^{2x}y + 4e^{2x} \frac{dy}{dx}$	A1	
	Obtain $\left[8e^{2x}y + 4e^{2x} \frac{dy}{dx} \right] + 2y \frac{dy}{dx} = 0$	B1	
	Substitute $x=0$ and $y=-7$ to find value of $\frac{dy}{dx}$	M1	dependent at least one term involving $\frac{dy}{dx}$ from implicit differentiation.
	Obtain $-\frac{28}{5}$	A1	OE
		5	

Question	Answer	Marks	Guidance
1	State or imply that $\cos\theta = \frac{1}{3}\sqrt{5}$	B1	or exact equivalent.
	Substitute appropriate values into $\sin\theta\cos 60^\circ + \cos\theta\sin 60^\circ$	M1	
	Obtain $\frac{1}{3} + \frac{1}{6}\sqrt{15}$	A1	or exact equivalent.
		3	

Question Number	Scheme	Marks
1(a)	$h = 1.25$	B1
	$A \approx \frac{1}{2} \times 1.25 \{ 3.479 + 5.182 + 2(6.101 + 7.448 + 6.823) \}$	M1
	$= 30.9$	A1
		(3)
(b)	$\int_{0.5}^{5.5} (f(x) + 4x) dx = 30.9 + [2x^2]_{0.5}^{5.5} = 30.9 + 2 \times 5.5^2 - 2 \times 0.5^2$	M1
	or $\int_{0.5}^{5.5} (f(x) + 4x) dx = \int_{0.5}^{5.5} f(x) dx + \frac{1}{2}(4 \times 0.5 + 4 \times 5.5) \times 5 = \dots$	
	$= 30.9 + 60 = 90.9$	A1ft
		(2)
		Total 5

Question Number	Scheme	Marks
2.(a)	E.g. $64 \times \left(-\frac{1}{2}\right)^3 = -8 \checkmark *$	M1, A1* (2)
(b)	Finds the value of a . E.g. $64 \div \left(-\frac{1}{2}\right)^2 = 256$	M1, A1
	Uses $S_{\infty} = \frac{a}{1-r} = \frac{256}{1-\left(-\frac{1}{2}\right)} = \frac{512}{3}$	M1, A1 (4) (6 marks)

Question Number	Scheme	Marks
8. (a)	$-5 < x < \frac{2}{3}$	M1, A1 (2)
(b)	$(2x-7)$	B1 (1)
(c)	$f'(x) = 2(3x-2)(x+5) = 6x^2 + 26x - 20$ $f(x) = 2x^3 + 13x^2 - 20x + c$ $x = \frac{7}{2}, y/f(x) = 0 \Rightarrow c = (-175)$ $f(x) = 2x^3 + 13x^2 - 20x - 175 = (2x-7)(x^2 + 10x + 25)$ $= (2x-7)(x+5)^2$	M1, A1 dM1, A1 ddM1 A1 (6) (9 marks)

Question Number	Scheme	Marks
1(a)	$f(-1) = (-1)^4 + a(-1)^3 - 3(-1)^2 + b(-1) + 5 = 4$	M1
	$1 - a - 3 - b + 5 = 4 \Rightarrow a + b = -1 *$	A1*
		(2)
(b)	$f(2) = (2)^4 + a(2)^3 - 3(2)^2 + b(2) + 5 = -23$	M1
	$\Rightarrow 8a + 2b = -32$ oe (eg $4a + b = -16$)	A1
	$b = -1 - a \Rightarrow 4a - 1 - a = -16 \Rightarrow a = \dots$	dM1
	$a = -5, b = 4$	A1
		(4) (6 marks)

Question Number	Scheme	Marks
3 (a)	States $h = 3$, or use of $\frac{1}{2} \times 3$	B1
	$\left\{ 8.485 + 1.100 + 2(2.502 + 1.524) \right\}$ $= \frac{1}{2} \times 3 \times \{ 17.637 \} = \text{awrt } 26.46$	M1 A1 (3)
(b)	Either adds 9 or halves their answer from part (a) Full attempt using a correct method Estimate = $9 + 13.23 = \text{awrt } 22.2$	M1 dM1A1ft (3)
		(6 marks)

Question Number	Scheme	Marks
4 (a)	$(3+2x)^6$ First term 3^6 or 729 Term in x , x^2 or x^3 : Award for one of ${}^6C_5(3)^5(2x)^1$, ${}^6C_4(3)^4(2x)^2$ or ${}^6C_3(3)^3(2x)^3$ Two of $\dots + 2916x + 4860x^2 + 4320x^3 + \dots$ $(3+2x)^6 = 729 + 2916x + 4860x^2 + 4320x^3 + \dots$	B1 M1 A1 A1 (4)
	(b) Attempts one correct term $2x^2 \times "729"$ or $\pm \frac{1}{6x} \times "4320" x^3$ Attempts to combine the correct two terms $2x^2 \times "729" \pm \frac{1}{6x} \times "4320" x^3 = \dots x^2$ 738 but condone $738x^2$	M1 dM1 A1 (3)
		Total 7