

1	$3 \tan^2 \theta + 7 \sec \theta - 3 = 0 \Rightarrow 3(\sec^2 \theta - 1) + 7 \sec \theta - 3 = 0$	M1
	$3 \sec^2 \theta + 7 \sec \theta - 6 = 0$	A1
	$(3 \sec \theta - 2)(\sec \theta + 3) = 0 \Rightarrow \sec \theta = \dots \Rightarrow \cos \theta = \dots$	dM1
	$\theta = 109.5^\circ, 250.5^\circ$	A1, A1
		(5)

6 (a)	$y = \frac{4x+3}{x-2} \Rightarrow yx - 2y = 4x + 3$ $\Rightarrow yx - 4x = 2y + 3$ $\Rightarrow x = \frac{2y+3}{y-4} \Rightarrow f^{-1}(x) = \frac{2x+3}{x-4}$	$y = 4 + \frac{11}{x-2} \Rightarrow y - 4 = \frac{11}{x-2}$ $x - 2 = \frac{11}{y-4}$ $\Rightarrow x = 2 + \frac{11}{y-4} \Rightarrow f^{-1}(x) = 2 + \frac{11}{x-4}$	M1
	$x \neq 4$		A1
(b)	$ff(x) = \frac{4 \times \frac{4x+3}{x-2} + 3}{\frac{4x+3}{x-2} - 2}$ or $ff(x) = 4 + \frac{11}{4 + \frac{11}{x-2} - 2}$ $= \frac{4 \times (4x+3) + 3(x-2)}{4x+3 - 2(x-2)} = \frac{19x+6}{2x+7}$		B1 (3)
(c)	Either $x = 1$ or $y = 38$ (1, 38)		M1 A1 (2)
(8 marks)			

4.(a)	$\begin{array}{r} 3x-5 \\ x^2+0x+1 \overline{) 3x^3-5x^2+7x-5} \\ \underline{3x^3+0x^2+3x} \\ -5x^2+4x \\ \underline{-5x^2+0x-5} \\ 4x \end{array}$	M1
	$A=3, B=-5, C=4$ $D=0$ *	B1, A1 A1* (4)
(b)	$\int 3x - 5 + \frac{4x}{x^2+1} dx = \frac{3x^2}{2} - 5x + 2 \ln(x^2+1) + c$ $\text{Area} = \left(\frac{3 \times 3^2}{2} - 5 \times 3 + 2 \ln(3^2+1) \right) - \left(\frac{3 \times 2^2}{2} - 5 \times 2 + 2 \ln(2^2+1) \right)$ $= \frac{5}{2} + \ln 4$	M1, A1ft dM1, A1 (4) (8 marks)

10(a)(i)	$(y=)10+k$	B1
(ii)	$x = \frac{10}{k}$ or $y = k$	B1
	$x = \frac{10}{k}$ and $y = k$	B1
		(3)

(b)	$kx - 10 + k = 2k \Rightarrow x = \dots$ or $-kx + 10 + k = 2k \Rightarrow x = \dots$	M1
	$kx - 10 + k = 2k \Rightarrow x = \dots$ and $-kx + 10 + k = 2k \Rightarrow x = \dots$	dM1
	$x, \frac{10-k}{k}$ or $x \dots \frac{10+k}{k}$ oe	A1
		(3)

(c)	$k > 3$	B1
	Maximum value of k occurs when $y = 3x + 1$ passes through vertex e.g. when " k " = $3 \times \frac{10}{k} + 1 \Rightarrow k = \dots$	M1
	See below for alternative approaches.	
	$k^2 - k - 30 = 0 \Rightarrow (k+5)(k-6) = 0 \Rightarrow k = 6$ So maximum k is 6	A1
	$3 < k < 6$	A1
		(4)
		Total 10

7 (a)	$\sqrt{2} \sin(x + 45^\circ) = \cos(x - 60^\circ)$ $\sqrt{2}(\sin x \cos 45^\circ + \cos x \sin 45^\circ) = \cos x \cos 60^\circ + \sin x \sin 60^\circ$ $\sin x + \cos x = \frac{1}{2} \cos x + \frac{\sqrt{3}}{2} \sin x$ $\cos x = (\sqrt{3} - 2) \sin x$ $\tan x \left(= \frac{1}{\sqrt{3} - 2} = \frac{\sqrt{3} + 2}{-1} \right) = -2 - \sqrt{3} \quad *$	M1 A1 M1 A1* (4)
(b)	States or uses $x + 45^\circ = 2\theta$ o.e. Proceeds from e.g. $\tan(2\theta - 45^\circ) = -2 - \sqrt{3} \Rightarrow 2\theta - 45^\circ = 105^\circ, 285^\circ$ Correct order of operations to find one angle $\theta = 75^\circ, 165^\circ$	B1 M1 dM1 A1 (4)

6.(a)	$(2, -10)$	B1 B1 (2)
(b)	$ff(0) = f(-4) = \dots$ $= 8$	M1 A1cso (2)
(c)	Attempts to solve $-3(x-2) - 10 = 5x + 10 \Rightarrow x = \dots$ $x > -\frac{7}{4}$ only	M1 A1 (2)
(d)	$x \text{ (or } x) = \frac{16}{3}$ Attempts $3(x - 2) - 10 = 0 \Rightarrow x = k, k > 0$ or $3(-x - 2) - 10 = 0 \Rightarrow x = -k$ or $3(x - 2) - 10 = 0 \Rightarrow x = k \Rightarrow x = -k$ $x = \left(\frac{16}{3} \text{ and } \right) -\frac{16}{3}$ with no other values	B1 M1 A1 (3)
		(9 marks)