

6 (a)	$y = \frac{4x+3}{x-2} \Rightarrow yx - 2y = 4x + 3$ $\Rightarrow yx - 4x = 2y + 3$	$y = 4 + \frac{11}{x-2} \Rightarrow y - 4 = \frac{11}{x-2}$ $x - 2 = \frac{11}{y-4}$	M1
	$\Rightarrow x = \frac{2y+3}{y-4} \Rightarrow f^{-1}(x) = \frac{2x+3}{x-4}$ $x \neq 4$	$\Rightarrow x = 2 + \frac{11}{y-4} \Rightarrow f^{-1}(x) = 2 + \frac{11}{x-4}$	A1
(b)	$ff(x) = \frac{4 \times \frac{4x+3}{x-2} + 3}{\frac{4x+3}{x-2} - 2}$ $= \frac{4 \times (4x+3) + 3(x-2)}{4x+3 - 2(x-2)} = \frac{19x+6}{2x+7}$	$ff(x) = 4 + \frac{11}{4 + \frac{11}{x-2} - 2}$	M1 dM1 A1 (3)
(c)	Either $x = 1$ or $y = 38$ (1, 38)		M1 A1 (2) (8 marks)

(c)	$g^{-1}(x) = e^{\frac{x-3}{2}}$	M1A1
	$x \dots 3$	B1
		(3)
(d)	$g\left(\frac{2a}{3a-5}\right) = 5 \Rightarrow 3 + 2\ln\left(\frac{2a}{3a-5}\right) = 5$	B1
	$\ln\left(\frac{2a}{3a-5}\right) = 1 \Rightarrow \frac{2a}{3a-5} = e$	M1
	$\frac{2a}{3a-5} = e \Rightarrow a = \dots$	dM1
	$a = \frac{5e}{3e-2}$	A1
		(4)

Question Number	Scheme	Marks
5(a) Way One	$\cot^2 x - \tan^2 x \equiv \frac{\cos^2 x}{\sin^2 x} - \frac{\sin^2 x}{\cos^2 x} \equiv \frac{\cos^4 x - \sin^4 x}{\sin^2 x \cos^2 x}$	M1
	$\equiv \frac{(\cos^2 x - \sin^2 x)(\cos^2 x + \sin^2 x)}{\sin^2 x \cos^2 x} \equiv \frac{\cos 2x}{\dots} \text{ or } \frac{\dots}{\left(\frac{1}{2} \sin 2x\right)^2}$	dM1
	$\equiv \frac{\cos 2x}{\left(\frac{1}{2} \sin 2x\right)^2}$	A1
	$\equiv 4 \frac{\cos 2x}{\sin 2x \sin 2x} \equiv 4 \cot 2x \operatorname{cosec} 2x^*$	A1*
	(4)	
(b)	$4 \cot 2\theta \operatorname{cosec} 2\theta = 2 \tan^2 \theta \Rightarrow \cot^2 \theta - \tan^2 \theta = 2 \tan^2 \theta \Rightarrow \cot^2 \theta - 3 \tan^2 \theta = 0$	M1
	$\cot^2 \theta - 3 \tan^2 \theta = 0 \Rightarrow \frac{1}{\tan^2 \theta} - 3 \tan^2 \theta = 0 \Rightarrow \tan^4 \theta = \frac{1}{3}$	A1
	$\tan^4 \theta = \frac{1}{3} \Rightarrow \tan \theta = \pm \sqrt[4]{\frac{1}{3}} = \pm 0.7598.. \Rightarrow \theta = \dots$	M1
	$\theta = \text{awrt } 0.65, -0.65$	A1A1
	(5)	
		Total 9

Question Number	Scheme	Marks
1(a)	$(-2, -3)$	B1
		(1)
(b)	$(-3, -9)$	B1B1
		(2)
(c)	$(-4, 3)$	B1
		(1)
		(4 marks)

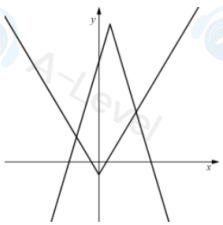
Question Number	Scheme	Marks
1(a)	$gf(1) = g\left(\frac{2(1)}{3 \times 1 + 1}\right) = 4 - \left(\frac{2(1)}{3 \times 1 + 1}\right)^2$	M1
	$= \frac{15}{4} \text{ oe}$	A1
		(2)
(b)	$f(x) \dots 0 \text{ or } f(x) < \frac{2}{3}$	B1
	$0, f(x) < \frac{2}{3}$	B1
		(2)

