

Question Number	Scheme	Marks
1 (a)	$\frac{5x+10}{(1-x)(2+3x)} \equiv \frac{A}{1-x} + \frac{B}{2+3x} \Rightarrow$ Value for A or B	M1
	One correct value, either $A = 3$ or $B = 4$	A1
	Correct PF form $\frac{3}{1-x} + \frac{4}{2+3x}$	A1
		(3)
(b)(i)	$\frac{A}{1-x} = A(1-x)^{-1} = A(1+x+x^2+\dots)$	B1
	$\left\{\frac{B}{2}\right\}\left(1+\frac{3x}{2}\right)^{-1} = \left\{\frac{B}{2}\right\}\left(1+(-1)\frac{3x}{2} + \frac{(-1)(-2)}{2}\left(\frac{3x}{2}\right)^2 + \dots\right); = \frac{B}{2}\left(1-\frac{3x}{2} + \frac{9x^2}{4} + \dots\right)$	M1; A1
	$f(x) = 3 \times \left(1+x+x^2+\dots\right) + \frac{4}{2}\left(1-\frac{3x}{2} + \frac{9x^2}{4} + \dots\right)$	M1
	$= 5 + \frac{15}{2}x^2 + \dots$	A1
		(5)
(b)(ii)	$ x < \frac{2}{3}$	B1
		(1)
		(9 marks)

Question Number	Scheme	Marks
9(a)(i)	$\frac{dy}{dx} = \frac{dy/dt}{dx/dt} = \frac{3 \sin^2 t \cos t}{-4 \sin 2t}$	M1A1
	$\frac{3 \sin^2 t \cos t}{-4 \sin 2t} = \frac{3 \sin^2 t \cos t}{-8 \sin t \cos t} = -\frac{3}{8} \sin t$ <p>or e.g.</p> $\frac{3 \sin^2 t \cos t}{-4 \sin 2t} = \frac{\frac{3}{2} \sin 2t \sin t}{-4 \sin 2t} = -\frac{3}{8} \sin t$	A1
(ii)	$t = \frac{\pi}{6} \Rightarrow x = 1, y = \frac{1}{8}$	B1
	$m = -\frac{3}{8} \sin\left(\frac{\pi}{6}\right) = -\frac{3}{16} \Rightarrow y - \frac{1}{8} = -\frac{3}{16}(x - 1)$	M1
	$3x + 16y - 5 = 0 *$	A1*
		(6)
(b)	$3(2 \cos 2t) + 16(\sin^3 t) - 5 = 0$	M1
	$6(1 - 2 \sin^2 t) + 16 \sin^3 t - 5 = 0$	dM1
	$16 \sin^3 t - 12 \sin^2 t + 1 = 0$	A1
	$(2 \sin t - 1)^2 (4 \sin t + 1) = 0 \Rightarrow \sin t = -\frac{1}{4}$	ddM1
	$\sin t = -\frac{1}{4} \Rightarrow x = 2 \cos 2t = \dots \text{ and } y = \sin^3 t = \dots$	dddM1
	$Q\left(\frac{7}{4}, -\frac{1}{64}\right)$	A1
		(12 marks)

Question Number	Scheme	Marks
1 (a)	$(1+kx)^{\frac{1}{2}} = 1 + \left(\frac{1}{2}\right) \times (kx) + \frac{\left(\frac{1}{2}\right) \times \left(-\frac{1}{2}\right)}{2!} \times (kx)^2 + \frac{\left(\frac{1}{2}\right) \times \left(-\frac{1}{2}\right) \times \left(-\frac{3}{2}\right)}{3!} \times (kx)^3 \dots$	
(i)	$\frac{1}{2}k = \frac{1}{8} \Rightarrow k = \frac{1}{4}$	M1A1
(ii)	$A = \frac{\left(\frac{1}{2}\right) \times \left(-\frac{1}{2}\right)}{2!} \times "k"^{n2} = -\frac{1}{128} \quad B = \frac{\left(\frac{1}{2}\right) \times \left(-\frac{1}{2}\right) \times \left(-\frac{3}{2}\right)}{3!} \times "k"^{n3} = \frac{1}{1024}$	M1 A1 A1
(b)	Substitutes $x = 0.6 \Rightarrow \sqrt{1.15} = 1 + \frac{1}{8} \times 0.6 - \frac{1}{128} \times 0.6^2 + \frac{1}{1024} \times 0.6^3 = 1.072398$	M1 A1
		(5)
		(2)
		(7 marks)
1(b) alt	$(1+kx)^{\frac{1}{2}} = 1 + \left(\frac{1}{2}\right) \times (kx) - \left(\frac{1}{8}\right) \times (kx)^2 + \left(\frac{1}{16}\right) \times (kx)^3$ <p>Substitutes "kx" = 0.15</p> $\Rightarrow \sqrt{1.15} = 1 + \frac{1}{2} \times 0.15 - \frac{1}{8} \times 0.15^2 + \frac{1}{16} \times 0.15^3 = 1.072398$	M1A1
		(2)

