

5: Find

(i) $\int \sin^2 3x \, dx$ (2)

(ii) $\int x(x^2 + 4)^{\frac{3}{2}} \, dx$ (2)

3. (a) Using the identity for $\cos(A + B)$, prove that

$$\cos 2A \equiv 2 \cos^2 A - 1$$
 (2)

(b) Hence, using algebraic integration, find the exact value of

$$\int_{\frac{\pi}{12}}^{\frac{\pi}{8}} (5 - 4 \cos^2 3x) \, dx$$
 (4)

3. (i) Find $\frac{d}{dx} \ln(\sin^2 3x)$ writing your answer in simplest form. (2)

(ii)(a) Find $\frac{d}{dx} (3x^2 - 4)^6$ (2)

(b) Hence show that

$$\int_0^{\sqrt{2}} x(3x^2 - 4)^5 \, dx = R$$

where R is an integer to be found.

(Solutions relying on calculator technology are not acceptable.)

(3)

6.

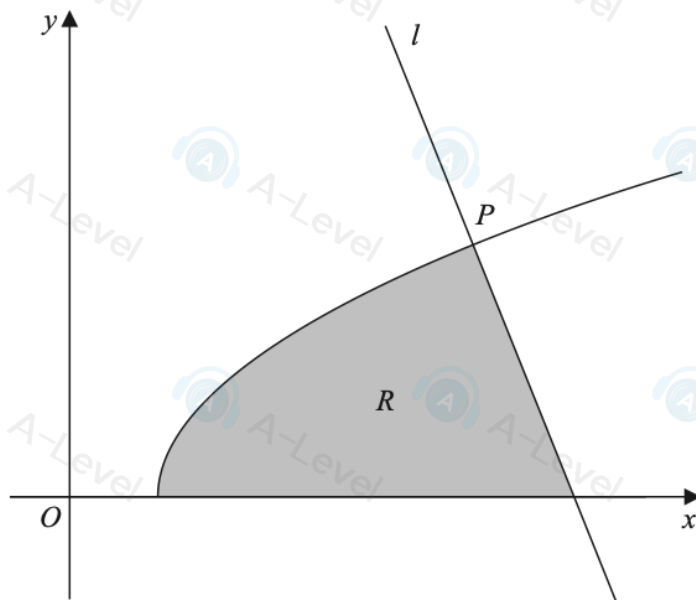


Figure 3

In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

Figure 3 shows a sketch of part of the curve with equation

$$y = \sqrt{4x - 7}$$

The line l , shown in Figure 3, is the normal to the curve at the point $P(8, 5)$

(a) Use calculus to show that an equation of l is

$$5x + 2y - 50 = 0 \quad (5)$$

The region R , shown shaded in Figure 3, is bounded by the curve, the x -axis and l .

(b) Use algebraic integration to find the exact area of R .

(4)