

Question Number	Scheme	Marks
8(a)	$a_2 = 2p^2 - 7$	B1
		(1)
(b)	$a_3 = 2(2p^2 - 7 + 3)^2 - 7$	M1
	$p - 3 + 2p^2 - 7 + 8p^4 - 32p^2 + 25 = p + 15$ $\Rightarrow 8p^4 - 30p^2 = 0$	M1 A1
	Correct values of $p^2 = 0$ and $\frac{15}{4}$ (may be implied by $p = 0$ and $\pm\sqrt{\frac{15}{4}}$)	A1
	Uses their values of p to find a_2 using a correct method	dM1
	Possible values for a_2 are -7 and $\frac{1}{2}$	A1
		(6)
Alt (b)	$\sum_{n=1}^3 a_n = p + 15 \Rightarrow p - 3 + a_2 + 2(a_2 + 3)^2 - 7 = p + 15$	M1
	$\Rightarrow a_2 + 2(a_2 + 3)^2 - 25 = 0$ $\Rightarrow 2a_2^2 + 13a_2 - 7 = 0$	M1A1 A1
	$\Rightarrow (2a_2 - 1)(a_2 + 7) = 0 \Rightarrow a_2 = \dots$	dM1
	Possible values for a_2 are -7 and $\frac{1}{2}$	A1
		(6)
		(7 marks)

Question	Answer	Marks	Guidance
7(a)	Attempt use of quotient rule (or equivalent) to find $\frac{dx}{dt}$	M1*	
	Obtain $\frac{1}{(t+2)^2}$	A1	or (unsimplified) equivalent.
	Equate $\frac{dy}{dx}$ to 1	DM1	Must be using <i>their</i> $\frac{dy}{dx}$.
	Obtain $(2t+a)(t+2)^2 = 1$ and expand to confirm given result	A1	AG necessary detail required.
		4	
7(b)	Substitute $t = -1$, equate to zero and attempt solution for a	M1	Allow a complete method using algebraic long division or synthetic division.
	Obtain $a = 3$	A1	
		2	
7(c)	Divide their cubic by $t+1$ at least as far as the x term	M1	or equivalent (inspection, identity, ...).
	Obtain $2t^2 + 9t + 11$	A1	
	Calculate discriminant, obtain -7 and conclude no further value of t	A1	OE
		3	

Question Number	Scheme	Marks
2.	$\left(2 - \frac{x}{2}\right)^6 = 2^6 + \binom{6}{1} 2^5 \cdot \left(-\frac{x}{2}\right) + \binom{6}{2} 2^4 \cdot \left(-\frac{x}{2}\right)^2 + \dots$ $= 64 - 96x + 60x^2 + \dots$	M1 B1A1A1 (4)
		(4 marks)

Question Number	Scheme	Marks
1 (a)	Attempts $u_3 = 3u_2 - 2u_1 \Rightarrow 4 = 3u_2 - 2 \times 7 \Rightarrow u_2 = \dots$ $\Rightarrow u_2 = 6$	M1 A1
		(2)
(b)	Attempts $u_4 = 3u_3 - 2u_2 = 3 \times 4 - 2 \times "6" = (0)$ $\sum_{r=1}^4 (u_r + 2r) = (7 + 2 \times 1) + ("6" + 2 \times 2) + (4 + 2 \times 3) + ("0" + 2 \times 4)$ $= 37$	M1 dM1 A1
		(3)
		Total 5

Question Number	Scheme	Notes	Marks
8(a)	$u_{20} = 100 + 19(-2) = 62^*$	Correct method shown	B1*
			(1)
(b)	$S_{20} = \frac{1}{2}(20)\{2 \times 100 + 19(-2)\} = \dots$ or $S_{20} = \frac{1}{2}(20)\{100 + 62\} = \dots$	Applies a correct AP sum formula with $n = 20, a = 100$ and $d = -2$ or $n = 20, a = 100$ and $l = 62$	M1
	$= 1620 \text{ (mm)}$	Correct value	A1
			(2)
(c)	$62 \times r^2 = 60 \Rightarrow r^2 = \dots$	Correct strategy to find r	M1
	$r^2 = \frac{60}{62} \Rightarrow r = \sqrt{\frac{60}{62}}$ $= 0.983738\dots$	$r = \text{awrt } 0.984$	A1
			(2)
(d)	$\text{Total distance from GS hits} = \frac{62 \times 0.983\dots(1 - 0.983\dots^n)}{1 - 0.983\dots}$		M1
	$1620 + \frac{62 \times 0.983\dots(1 - 0.983\dots^n)}{1 - 0.983\dots} > 3000$	Correct equation set up with their r and suitable a	M1
	$0.983\dots^n < 0.63207\dots \Rightarrow n = \frac{\log(0.63207\dots)}{\log(0.983\dots)}$	Fully correct processing to find n from an equation of suitable form,	M1
	$n = 27.98\dots \Rightarrow N = 20 + 28 = 48$	$N = 48$ only	A1cso
			(4)
(d) Alternative taking 20th hit as first term of GP			
	$\text{Total distance from GS hits} = \frac{62(1 - 0.983\dots^n)}{1 - 0.983\dots}$		M1
	$1620 - 62 + \frac{62(1 - 0.983\dots^n)}{1 - 0.983\dots} > 3000$	Correct equation set up with their r and suitable a	M1
	$0.983\dots^n < 0.62179\dots \Rightarrow n = \frac{\log(0.62179\dots)}{\log(0.983\dots)}$	Fully correct processing to find n from an equation of suitable form,	M1
	$n = 28.98\dots \Rightarrow N = 19 + 29 = 48$	$N = 48$ only	A1cso
Total 9			

Question Number	Scheme	Marks
1(a)	$(u_2 =) k - \frac{8}{1}$ and $(u_3 =) k - \frac{8}{k-8} \left(= \frac{k^2 - 8k - 8}{k-8} \right)$ oe	M1A1 (2)
(b)	$u_3 = 6 \Rightarrow k - \frac{8}{k-8} = 6 \Rightarrow k^2 - 14k + 40 = 0$ $(k-4)(k-10) = 0 \Rightarrow k = \dots$ or $(k =) \frac{14 \pm \sqrt{14^2 - 4 \times 1 \times 40}}{2 \times 1}$ $(k =) 4, 10$	M1 dM1 A1 (3)
		(5 marks)

Question Number	Scheme	Marks
4 (a)	$(3+2x)^6$ First term 3^6 or 729 Term in x , x^2 or x^3 : Award for one of ${}^6C_5(3)^5(2x)^1$, ${}^6C_4(3)^4(2x)^2$ or ${}^6C_3(3)^3(2x)^3$ Two of $\dots + 2916x + 4860x^2 + 4320x^3 + \dots$ $(3+2x)^6 = 729 + 2916x + 4860x^2 + 4320x^3 + \dots$	B1 M1 A1 A1 (4)
(b)	Attempts one correct term $2x^2 \times "729"$ or $\pm \frac{1}{6x} \times "4320" x^3$ Attempts to combine the correct two terms $2x^2 \times "729" \pm \frac{1}{6x} \times "4320" x^3 = \dots x^2$ 738 but condone $738x^2$	M1 dM1 A1 (3)
		Total 7