

<p>6 (a)</p>	$y = \frac{4x+3}{x-2} \Rightarrow yx - 2y = 4x + 3$ $\Rightarrow yx - 4x = 2y + 3$ $\Rightarrow x = \frac{2y+3}{y-4} \Rightarrow f^{-1}(x) = \frac{2x+3}{x-4}$	$y = 4 + \frac{11}{x-2} \Rightarrow y - 4 = \frac{11}{x-2}$ $x - 2 = \frac{11}{y-4}$ $\Rightarrow x = 2 + \frac{11}{y-4} \Rightarrow f^{-1}(x) = 2 + \frac{11}{x-4}$	<p>M1</p> <p>A1</p> <p>B1</p> <p>(3)</p>
<p>(b)</p>	$ff(x) = \frac{4 \times \frac{4x+3}{x-2} + 3}{\frac{4x+3}{x-2} - 2} \quad \text{or} \quad ff(x) = 4 + \frac{11}{4 + \frac{11}{x-2} - 2}$ $= \frac{4 \times (4x+3) + 3(x-2)}{4x+3 - 2(x-2)} = \frac{19x+6}{2x+7}$		<p>M1</p> <p>dM1 A1</p> <p>(3)</p>
<p>(c)</p>	<p>Either $x = 1$ or $y = 38$ (1, 38)</p>		<p>M1</p> <p>A1</p> <p>(2)</p> <p>(8 marks)</p>

<p>7.(a)</p>	<p>States or implies that $A = 2\,500$</p> $10\,000 = 2\,500e^{k \times 8} \Rightarrow 8k = \ln 4 \Rightarrow k = \dots$ $\Rightarrow k = \frac{1}{8} \ln 4 \text{ or awrt } 0.1733$	<p>B1</p> <p>M1</p> <p>A1</p> <p>(3)</p>
<p>(b)</p>	$\frac{dN}{dt} = 60\,000 \times -0.6e^{-0.6 \times 5} = -1792$ <p>So decrease is 1790</p>	<p>M1, A1</p> <p>(2)</p>
<p>(c)</p>	$60\,000e^{-0.6t} = 2\,500e^{0.1733t}$ $24 = e^{0.1733t + 0.6t} \Rightarrow 0.1733t + 0.6t = \ln 24 \Rightarrow t = \dots$ <p>$T = 4.11$</p>	<p>M1</p> <p>dM1</p> <p>A1</p> <p>(3)</p> <p>8 marks</p>

<p>8(a)</p>	<p>Starting with the LHS: $2\operatorname{cosec}^2 2\theta (1 - \cos 2\theta) = \frac{2 - 2\cos 2\theta}{\sin^2 2\theta}$</p> $= \frac{2 - 2(1 - 2\sin^2 \theta)}{4\sin^2 \theta \cos^2 \theta}$ $= \sec^2 \theta = 1 + \tan^2 \theta \equiv \text{RHS} \quad *$	<p>M1</p> <p>M1dM1</p> <p>A1*</p> <p>(4)</p>
<p>(b)</p>	$\sec^2 x - 3\sec x - 4 = 0 \Rightarrow \sec x = \dots$ $\cos x = \frac{1}{4} \quad (\text{ignore } -1)$ $\cos x = \frac{1}{4} \Rightarrow x = \dots$ $x = 75.5^\circ, 284.5^\circ$	<p>M1</p> <p>A1</p> <p>dM1</p> <p>A1</p> <p>(4)</p> <p>(8 marks)</p>

Question Number	Scheme	Marks
8(a)	$25 = a + -(5 \times -2 + b) (\Rightarrow 25 = a + 10 - b) \Rightarrow a = 15 + b$ *	M1A1*
		(2)
(b)	$9 = a + 10 + b \Rightarrow a = \dots$ or $b = \dots$	M1
	$a = 7, b = -8$	A1A1
		(3)
(c)	$\left(\frac{8}{5}, 7\right)$	B1ftB1
		(2)
(d)	$15 - 5x = -2x^3 + 5x^2 + 4x - 3 \Rightarrow 2x^3 - 5x^2 - 9x + 18 = 0$	M1
	$2x^3 - 5x^2 - 9x + 18 = (x+2)(2x^2 - 9x + 9)$	dM1A1
	$2x^2 - 9x + 9 = 0 \Rightarrow x = \frac{3}{2}$ (ignore $x = 3$)	ddM1
	$\left(\frac{3}{2}, \frac{15}{2}\right)$	M1A1
		(6)
		(13 marks)

9(a)	$k = -1$	B1
		(1)
(b)(i)	$f(0) = 2 - 4 \ln(0+1) = 2 - 0 = 2$	B1
(ii)	$0 = 2 - 4 \ln(x+1) \Rightarrow \ln(x+1) = \frac{1}{2} \Rightarrow x = e^{\frac{1}{2}} - 1$	M1
	$x = e^{\frac{1}{2}} - 1$	A1
		(3)
(c)	$2 - 4 \ln(x+1) = 3 \Rightarrow \ln(x+1) = \dots$ or $-2 + 4 \ln(x+1) = 3 \Rightarrow \ln(x+1) = \dots$	M1
	$2 - 4 \ln(x+1) = 3 \Rightarrow x = \dots$ and $-2 + 4 \ln(x+1) = 3 \Rightarrow x = \dots$	dM1
	CVs $e^{\frac{1}{4}} - 1, e^{\frac{5}{4}} - 1$	A1
	$-1 < x < e^{\frac{1}{4}} - 1$ or $x > e^{\frac{5}{4}} - 1$	ddM1A1ft
		(5)
		(9 marks)