Question Number	Scheme	Marks
4(a)	$\frac{1}{\sqrt{4-x^2}} = \left(4-x^2\right)^{-\frac{1}{2}} = 4^{-\frac{1}{2}} \left(1-\dots\right)$ $\left(1-\frac{1}{4}x^2\right)^{-\frac{1}{2}} = 1 + \left(-\frac{1}{2}\right) \left(-\frac{1}{4}x^2\right) + \frac{\left(-\frac{1}{2}\right) \times \left(-\frac{3}{2}\right)}{2} \left(-\frac{1}{4}x^2\right)^2 + \frac{\left(-\frac{1}{2}\right) \times \left(-\frac{3}{2}\right) \times \left(-\frac{5}{2}\right)}{3!} \left(-\frac{1}{4}x^2\right)^3$ $\frac{1}{\sqrt{4-x^2}} = \frac{1}{2} + \frac{1}{16}x^2 + \frac{3}{256}x^4 + \frac{5}{2048}x^6$	B1
		M1, A1
		A1, A1
		(5)
(b)	$ x < 2$	B1
		(1)
(c)	Substitutes an appropriate value of x in both sides with LHS in terms of $\sqrt{3}$	M1
	E.g. with $x = 1 \quad \sqrt{3} = \frac{2048}{1181}$ or $\frac{3543}{2048}$	A1
		(2)
		(8 marks)

Question Number	Scheme	Marks
1(a)	$(8-3x)^{-\frac{1}{3}} = \frac{1}{2} \left(1 - \frac{3}{8}x\right)^{-\frac{1}{3}}$	B1
	$\left(1 - \frac{3}{8}x\right)^{-\frac{1}{3}} = 1 + \left(-\frac{1}{3}\right)\left(-\frac{3}{8}x\right) + \frac{-\frac{1}{3}\left(-\frac{1}{3}-1\right)\left(-\frac{3}{8}x\right)^2}{2!} + \frac{-\frac{1}{3}\left(-\frac{1}{3}-1\right)\left(-\frac{1}{3}-2\right)\left(-\frac{3}{8}x\right)^3}{3!} + \dots$	M1
	$(8-3x)^{-\frac{1}{3}} = \frac{1}{2} + \frac{1}{16}x + \frac{1}{64}x^2 + \frac{7}{1536}x^3 + \dots$	A1 A1
		(4)
(b)	$\frac{1}{2} + \frac{1}{16}\left(\frac{2}{3}\right) + \frac{1}{64}\left(\frac{2}{3}\right)^2 + \frac{7}{1536}\left(\frac{2}{3}\right)^3 + \dots = \frac{2851}{5184} \Rightarrow \sqrt[3]{6} = \left(\frac{2851}{5184}\right)^{-1} = \dots$	M1
	$= \frac{5184}{2851}$ or $1 \frac{2333}{2851}$	A1
		(2)
		Total 6

Question Number	Scheme	Marks
4 (a)	Attempt at chain rule $y^2 \rightarrow \dots y \frac{dy}{dx}$	M1
	Attempt at product rule $2xy \rightarrow \alpha x \frac{dy}{dx} + \beta y$	M1
	Correct differentiation $8x + 2y \frac{dy}{dx} - 2y - 2x \frac{dy}{dx} = 24$ oe	A1
	Collects terms in $(2y - 2x) \frac{dy}{dx} = 24 - 8x + 2y$	M1
	$\left(\frac{dy}{dx} = \right) \frac{12 - 4x + y}{y - x}$ oe	A1
		(5)
(b)	Sets $\frac{12 - 4x + y}{y - x} = 2 \Rightarrow y = 12 - 2x$ or $x = 6 - \frac{1}{2}y$	M1
	Substitute $y = 12 - 2x$ or $x = 6 - \frac{1}{2}y$ into $4x^2 + y^2 - 2xy = 24x$	dM1
	$x^2 - 8x + 12 = 0$ oe or $y^2 - 8y = 0$	A1
	Solves $x = 6, y = 0$ or $x = 2, y = 8$	ddM1
	Chooses $a(x) = 2, b(y) = 8$ or states $(2, 8)$ only	A1
		(5)
		(10 marks)