(c)	$y = \frac{2x}{3x+1} \Rightarrow 3xy + y = 2x \Rightarrow 3xy - 2x = -y \Rightarrow x(3y-2) = -y$ or $x = \frac{2y}{3y+1} \Rightarrow 3xy + x = 2y \Rightarrow 3xy - 2y = -x \Rightarrow y(3x-2) = -x$	M1
	$\Rightarrow f^{-1}(x) = \frac{x}{2-3x}$	A1
		(2)
(d)	$f^{-1}(x) = f(x) \text{ or } f^{-1}(x) = x \text{ or } f(x) = x$ $\frac{x}{2-3x} = \frac{2x}{3x+1} \text{ or } \frac{x}{2-3x} = x \text{ or } \frac{2x}{3x+1} = x$ $\Rightarrow x(3x+1) = 2x(2-3x) \text{ or } x = x(2-3x) \text{ or } 2x = x(3x+1)$ $\Rightarrow x = \dots$ $x = 0, \frac{1}{3}$	M1
		A1
		(2)
		Total 8

Question Number	Scheme	Marks
8 (i)	States or uses $\operatorname{cosec} \theta = \frac{1}{\sin \theta}$	B1
	Uses both $\operatorname{cosec} \theta = \frac{1}{\sin \theta}$ and $\sin 2\theta = 2 \sin \theta \cos \theta$	M1
	$3 \operatorname{cosec} \theta = 8 \cos \theta \Rightarrow \sin 2\theta = \frac{3}{4}$	A1
	$\Rightarrow \theta = \frac{1}{2} \arcsin\left(\frac{3}{4}\right) = \text{awrt } 0.424, \text{awrt } 1.15$	M1 A1
		(5)
(ii)	$\frac{\tan 2x - \tan 70^\circ}{1 + \tan 2x \tan 70^\circ} = -\frac{3}{8} \Rightarrow \tan(2x - 70^\circ) = -\frac{3}{8}$ $\text{Correct order of operations } x = \frac{\arctan\left(-\frac{3}{8}\right) + 70^\circ}{2}$ $\text{awrt } 24.7^\circ, \text{awrt } 114.7^\circ$	M1 A1
		dM1
		A1
		(4)
		(9 marks)

8(a)	Starting with the LHS: $2 \operatorname{cosec}^2 2\theta (1 - \cos 2\theta) = \frac{2 - 2 \cos 2\theta}{\sin^2 2\theta}$	M1
	$= \frac{2 - 2(1 - 2 \sin^2 \theta)}{4 \sin^2 \theta \cos^2 \theta}$	M1dM1
	$= \sec^2 \theta = 1 + \tan^2 \theta \equiv \text{RHS} \quad *$	A1*
		(4)
(b)	$\sec^2 x - 3 \sec x - 4 = 0 \Rightarrow \sec x = \dots$	M1
	$\cos x = \frac{1}{4} \text{ (ignore } -1)$	A1
	$\cos x = \frac{1}{4} \Rightarrow x = \dots$	dM1
	$x = 75.5^\circ, 284.5^\circ$	A1
		(4)
		(8 marks)

Question Number	Scheme	Marks
8(a)(i)	$\left(\frac{b}{2}, a\right)$	B1B1
(ii)	$(0, a-b)$	B1
(iii)	$\left(\frac{b-a}{2}, 0\right)$ and $\left(\frac{a+b}{2}, 0\right)$	B1B1
		(5)

(b)		B1B1
		(2)
(c)	$-x-1=2x+a-b, x=-3 \Rightarrow 2=-6+a-b$ or $x-1=a+b-2x, x=5 \Rightarrow 5-1=a+b-10$	M1
	$-x-1=2x+a-b, x=-3 \Rightarrow 2=-6+a-b$ and $x-1=a+b-2x, x=5 \Rightarrow 5-1=a+b-10$	dM1 (A1 on ePEN)
	$a-b=8$ $a+b=14 \Rightarrow a=\dots$ or $b=\dots$	ddM1
	$a=11, b=3$	A1
		(4)
		(11 marks)

Question Number	Scheme	Marks
1(a)	$f(x)$,, 9	B1
		(1)
(b)	$fg(1.5) = f\left(\frac{3}{2 \times 1.5 + 1}\right) = 9 - \left(\frac{3}{2 \times 1.5 + 1}\right)^2$ $= \frac{135}{16}$	M1
		A1
		(2)
(c)	$g(x) = \frac{3}{2x+1} \Rightarrow g^{-1}(x) = \frac{3-x}{2x}$ $0 < x$,, 3	M1 A1
		B1
		(3)
		Total 6

4.(a)	$x^2 + 0x + 1 \overline{) 3x^3 - 5x^2 + 7x - 5}$ $\underline{3x^3 + 0x^2 + 3x}$ $-5x^2 + 4x$ $\underline{-5x^2 + 0x - 5}$ $4x$ $A = 3, \quad B = -5, C = 4$ $D = 0$ * (b) $\int 3x - 5 + \frac{4x}{x^2 + 1} dx = \frac{3x^2}{2} - 5x + 2\ln(x^2 + 1) + c$ $\text{Area} = \left(\frac{3 \times 3^2}{2} - 5 \times 3 + 2\ln(3^2 + 1) \right) - \left(\frac{3 \times 2^2}{2} - 5 \times 2 + 2\ln(2^2 + 1) \right)$ $= \frac{5}{2} + \ln 4$	M1 B1, A1 A1* (4) M1, A1ft dM1, A1 (4) (8 marks)
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