

Question Number	Scheme	Marks
5 (a)	$f(x) = 3x^3 + ax^2 - 10x + b$ $f\left(\frac{4}{3}\right) = 0 \Rightarrow 3 \times \left(\frac{4}{3}\right)^3 + a\left(\frac{4}{3}\right)^2 - 10\left(\frac{4}{3}\right) + b = 0$ $\frac{64}{9} + \frac{16}{9}a - \frac{40}{3} + b = 0 \Rightarrow 64 + 16a - 120 + 9b = 0 \Rightarrow 16a + 9b = 56^*$	M1 A1* (2)
(b)	$f(2) = b \Rightarrow 3 \times (2)^3 + a(2)^2 - 10(2) + b = b \text{ leading to an equation in just } a$ $4a = -4 \Rightarrow a = -1$ Substitutes $a = -1$ in $-16 + 9b = 56 \Rightarrow b = \dots$ $\Rightarrow b = 8$	M1 A1 M1 A1 (4)
(c)	$f(x) = 3x^3 - x^2 - 10x + 8 = (3x - 4)(x^2 + x - 2)$ $= (3x - 4)(x + 2)(x - 1)$	M1, A1 A1 (3) (9 marks)

Question	Scheme	Marks
6(a)	Way 1: Eqn is $(x - 3)^2 + (y + 4)^2 - 9 - 16 + k = 0$	M1
	So radius must be 4 $\Rightarrow 25 - k = 16$	M1
	$\Rightarrow k = 9$	A1
		(3)
	Way 2: $y = 0 \Rightarrow x^2 - 6x + k = 0$ has one solution	M1
	$\Rightarrow 6^2 - 4 \times 1 \times k = 0$	M1
	$\Rightarrow k = 9$	A1
		(3)
(b)	C intersects x axis at (3,0)	B1
	Intersects y axis when $y^2 + 8y + 9 = 0 \Rightarrow y = \dots$ or $y = -4 \pm \sqrt{16 - 9}$	M1
	Or uses base of triangle is $2\sqrt{16 - 9}$	
	Area $RST = \frac{1}{2} \times 2\sqrt{7} \times 3$	M1
	$= 3\sqrt{7}$	A1
		(4)
(7 marks)		

Question Number	Scheme	Marks
3(a)	Attempts to complete the square for both variables $(x+4)^2, (y-7)^2$	M1
	Centre $(-4, 7)$	A1
	Radius = 12	A1
		(3)
(b)	Attempts $\pm \left(12 - \sqrt{4^2 + 7^2} \right)$	M1
	$12 - \sqrt{65}$	A1 ft
		(2)
		Total 5

Question	Answer	Marks	Guidance
1	Attempt to express equation in terms of $\sec \theta$ only	M1	or equivalent in terms of $\cos \theta$ only, using a correct identity, allow if '5' omitted.
	Obtain $6\sec^2 \theta - 17\sec \theta - 14 (=0)$	A1	or $14 \cos^2 \theta + 17 \cos \theta - 6 = 0$.
	Attempt solution of 3-term quadratic equation to find one value of θ , from $\cos \theta = \dots$	M1	
	Obtain 73.4	A1	or greater accuracy.
	Obtain 286.6	A1	or greater accuracy; and no others between 0 and 360.
		5	

Question Number	Scheme	Marks
9 (i)	$2 \log_3 (4x+5) - \log_3 (x+3) = 2 \Rightarrow \log_3 \frac{(4x+5)^2}{(x+3)} = 2$ $\Rightarrow \frac{(4x+5)^2}{(x+3)} = 9$ $\Rightarrow 16x^2 + 31x - 2 = 0$ $(16x-1)(x+2) = 0 \Rightarrow x = \frac{1}{16} \text{ only}$	M1, M1 A1 dM1, A1 (5)
(ii) (a)	States that $\log a + \log b = \log(ab)$ or else uses rule and proceeds from given equation $\log a + \log b = \log(a+b)$ to $\log ab = \log(a+b)$ Deduces $ab = a+b \Rightarrow ab - a = b \Rightarrow a(b-1) = b \Rightarrow a = \frac{b}{b-1}^*$	B1 M1, A1*
(b)	States either $b > 1$ or $b \neq 1$ as a would not be defined $b > 1$ as logs only exist for positive numbers	B1 B1 (5) (10 marks)

Question Number	Scheme	Marks
8 (i)	Substitutes a value e.g. $n = 6$ into $n^2 + 3n + 1$ where $n^2 + 3n + 1$ is not prime	M1
	Correct calculation for that value e.g. $n^2 + 3n + 1 = 55$ And conclusion "which is not prime"	A1
		(2)
(ii)	Attempts to find $n^2 - 2$ for either odds or evens E.g Attempts $(2p+1)^2 - 2$ or $(2p)^2 - 2$	M1
	Achieves either $(2p+1)^2 - 2 = 4p^2 + 4p - 1$ or $(2p)^2 - 2 = 4p^2 - 2$ and shows or gives a reason why the expression is not a multiple of 4 where required (see notes)	A1
	Attempts to find $n^2 - 2$ for both odds and evens (See above)	dM1
	Achieves both $(2p+1)^2 - 2 = 4p^2 + 4p - 1$ and $(2p)^2 - 2 = 4p^2 - 2$ and shows or gives reasons why these are not multiples of 4 where required (see notes) With a conclusion that they are not multiples of 4. *	A1*
		(4)
		(6 marks)

Question Number	Scheme	Marks
6(a)	$\frac{3 \sin \theta \cos \theta}{2 \sin \theta - 1} = 5 \tan \theta \Rightarrow \frac{3 \sin \theta \cos \theta}{2 \sin \theta - 1} = 5 \frac{\sin \theta}{\cos \theta}$	<u>M1</u>
	$\frac{3 \sin \theta \cos \theta}{2 \sin \theta - 1} = 5 \frac{\sin \theta}{\cos \theta} \Rightarrow 3 \sin \theta \cos^2 \theta = 5 \sin \theta (2 \sin \theta - 1)$	M1
	$3 \sin \theta \cos^2 \theta = 10 \sin^2 \theta - 5 \sin \theta \Rightarrow 3 \sin \theta (1 - \sin^2 \theta) = 10 \sin^2 \theta - 5 \sin \theta *$	M1
	$\Rightarrow 3 \sin^3 \theta + 10 \sin^2 \theta - 8 \sin \theta = 0$	A1*
		(4)
(b)	$3 \sin^3 2x + 10 \sin^2 2x - 8 \sin 2x = 0 \Rightarrow \sin 2x (3 \sin^2 2x + 10 \sin 2x - 8) = 0$ $(3 \sin 2x - 2)(\sin 2x + 4) = 0 \Rightarrow \sin 2x = \dots$	M1
	$\sin 2x = \frac{2}{3}$	A1
	$(x =) 0.365$	A1
	$x = 0$	B1
		(4)
		(8 marks)