

Question Number	Scheme	Marks
8. (a)	$-5 < x < \frac{2}{3}$	M1, A1 (2)
(b)	$(2x-7)$	B1 (1)
(c)	$f'(x) = 2(3x-2)(x+5) = 6x^2 + 26x - 20$ $f(x) = 2x^3 + 13x^2 - 20x + c$ $x = \frac{7}{2}, y/f(x) = 0 \Rightarrow c = (-175)$ $f(x) = 2x^3 + 13x^2 - 20x - 175 = (2x-7)(x^2 + 10x + 25)$ $= (2x-7)(x+5)^2$	M1, A1 dM1, A1 ddM1 A1 (6) (9 marks)

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4. (a)	$\log_3(a+1) - \log_3 a = 4 \Rightarrow \log_3\left(\frac{a+1}{a}\right) = 4$ $\Rightarrow \left(\frac{a+1}{a}\right) = 3^4$ $\Rightarrow a+1 = 81a \Rightarrow a = \frac{1}{80}$	M1 A1 dM1, A1 (4)
(b)	$\text{Area} \approx \frac{1}{2} \left\{ \log_3\left(\frac{2}{1}\right) + \log_3\left(\frac{6}{5}\right) + 2 \left(\log_3\left(\frac{3}{2}\right) + \log_3\left(\frac{4}{3}\right) + \log_3\left(\frac{5}{4}\right) \right) \right\}$ $= \frac{1}{2} \log_3 \left(\frac{2}{1} \times \frac{6}{5} \times \frac{3^2}{2^2} \times \frac{4^2}{3^2} \times \frac{5^2}{4^2} \right) = \frac{1}{2} \log_3 15 = \log_3 \sqrt{15}$	M1, A1 dM1, A1 (4)
(c)	States 'increase the number of strips'	B1 (1) (9 marks)

Question Number	Scheme	Marks
10 (a)	$\left(\frac{dy}{dx} = \right) x - 2187x^{-\frac{5}{2}}$	M1, A1
	Sets $x - 2187x^{-\frac{5}{2}} = 0 \Rightarrow x^{\frac{7}{2}} = 2187 \left(\text{or e.g. } x = (\sqrt[7]{2187})^2 \right) \Rightarrow x = 9$ *	dM1A1*
		(4)
(b)	e.g. $\int \left\{ \frac{1}{2}x^2 + 1458x^{-\frac{3}{2}} - 74 \right\} dx = \frac{1}{6}x^3 - 2916x^{-\frac{1}{2}} - 74x$ or $\int \left\{ \frac{1}{2}x^2 + 1458x^{-\frac{3}{2}} - "94.5" \right\} dx = \frac{1}{6}x^3 - 2916x^{-\frac{1}{2}} - 94.5x$	M1A1ft
	y value at P is 20.5	B1
	e.g. Area R = $\left[\frac{1}{6}x^3 - 2916x^{-\frac{1}{2}} - 74x \right]_4^9 - (9-4) \times "20.5"$ $= \left(\frac{1}{6} \times 9^3 - 2916 \times 9^{-\frac{1}{2}} - 74 \times 9 \right) - \left(\frac{1}{6} \times 4^3 - 2916 \times 4^{-\frac{1}{2}} - 74 \times 4 \right) - (9-4) \times "20.5"$	dM1
	$\left(-1516\frac{1}{2} + 1743\frac{1}{3} - 102\frac{1}{2} \right) = 124\frac{1}{3}$	A1
		(5)
		Total 9

Question Number	Scheme	Marks
9(a)	$y = \frac{9x^2(5-\sqrt{x})}{5}$	
	$y = 9x^2 - \frac{9}{5}x^{\frac{5}{2}} \Rightarrow \frac{dy}{dx} = 18x - \frac{9}{2}x^{\frac{3}{2}}$	M1, A1
	$18x - \frac{9}{2}x^{\frac{3}{2}} = 0 \Rightarrow x^{\frac{1}{2}} = (4)$	dM1
	$(16, 460.8)$	A1, A1
		(5)
(b)	$5 - \sqrt{x} = 0 \Rightarrow x = 25$	M1, A1
(c)	$\int 9x^2 - \frac{9}{5}x^{\frac{5}{2}} dx = 3x^3 - \frac{18}{35}x^{\frac{7}{2}}$	M1A1
	Shaded area = $\frac{(25-16) \times 460.8}{5} - \left[3x^3 - \frac{18}{35}x^{\frac{7}{2}} \right]_{16}^{25}$	M1, dM1
	$= 1312.7$	A1
		(5)
		(12 marks)

Question Number	Scheme	Marks
8 (i)	$\int \frac{8\sqrt{x}-5}{2x^2} dx = \int 4x^{-\frac{3}{2}} - \frac{5}{2}x^{-2} dx$ $= -8x^{-\frac{1}{2}} + \frac{5}{2}x^{-1} (+C)$ $\int_2^4 \left(4x^{-\frac{3}{2}} - \frac{5}{2}x^{-2}\right) dx = \left(-4 + \frac{5}{8}\right) - \left(-4\sqrt{2} + \frac{5}{4}\right) = 4\sqrt{2} - \frac{37}{8}$	B1 M1 A1 dM1 A1 (5)
(ii)	$\int \left(\frac{1}{2}x^2 + k\right) dx = \left[\frac{1}{6}x^3 + kx\right]$ $\int_{-3}^6 \left(\frac{1}{2}x^2 + k\right) dx = 55 \Rightarrow \left[\frac{1}{6}x^3 + kx\right]_{-3}^6 = 55 \Rightarrow (36 + 6k) - \left(-\frac{9}{2} - 3k\right) = 55 \Rightarrow k = \dots$ $k = \frac{29}{18}$	M1 A1 dM1 A1 (4) (9 marks)

Question Number	Scheme		Marks
3.(a)	OPEN TOPPED $120 = 3x^2y \Rightarrow y = \frac{40}{x^2}$ $A = 3x^2 + 8xy$ $= 3x^2 + 8x \times \frac{40}{x^2} = 3x^2 + \frac{320}{x}$	CLOSED CONTAINER $120 = 3x^2y \Rightarrow y = \frac{40}{x^2}$ $A = 6x^2 + 8xy$ $= 6x^2 + 8x \times \frac{40}{x^2} = 6x^2 + \frac{320}{x}$	M1, A1 dM1, A1 (4)
(b)	$\frac{dA}{dx} = 6x - \frac{320}{x^2}$ $\frac{dA}{dx} = 6x - \frac{320}{x^2} = 0$ $\Rightarrow x^3 = \frac{160}{3} \Rightarrow x = \text{awrt } 3.76$	$\frac{dA}{dx} = 12x - \frac{320}{x^2}$ $\frac{dA}{dx} = 12x - \frac{320}{x^2} = 0$ $\Rightarrow x^3 = \frac{80}{3} \Rightarrow x = \text{awrt } 2.99$	M1, A1ft dM1, A1 (4)
(c)	Attempts $\frac{d^2A}{dx^2} \Big _{x=3.76} = 6 + \frac{640}{x^3}$ $= 6 + \frac{640}{3.76^3} = \dots$ $\frac{d^2A}{dx^2} \Big _{x=3.76} = \text{awrt } 18 > 0 \text{ MINIMUM*}$	Attempts $\frac{d^2A}{dx^2} \Big _{x=2.99} = 12 + \frac{640}{x^3}$ $= 12 + \frac{640}{2.99^3} = \dots$ $\frac{d^2A}{dx^2} \Big _{x=2.99} = \text{awrt } 36 > 0 \text{ MINIMUM*}$	M1 A1* (2) (10 marks)