

Question Number	Scheme	Marks
8(a)	$25 = a + -(5 \times -2 + b) (\Rightarrow 25 = a + 10 - b) \Rightarrow a = 15 + b$ *	M1A1*
		(2)
(b)	$9 = a + 10 + b \Rightarrow a = \dots$ or $b = \dots$	M1
	$a = 7, b = -8$	A1A1
		(3)
(c)	$\left(\frac{8}{5}, 7\right)$	B1ftB1
		(2)
(d)	$15 - 5x = -2x^3 + 5x^2 + 4x - 3 \Rightarrow 2x^3 - 5x^2 - 9x + 18 = 0$	M1
	$2x^3 - 5x^2 - 9x + 18 = (x+2)(2x^2 - 9x + 9)$	dM1A1
	$2x^2 - 9x + 9 = 0 \Rightarrow x = \frac{3}{2}$ (ignore $x = 3$)	ddM1
	$\left(\frac{3}{2}, \frac{15}{2}\right)$	M1A1
		(6)
		(13 marks)

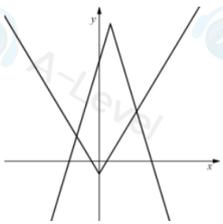
Question Number	Scheme	Marks
8 (i)	States or uses $\operatorname{cosec} \theta = \frac{1}{\sin \theta}$	B1
	Uses both $\operatorname{cosec} \theta = \frac{1}{\sin \theta}$ and $\sin 2\theta = 2 \sin \theta \cos \theta$	M1
	$3 \operatorname{cosec} \theta = 8 \cos \theta \Rightarrow \sin 2\theta = \frac{3}{4}$	A1
	$\Rightarrow \theta = \frac{1}{2} \arcsin\left(\frac{3}{4}\right) = \text{awrt } 0.424, \text{ awrt } 1.15$	M1 A1
		(5)
(ii)	$\frac{\tan 2x - \tan 70^\circ}{1 + \tan 2x \tan 70^\circ} = -\frac{3}{8} \Rightarrow \tan(2x - 70^\circ) = -\frac{3}{8}$	M1 A1
	Correct order of operations $x = \frac{\arctan\left(-\frac{3}{8}\right) + 70^\circ}{2}$	dM1
	awrt 24.7° , awrt 114.7°	A1
		(4)
		(9 marks)

Question Number	Scheme	Marks
2. (a)	$f(1) = 4 \times 1^3 + 2 \times 1^2 - 12 = -6$ AND $f(2) = 4 \times 2^3 + 2 \times 2^2 - 12 = 28$ States change of sign, continuous and hence root	M1 A1 (2)
(b)	$4x^3 + 2x^2 - 12 = 0 \Rightarrow x^2(4x+2) = 12$ $\Rightarrow x^2 = \frac{12}{4x+2} = \frac{6}{2x+1} \Rightarrow x = \sqrt{\frac{6}{2x+1}}$	M1 A1 (2)
(c) (i)	$\left(x_2 = \sqrt{\frac{6}{2+1}} = 1.4\dots\right), x_3 = 1.2519$	M1, A1
(ii)	$\alpha = 1.2934$	B1 (3)
		(7 marks)

Question Number	Scheme	Marks
1(a)	$gf(1) = g\left(\frac{2(1)}{3 \times 1 + 1}\right) = 4 - \left(\frac{2(1)}{3 \times 1 + 1}\right)^2$ $= \frac{15}{4}$ oe	M1 A1 (2)
(b)	$f(x) \dots 0$ or $f(x) < \frac{2}{3}$ $0, \dots, f(x) < \frac{2}{3}$	B1 B1 (2)

(c)	$y = \frac{2x}{3x+1} \Rightarrow 3xy + y = 2x \Rightarrow 3xy - 2x = -y \Rightarrow x(3y-2) = -y$ or $x = \frac{2y}{3y+1} \Rightarrow 3xy + x = 2y \Rightarrow 3xy - 2y = -x \Rightarrow y(3x-2) = -x$ $\Rightarrow f^{-1}(x) = \frac{x}{2-3x}$	M1 A1 (2)
(d)	$f^{-1}(x) = f(x)$ or $f^{-1}(x) = x$ or $f(x) = x$ $\frac{x}{2-3x} = \frac{2x}{3x+1}$ or $\frac{x}{2-3x} = x$ or $\frac{2x}{3x+1} = x$ $\Rightarrow x(3x+1) = 2x(2-3x)$ or $x = x(2-3x)$ or $2x = x(3x+1)$ $\Rightarrow x = \dots$ $x = 0, \frac{1}{3}$	M1 A1 (2)
		Total 8

