

7 (a)	$\sqrt{2} \sin(x + 45^\circ) = \cos(x - 60^\circ)$ $\sqrt{2}(\sin x \cos 45^\circ + \cos x \sin 45^\circ) = \cos x \cos 60^\circ + \sin x \sin 60^\circ$ $\sin x + \cos x = \frac{1}{2} \cos x + \frac{\sqrt{3}}{2} \sin x$ $\cos x = (\sqrt{3} - 2) \sin x$ $\tan x \left(= \frac{1}{\sqrt{3} - 2} = \frac{\sqrt{3} + 2}{-1} \right) = -2 - \sqrt{3} *$	M1 A1 M1 A1*	(4)
(b)	<p>States or uses $x + 45^\circ = 2\theta$ o.e.</p> <p>Proceeds from e.g. $\tan(2\theta - 45^\circ) = -2 - \sqrt{3} \Rightarrow 2\theta - 45^\circ = 105^\circ, 285^\circ$</p> <p>Correct order of operations to find one angle</p> $\theta = 75^\circ, 165^\circ$	B1 M1 dM1 A1	(4)

Question Number	Scheme	Marks	
8 (i)	<p>States or uses $\operatorname{cosec} \theta = \frac{1}{\sin \theta}$</p> <p>Uses both $\operatorname{cosec} \theta = \frac{1}{\sin \theta}$ and $\sin 2\theta = 2 \sin \theta \cos \theta$</p> $3 \operatorname{cosec} \theta = 8 \cos \theta \Rightarrow \sin 2\theta = \frac{3}{4}$ $\Rightarrow \theta = \frac{1}{2} \arcsin\left(\frac{3}{4}\right) = \text{awrt } 0.424, \text{awrt } 1.15$	B1 M1 A1 M1 A1	(5)
(ii)	$\frac{\tan 2x - \tan 70^\circ}{1 + \tan 2x \tan 70^\circ} = -\frac{3}{8} \Rightarrow \tan(2x - 70^\circ) = -\frac{3}{8}$ <p>Correct order of operations $x = \frac{\arctan\left(-\frac{3}{8}\right) + 70^\circ}{2}$</p> <p style="text-align: center;">awrt 24.7°, awrt 114.7°</p>	M1 A1 dM1 A1	(4)
(9 marks)			

2(a)	$R = 25$	B1
	$\tan \alpha = \frac{24}{7} \Rightarrow \alpha = \dots$	M1
	$\alpha = 1.287$	A1
	(3)	
(b)(i)	$\text{Min} = \frac{5}{90 - 3 \times "25" \times (-1)}$	M1
	$= \frac{1}{33}$	A1
(b)(ii)	$(2x + "1.287") = \pi, \dots \Rightarrow x = \dots$	M1
	$\Rightarrow x = \frac{\pi - "1.287"}{2} = 0.927$	A1
(4)		
Total 7		