

5(i)	$\cos 6x = 1 - 2 \sin^2 3x \Rightarrow \sin^2 3x = \frac{1}{2} - \frac{1}{2} \cos 6x$	M1
	$\int \sin^2 3x \, dx = \int \left(\frac{1}{2} - \frac{1}{2} \cos 6x \right) dx$	
	$= \frac{1}{2} x - \frac{1}{12} \sin 6x (+c)$	A1
		(2)
(ii)	$\int x(x^2 + 4)^{\frac{3}{2}} \, dx = \frac{1}{5} (x^2 + 4)^{\frac{5}{2}} (+c)$	M1A1
		(2)
		Total 4

3(a)	$(\cos 2A \equiv) \cos A \cos A - \sin A \sin A \equiv \cos^2 A - (1 - \cos^2 A)$	M1
	$\Rightarrow \cos 2A \equiv 2 \cos^2 A - 1 \quad *$	A1 *
		(2)
(b)	$\int (3 - 2 \cos 6x) \, dx = 3x - \frac{\sin 6x}{3} (+c)$	M1A1
	$\left[3x - \frac{\sin 6x}{3} \right]_{\frac{\pi}{12}}^{\frac{\pi}{8}} = \left(3 \left(\frac{\pi}{8} \right) - \frac{\sin \left(6 \times \frac{\pi}{8} \right)}{3} \right) - \left(3 \left(\frac{\pi}{12} \right) - \frac{\sin \left(6 \times \frac{\pi}{12} \right)}{3} \right) = \frac{1}{8} \pi + \frac{2 - \sqrt{2}}{6}$	dM1A1
		(4)
		(6 marks)

3 (i)	$\frac{d}{dx} \ln(\sin^2 3x) = \frac{1}{\sin^2 3x} \times 2 \sin 3x \times 3 \cos 3x = 6 \cot 3x$	M1 A1 (2)
(ii) (a)	$\frac{d}{dx} (3x^2 - 4)^6 = 36x (3x^2 - 4)^5$	M1 A1 (2)
(b)	$\int x (3x^2 - 4)^5 \, dx = \frac{1}{36} (3x^2 - 4)^6$	B1ft
	$\int_0^{\sqrt{2}} x (3x^2 - 4)^5 \, dx = \left[\frac{1}{36} (3x^2 - 4)^6 \right]_0^{\sqrt{2}} = \frac{1}{36} (2)^6 - \frac{1}{36} (-4)^6 = -112$	M1 A1cso (3) (7 marks)

Question Number	Scheme	Marks
6 (a)	$y = (4x-7)^{\frac{1}{2}} \Rightarrow \left(\frac{dy}{dx} = \right) 2(4x-7)^{-\frac{1}{2}} \quad (\text{see notes})$ At $(8, 5)$ gradient of tangent is $2(4 \times 8 - 7)^{-\frac{1}{2}} \left(= \frac{2}{5} \right)$ Equation for l is $y - 5 = -\frac{5}{2}(x - 8)$ $2y - 10 = -5x + 40 \Rightarrow 5x + 2y - 50 = 0 \quad *$	M1 A1 dM1 ddM1 A1* (5)
(b)	$\int (4x-7)^{\frac{1}{2}} dx = \left[\frac{(4x-7)^{\frac{3}{2}}}{6} \right] \quad (\text{see notes})$ $\text{Complete area} = \int_{\frac{7}{4}}^8 (4x-7)^{\frac{1}{2}} dx = \left[\frac{(4x-7)^{\frac{3}{2}}}{6} \right]_{\frac{7}{4}}^8 + 5$ $= \frac{155}{6}$	M1, A1 dM1 A1 (4) (9 marks)