Question Number	Scheme	Marks
8(a)(i)	$\left(\frac{b}{2}, a\right)$	B1B1
(ii)	$(0, a-b)$	B1
(iii)	$\left(\frac{b-a}{2}, 0\right)$ and $\left(\frac{a+b}{2}, 0\right)$	B1B1
		(5)

(b)		B1B1
		(2)
(c)	$-x-1=2x+a-b, x=-3 \Rightarrow 2=-6+a-b$ or $x-1=a+b-2x, x=5 \Rightarrow 5-1=a+b-10$	M1
	$-x-1=2x+a-b, x=-3 \Rightarrow 2=-6+a-b$ and $x-1=a+b-2x, x=5 \Rightarrow 5-1=a+b-10$	dM1 (A1 on ePEN)
	$a-b=8$ $a+b=14 \Rightarrow a=\dots$ or $b=\dots$	ddM1
	$a=11, b=3$	A1
		(4)
		(11 marks)

Question Number	Scheme	Marks
5(a)	$(A=)8$	B1
		(1)
(b)	$16=10+"8"e^{-Bt} \Rightarrow e^{-Bt}=\dots$ $e^{-45B}=\frac{3}{4} \Rightarrow -45B=\ln\frac{3}{4} \Rightarrow B=\dots$	M1
	$B = \text{awrt } 0.00639$	dM1
		A1
		(3)
(c)	$\frac{dT}{dt} = -"8" \times \frac{1}{45} \ln\left(\frac{4}{3}\right) \times e^{-\frac{1}{45} \ln\left(\frac{4}{3}\right) \times 2} = \dots$	M1
	$= -0.0505$	A1
		(2)
(d)	The temperature has a (lower) limit of 10°C or $5=10+"8"e^{-Bt} \Rightarrow e^{-Bt} = -\frac{5}{"8"}$ e.g. which is not possible or cannot be solved or you cannot find the log of a negative number	B1
		(1)
		(7 marks)

8(a)	$\tan 3x \equiv \tan(2x+x) \equiv \frac{\tan 2x + \tan x}{1 - \tan 2x \tan x}$ <p style="text-align: center;">or e.g.</p> $\tan 3x \equiv \frac{\sin 3x}{\cos 3x} \equiv \frac{\sin(2x+x)}{\cos(2x+x)} \equiv \frac{\sin 2x \cos x + \cos 2x \sin x}{\cos 2x \cos x - \sin 2x \sin x} \equiv \frac{\tan 2x + \tan x}{1 - \tan 2x \tan x}$	M1
	$\frac{\tan 2x + \tan x}{1 - \tan 2x \tan x} \equiv \frac{\frac{2 \tan x}{1 - \tan^2 x} + \tan x}{1 - \frac{2 \tan x}{1 - \tan^2 x} \tan x}$	dM1
	$\frac{\frac{2 \tan x}{1 - \tan^2 x} + \tan x}{1 - \frac{2 \tan x}{1 - \tan^2 x} \tan x} \equiv \frac{2 \tan x + \tan x - \tan^3 x}{1 - \tan^2 x - 2 \tan^2 x}$ $\frac{3 \tan x - \tan^3 x}{1 - 3 \tan^2 x} *$	A1*
		(3)

(b)	$\frac{3 \tan \theta - \tan^3 \theta}{1 - 3 \tan^2 \theta} = 2 \sec^2 3\theta - 8 \Rightarrow \tan 3\theta = 2 \sec^2 3\theta - 8$ $\Rightarrow \tan 3\theta = 2(1 + \tan^2 3\theta) - 8$	M1
	$\Rightarrow 2 \tan^2 3\theta - \tan 3\theta - 6 = 0 \quad \text{or e.g.} \Rightarrow 2 \tan^2 3\theta - \tan 3\theta = 6$	A1
	$(2 \tan 3\theta + 3)(\tan 3\theta - 2) = 0 \Rightarrow \tan 3\theta = -\frac{3}{2}, 2$ $\tan 3\theta = -\frac{3}{2} \Rightarrow 3\theta = \dots \Rightarrow \theta = \dots \quad \text{or} \quad \tan 3\theta = 2 \Rightarrow 3\theta = \dots \Rightarrow \theta = \dots$	dM1
	$\theta = 0.37, 0.72, 1.42$	A1A1
		(5)
		Total 8

7.(a)	States or implies that $A = 2500$	B1
	$10000 = 2500e^{k \times 8} \Rightarrow 8k = \ln 4 \Rightarrow k = \dots$ $\Rightarrow k = \frac{1}{8} \ln 4 \quad \text{or awrt } 0.1733$	M1 A1
		(3)
(b)	$\frac{dN}{dt} = 60000 \times -0.6e^{-0.6 \times 5} = -1792$ <p style="text-align: right;">So decrease is 1790</p>	M1, A1
(c)	$60000e^{-0.6t} = 2500e^{0.1733t}$ $24 = e^{0.1733t + 0.6t} \Rightarrow 0.1733t + 0.6t = \ln 24 \Rightarrow t = \dots$ $T = 4.11$	M1 dM1 A1
		(3)
		8 marks

Question Number	Scheme	Marks
9(a)	$4 \sin \theta \cos \theta = 2 \sin 2\theta$	B1
	e.g. $\Rightarrow 6 \sin^2 \theta \cot 2\theta + 2 \sin 2\theta = (3 - 3 \cos 2\theta) \frac{\cos 2\theta}{\sin 2\theta} + 2 \sin 2\theta$	M1A1 (3)
(b)	$3 \cot 2\theta - 14 = 6 \sin^2 \theta \cot 2\theta + 4 \sin \theta \cos \theta$	
	e.g. $\Rightarrow 3 \cot 2\theta \sin 2\theta - 14 \sin 2\theta = (3 - 3 \cos 2\theta) \cos 2\theta + 2 \sin^2 2\theta$	M1
	$\Rightarrow -14 \sin 2\theta = -3(1 - \sin^2 2\theta) + 2 \sin^2 2\theta$	M1
	$5 \sin^2 2\theta + 14 \sin 2\theta - 3 = 0$ *	A1*
		(3)
(c)	$(\sin 2x =) \frac{1}{5} \Rightarrow x = \dots$	M1
	$x = \text{awrt } 5.8^\circ, \text{ awrt } 84.2^\circ$	A1A1
		(3)
		(9 marks)

10(a)(i)	$(y=)10+k$	B1
(ii)	$x = \frac{10}{k}$ or $y = k$	B1
	$x = \frac{10}{k}$ and $y = k$	B1
		(3)

(b)	$kx - 10 + k = 2k \Rightarrow x = \dots$ or $-kx + 10 + k = 2k \Rightarrow x = \dots$	M1
	$kx - 10 + k = 2k \Rightarrow x = \dots$ and $-kx + 10 + k = 2k \Rightarrow x = \dots$	dM1
	$x = \frac{10-k}{k}$ or $x = \frac{10+k}{k}$ oe	A1
		(3)

(c)	$k > 3$	B1
	Maximum value of k occurs when $y = 3x + 1$ passes through vertex e.g. when " k " = $3 \times \frac{10}{k} + 1 \Rightarrow k = \dots$	M1
	See below for alternative approaches.	
	$k^2 - k - 30 = 0 \Rightarrow (k+5)(k-6) = 0 \Rightarrow k = 6$	A1
	So maximum k is 6 $3 < k < 6$	A1
		(4)
		Total 10

$$f(x) = 2\sec x + 6x - 3$$

1. (a)

$$f(0.1) = -0.39 \quad f(0.2) = 0.24$$

States change of sign, continuous and hence root

M1

A1

(2)

(b)

Sets $f(x) = 0$, uses $\sec x = \frac{1}{\cos x}$ and makes x of $6x$ the subject

$$\Rightarrow 6x = 3 - \frac{2}{\cos x} \Rightarrow x = \frac{1}{2} - \frac{1}{3 \cos x}^*$$

B1*

(1)

(c)

(i) $x_2 = \frac{1}{2} - \frac{1}{3 \cos 0.15} = 0.16..$

$x_2 = \text{awrt } 0.1629$

(ii) $\alpha = 0.1622$

M1

A1

A1

(3)

(6 marks)